

**LIPEI DU**

McGILL U / UC BERKELEY / LBNL

---

## **THEORY OVERVIEW ON COLLECTIVITY**

**THE 15TH WORKSHOP ON CRITICAL POINT AND ONSET OF DECONFINEMENT**

BERKELEY, CA (MAY 20, 2024)

**LIPEI DU**

McGILL U / UC BERKELEY / LBNL

---

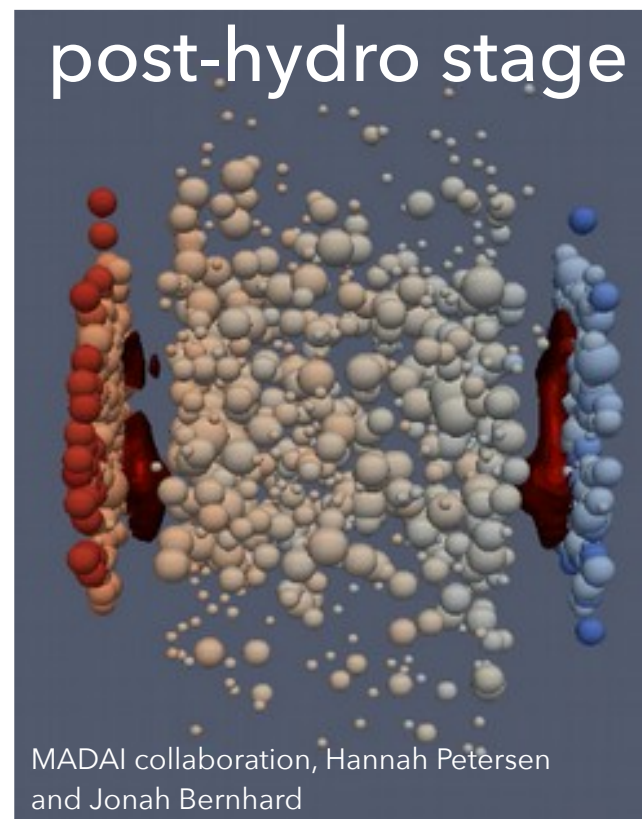
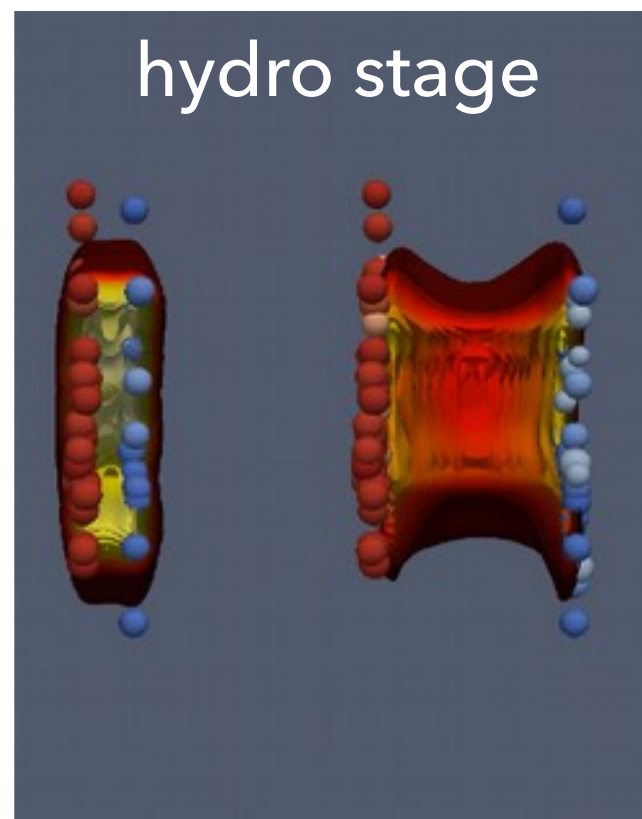
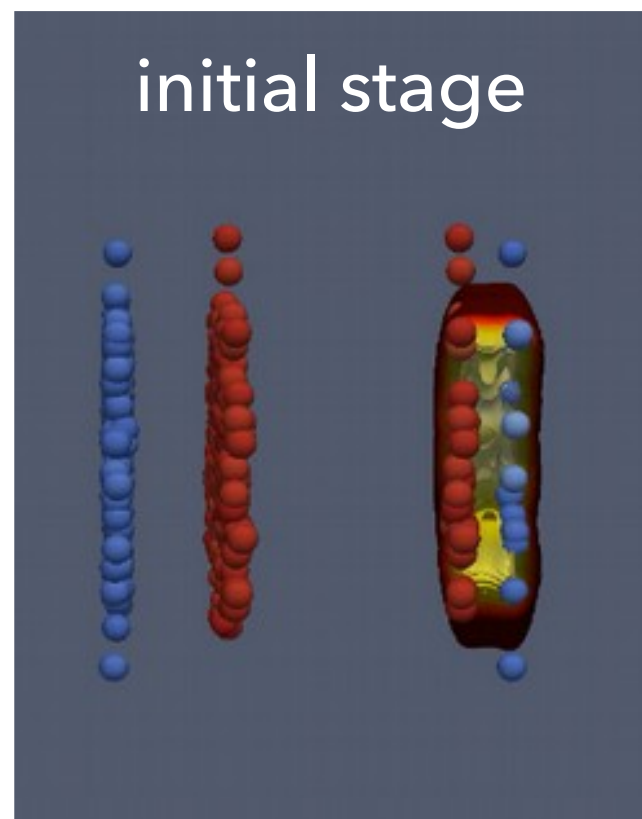
## **THEORY OVERVIEW ON COLLECTIVITY**

COLLECTIVITY IN THE BEAM DIRECTION

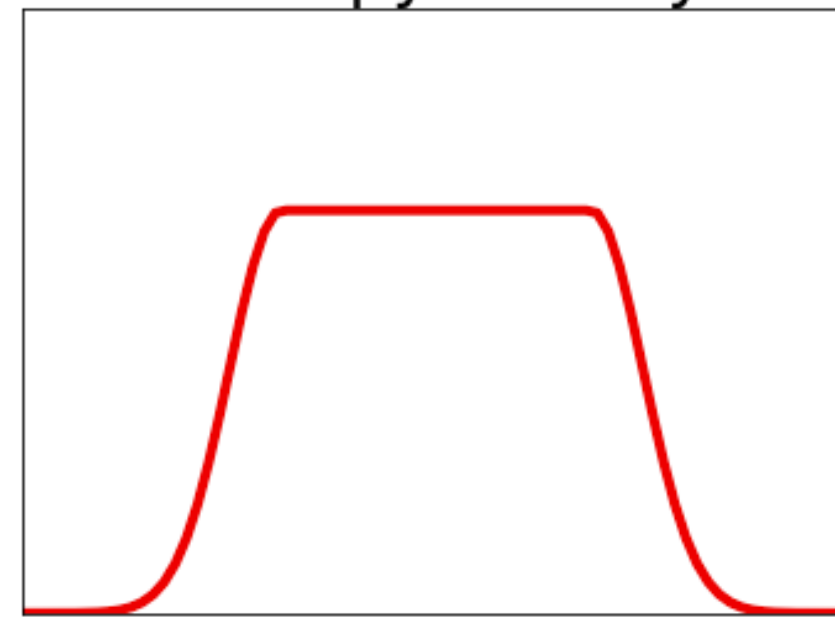
**THE 15TH WORKSHOP ON CRITICAL POINT AND ONSET OF DECONFINEMENT**

BERKELEY, CA (MAY 20, 2024)

# LONGITUDINAL DYNAMICS

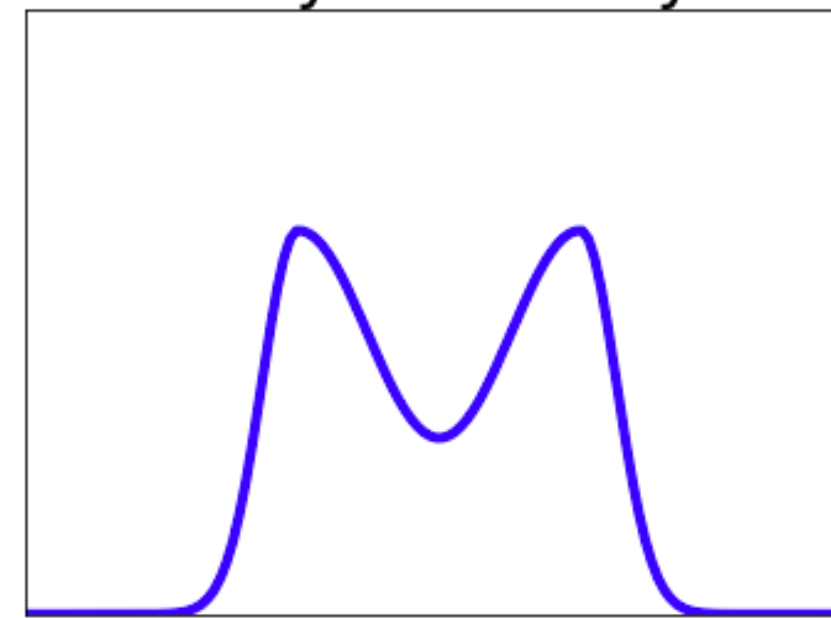


entropy density

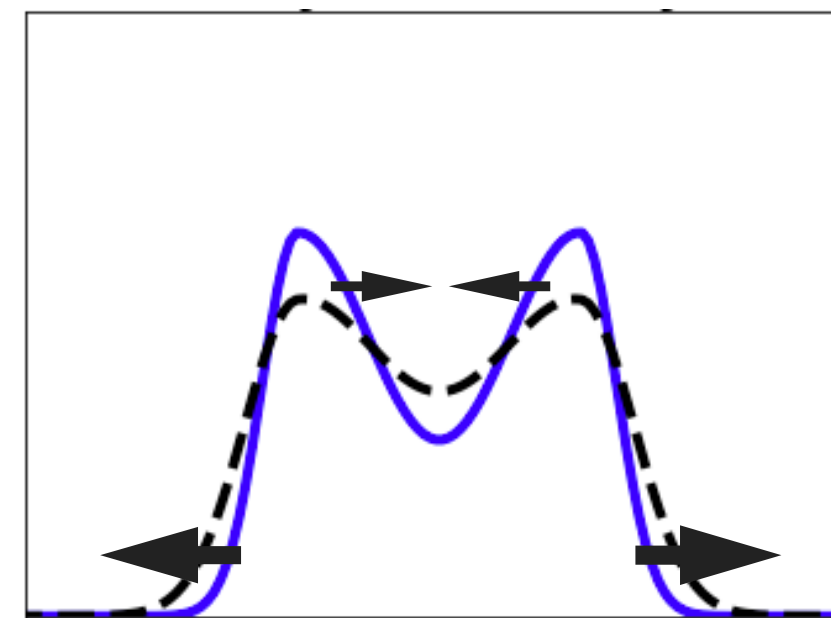
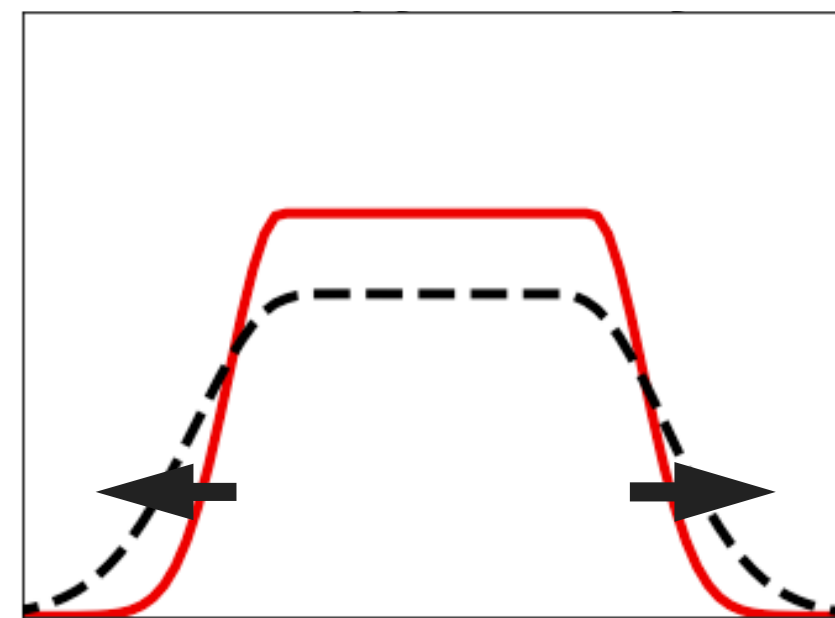


space-time rapidity

baryon density



space-time rapidity



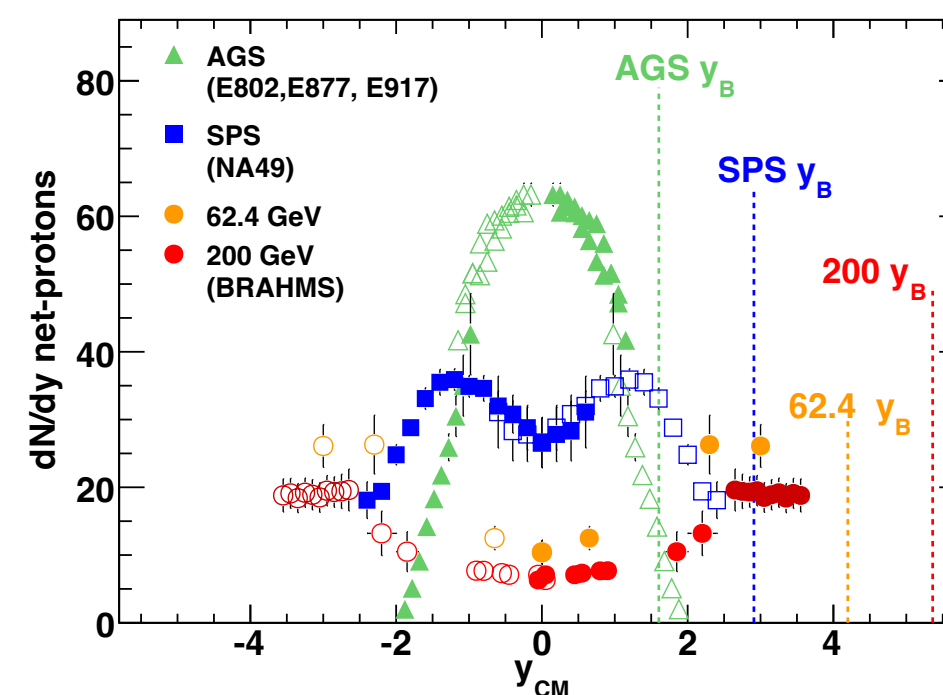
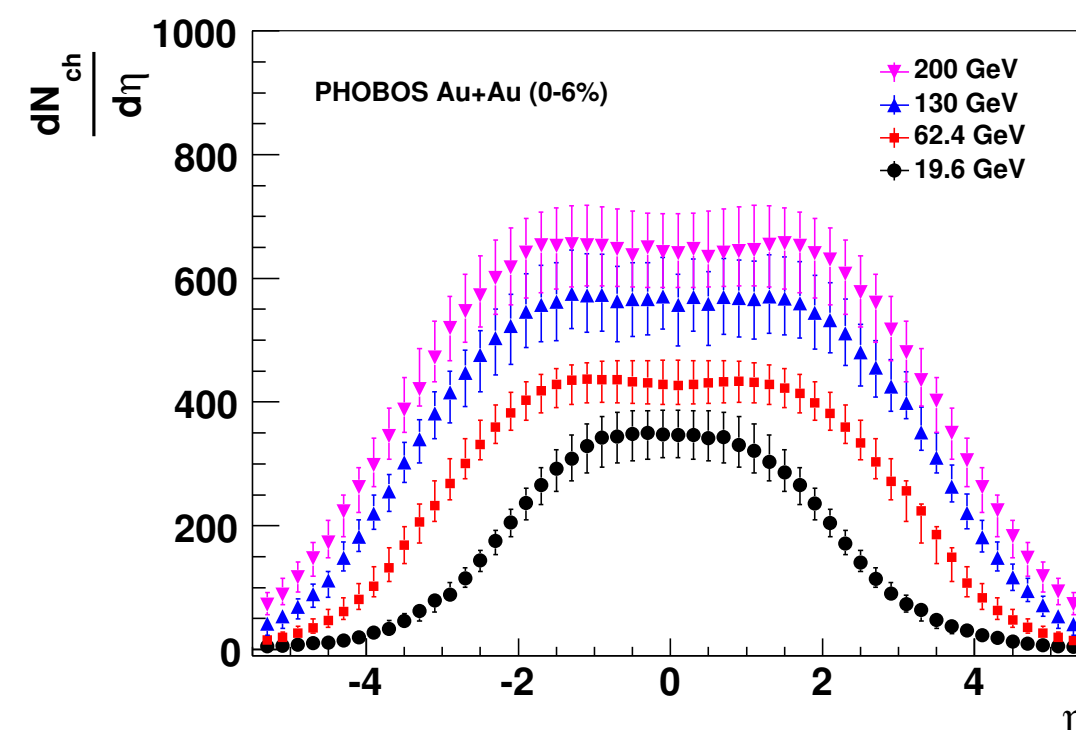
- ▶ initial energy deposition
- ▶ initial baryon stopping



- ▶ longitudinal pressure gradient  $\Rightarrow$  longitudinal flow & expansion
- ▶ baryon density gradient  $\Rightarrow$  baryon diffusion (hydro transport)

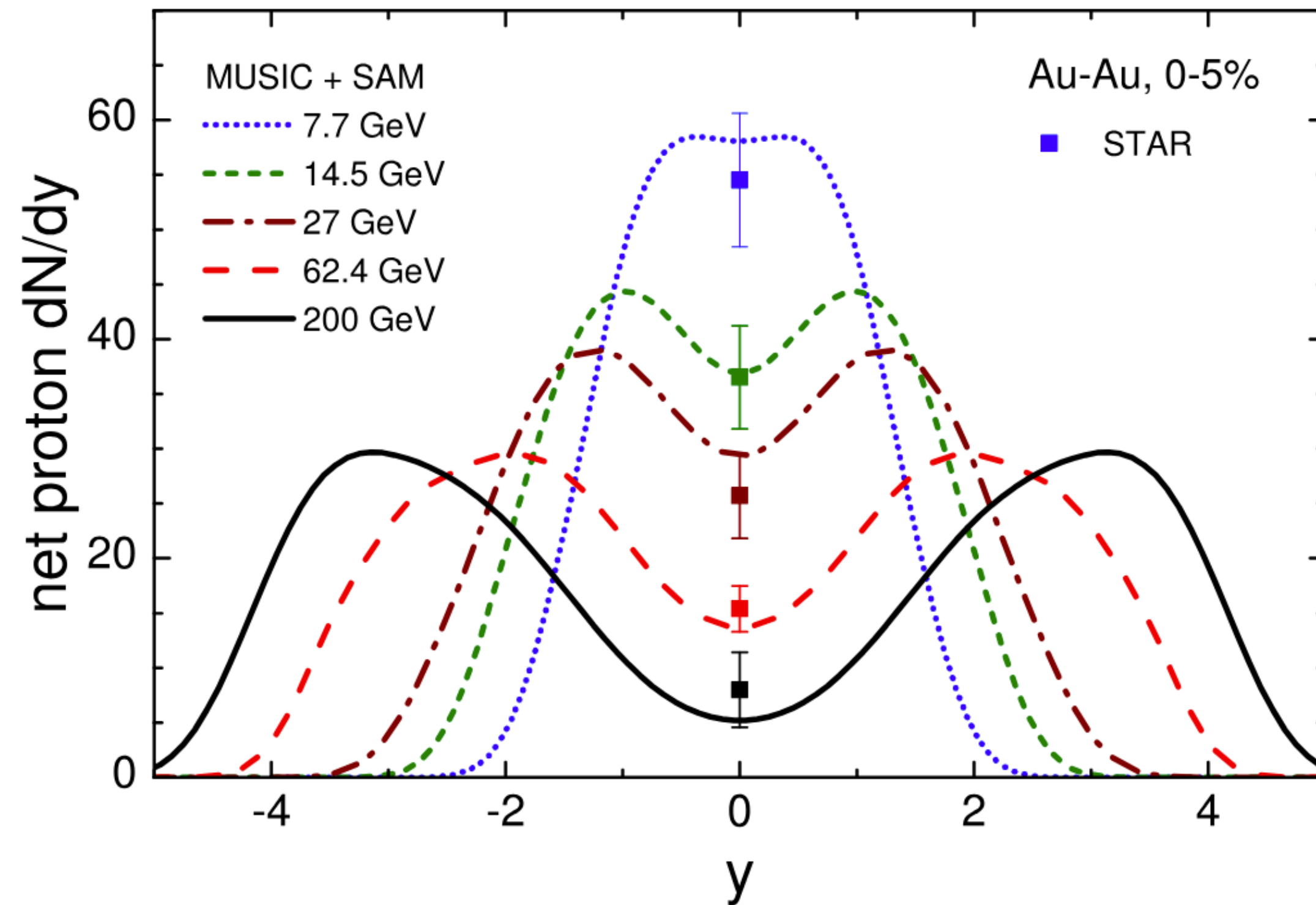


- ▶ rapidity-dependent particle distributions

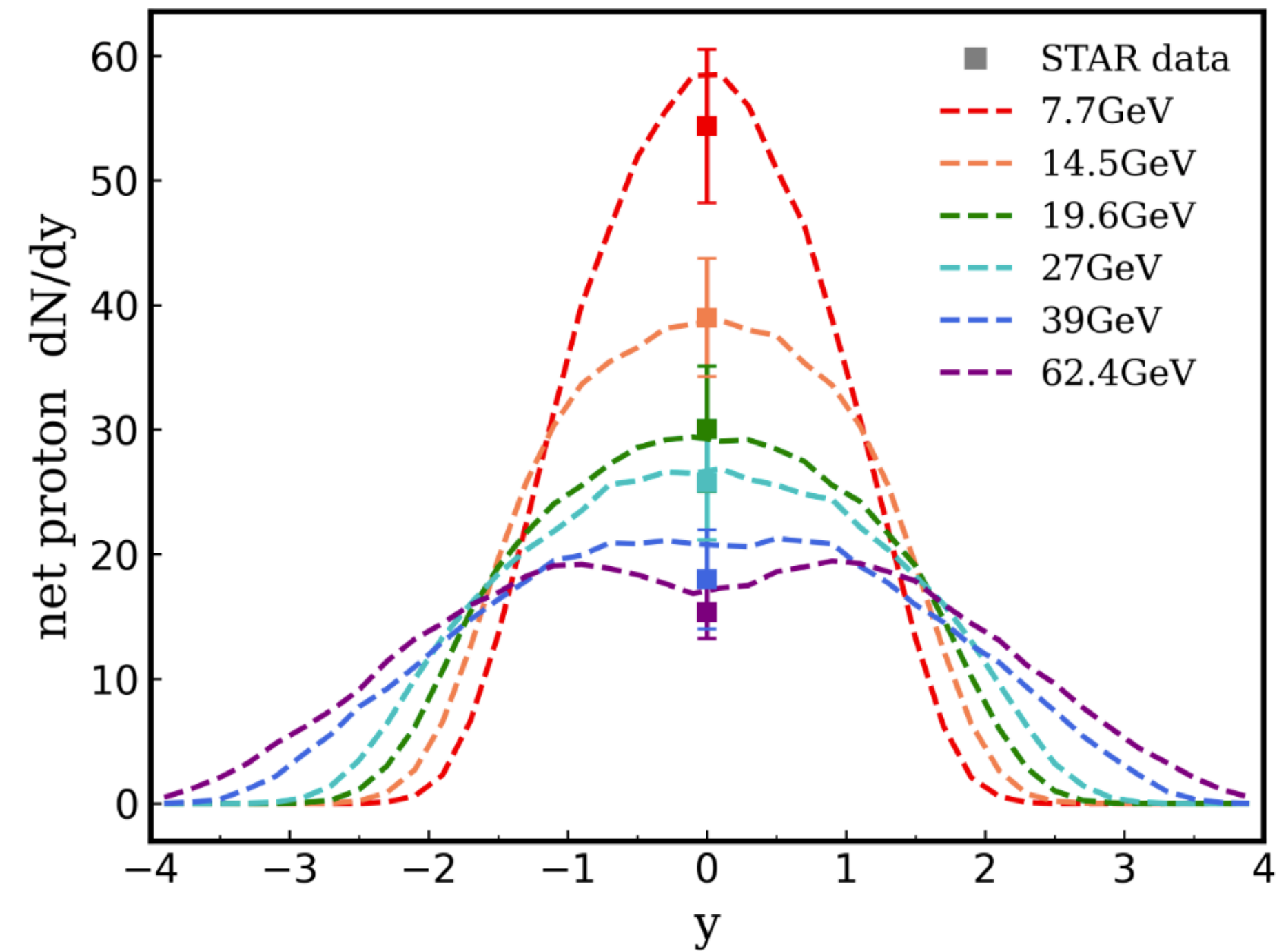


---

# **LONGITUDINAL THERMODYNAMIC PROPERTIES**



Vovchenko, Koch, and C. Shen, PRC 105, 014904 (2022)

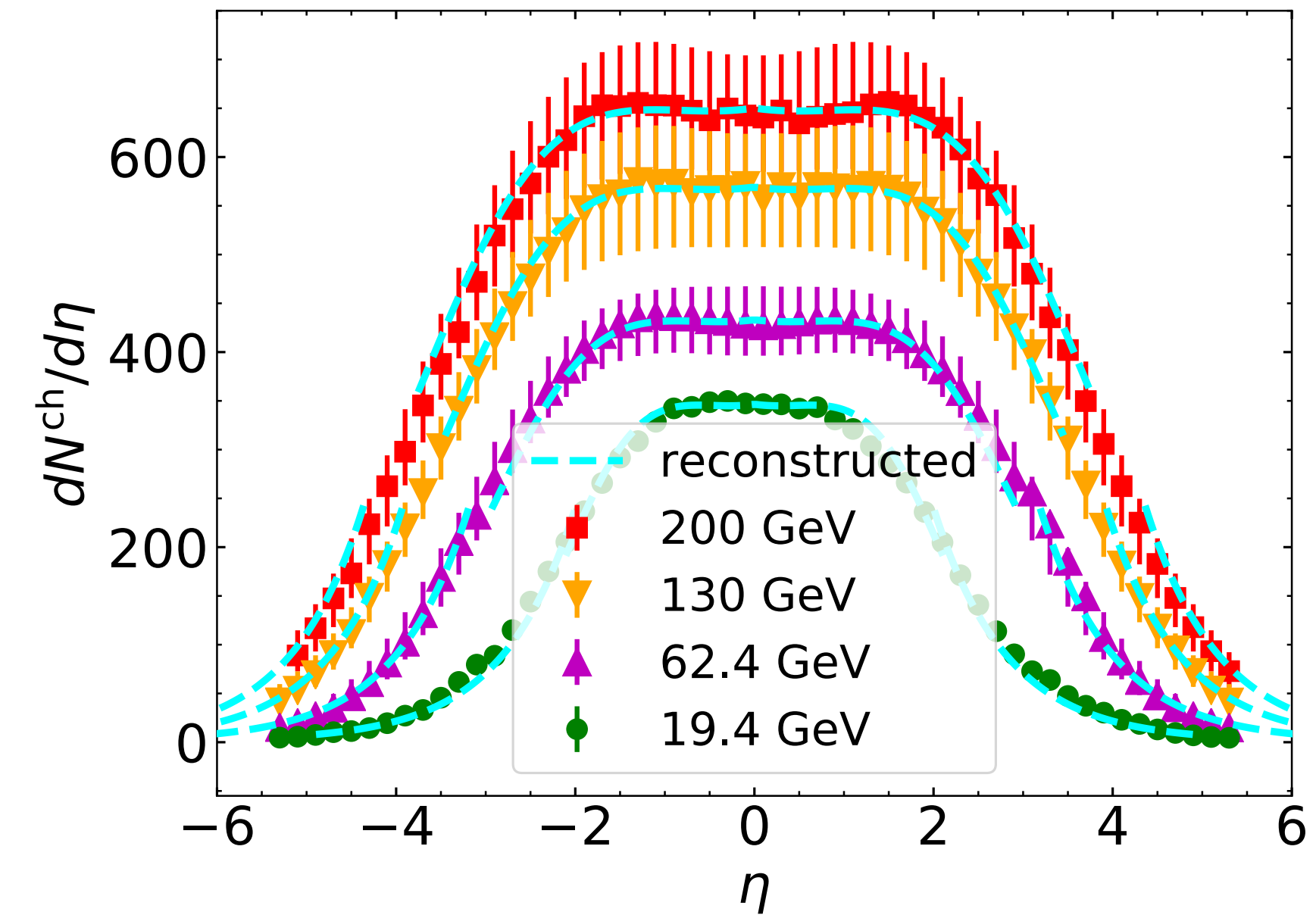
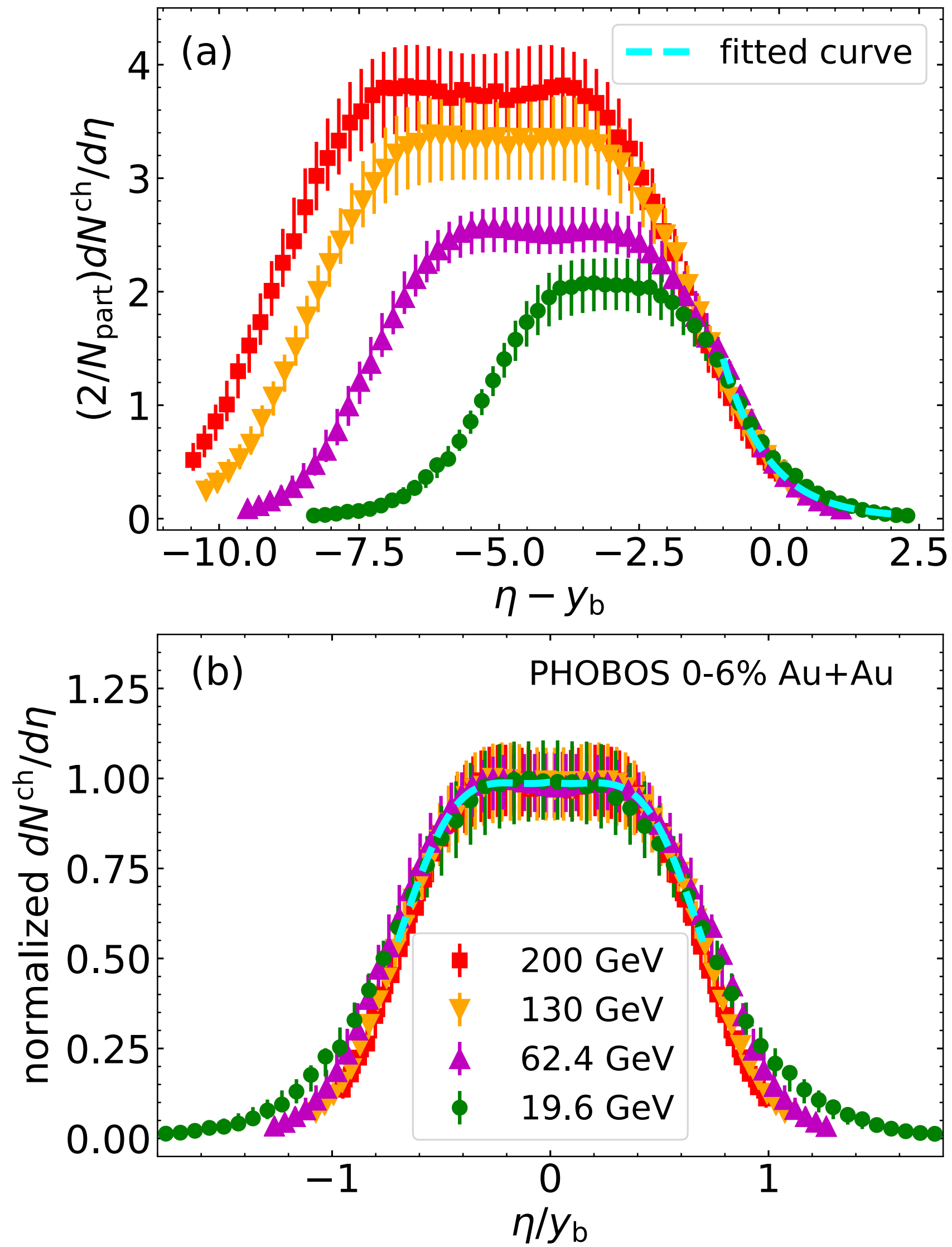


Y.-f. Shen, Chen, Wu, Xu, and Huang, 2404.02397

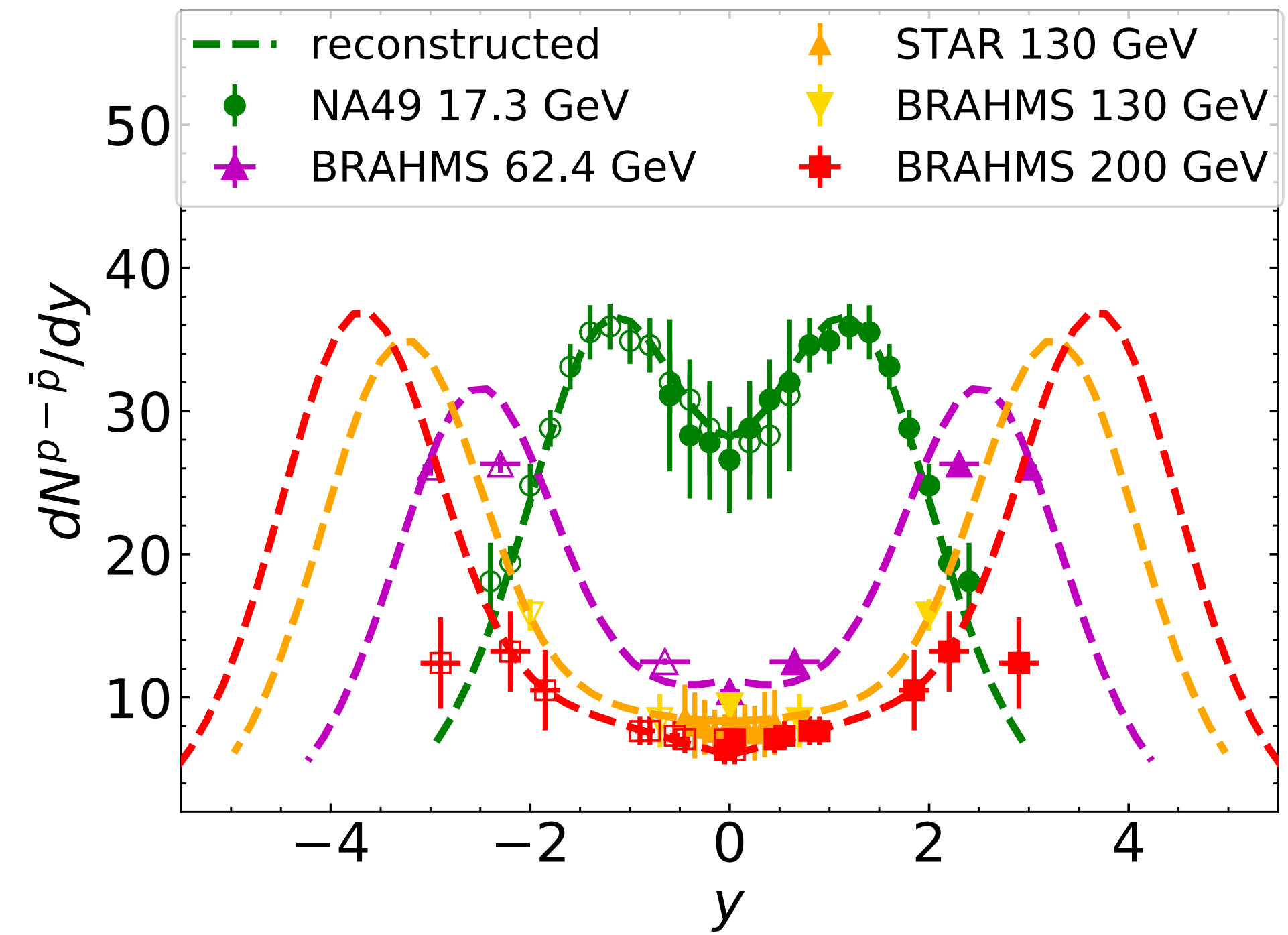
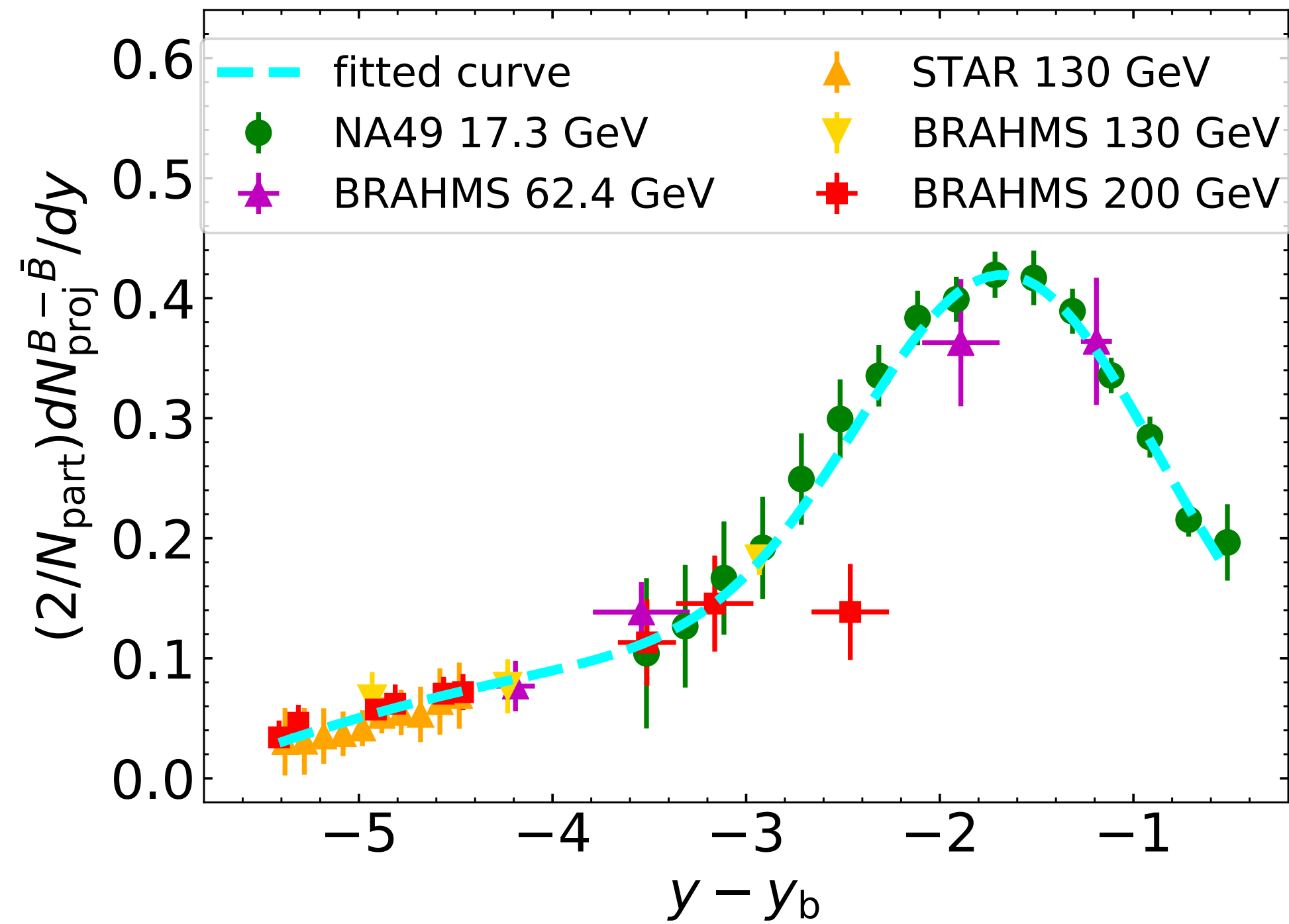
- If we only take measurements at mid-rapidity, the dynamics along the beam direction may not be well-constrained.



# CONSTRUCT RAPIDITY-DISTRIBUTION: $dN^{\text{ch}}/d\eta$

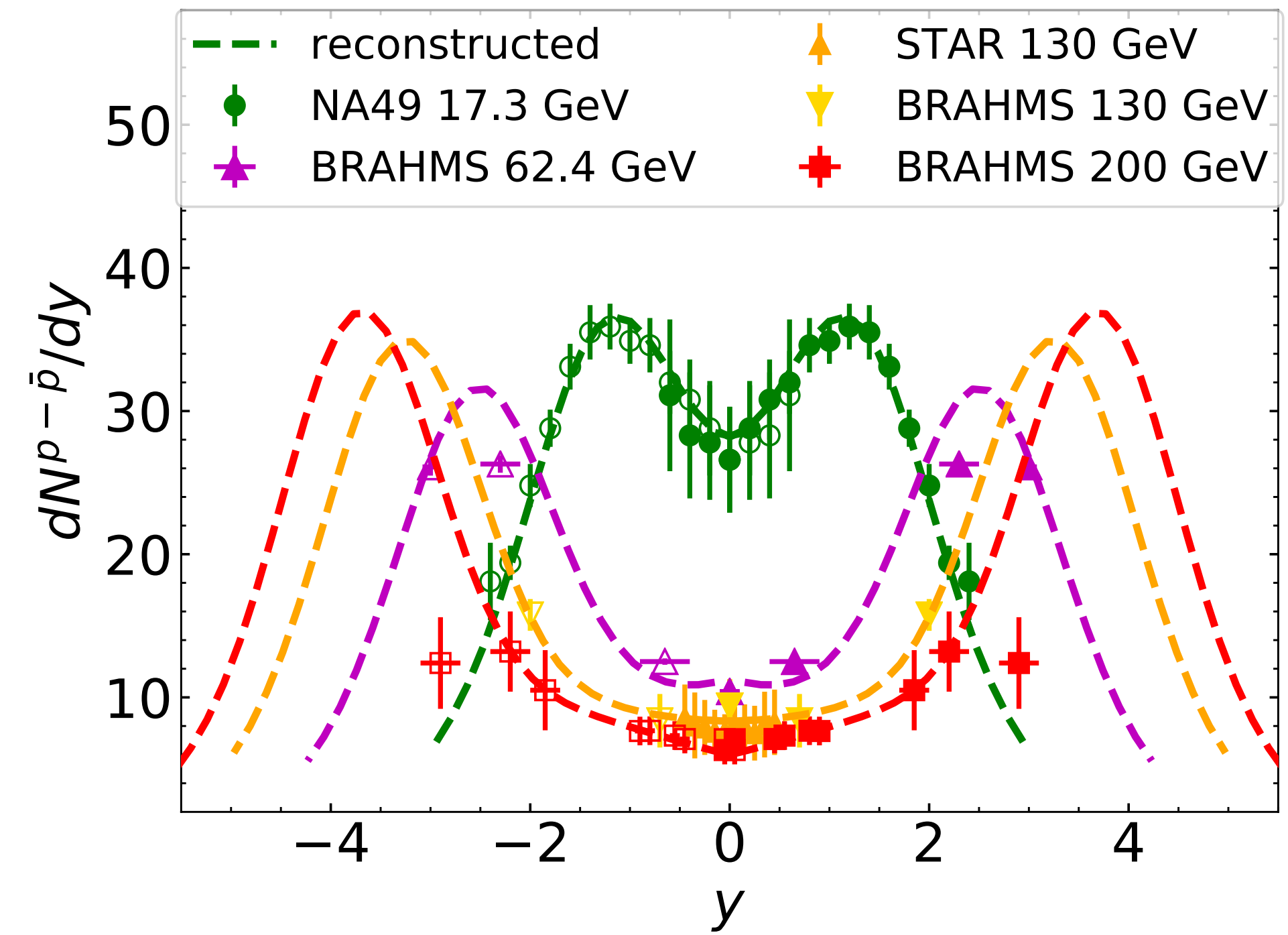
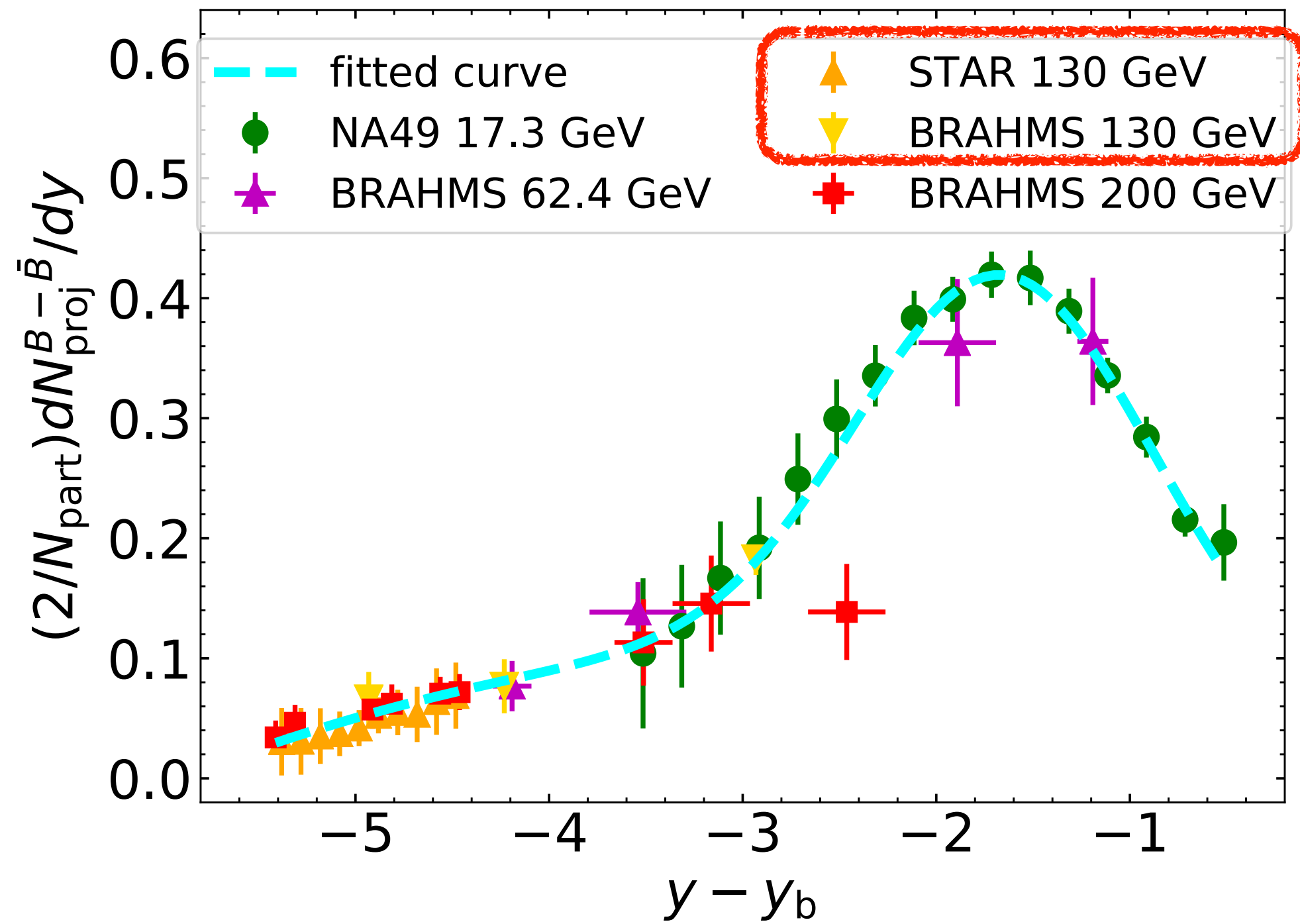


- ▶ Fit two regions separately: [Lipei Du, arXiv: 2401.00596](https://arxiv.org/abs/2401.00596)
  - ▶ forward-rapidity: limiting fragmentation
  - ▶ mid-rapidity: central plateau
- ▶ The fitted curves can be used to reconstruct  $dN^{\text{ch}}/d\eta$ , even at energies that were not directly measured.



Lipei Du, arXiv: 2401.00596

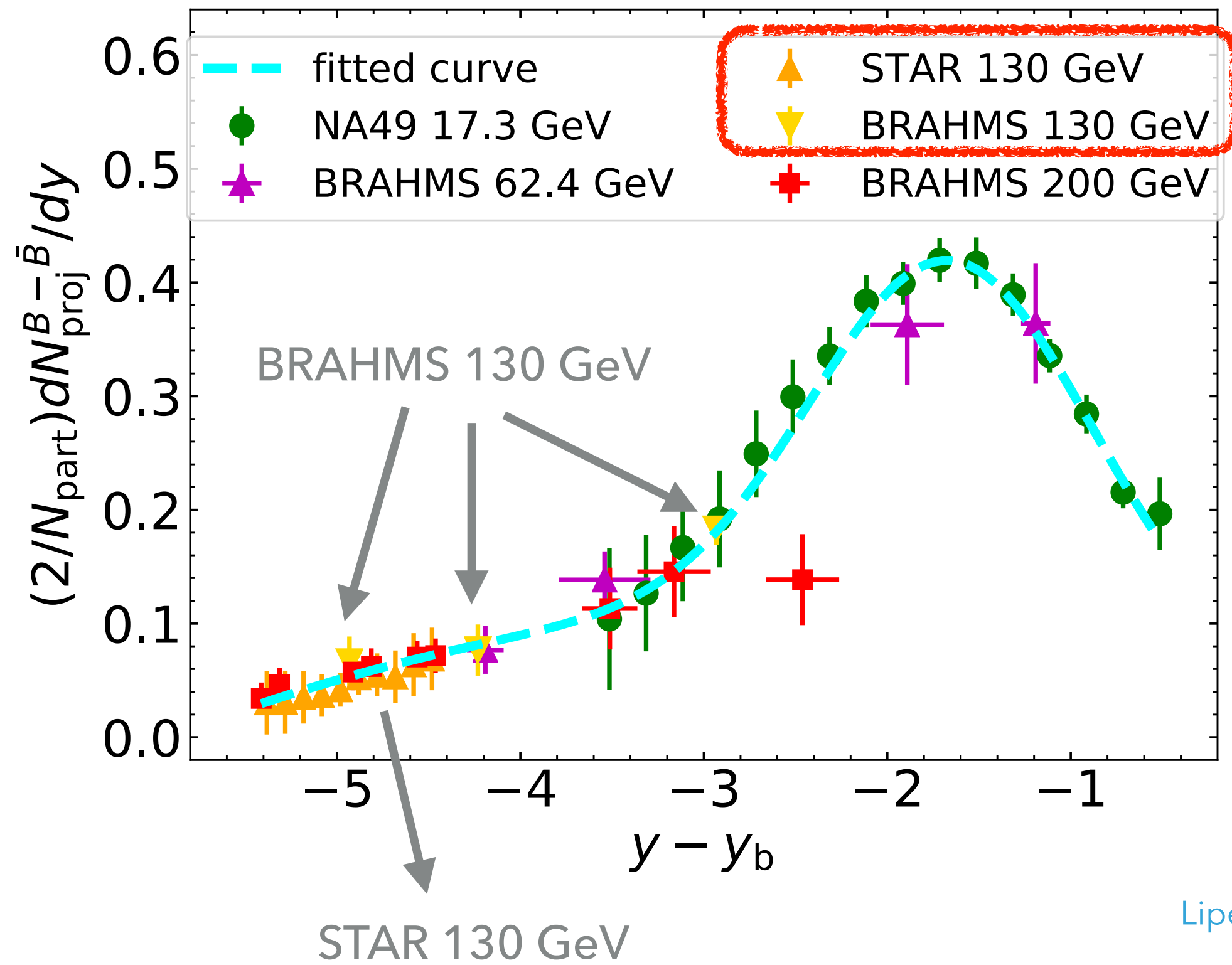
- ▶ Fit the net baryon rapidity density attributed to the projectile after subtraction of the target contribution.
- ▶ The reconstructed distributions can help constrain models at BES.



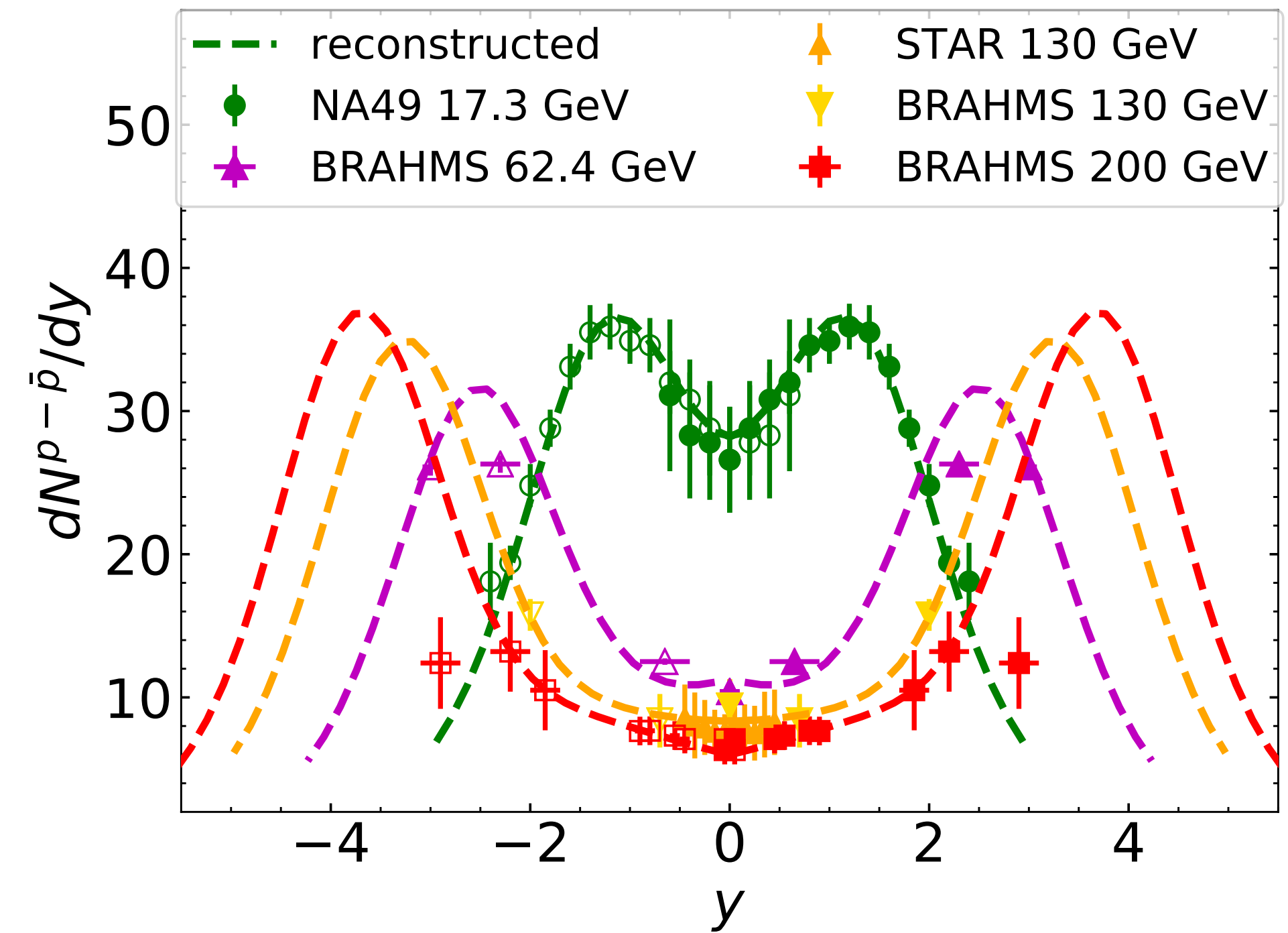
Lipei Du, arXiv: 2401.00596

- ▶ Fit the net baryon rapidity density attributed to the projectile after subtraction of the target contribution.
- ▶ The reconstructed distributions can help constrain models at BES.

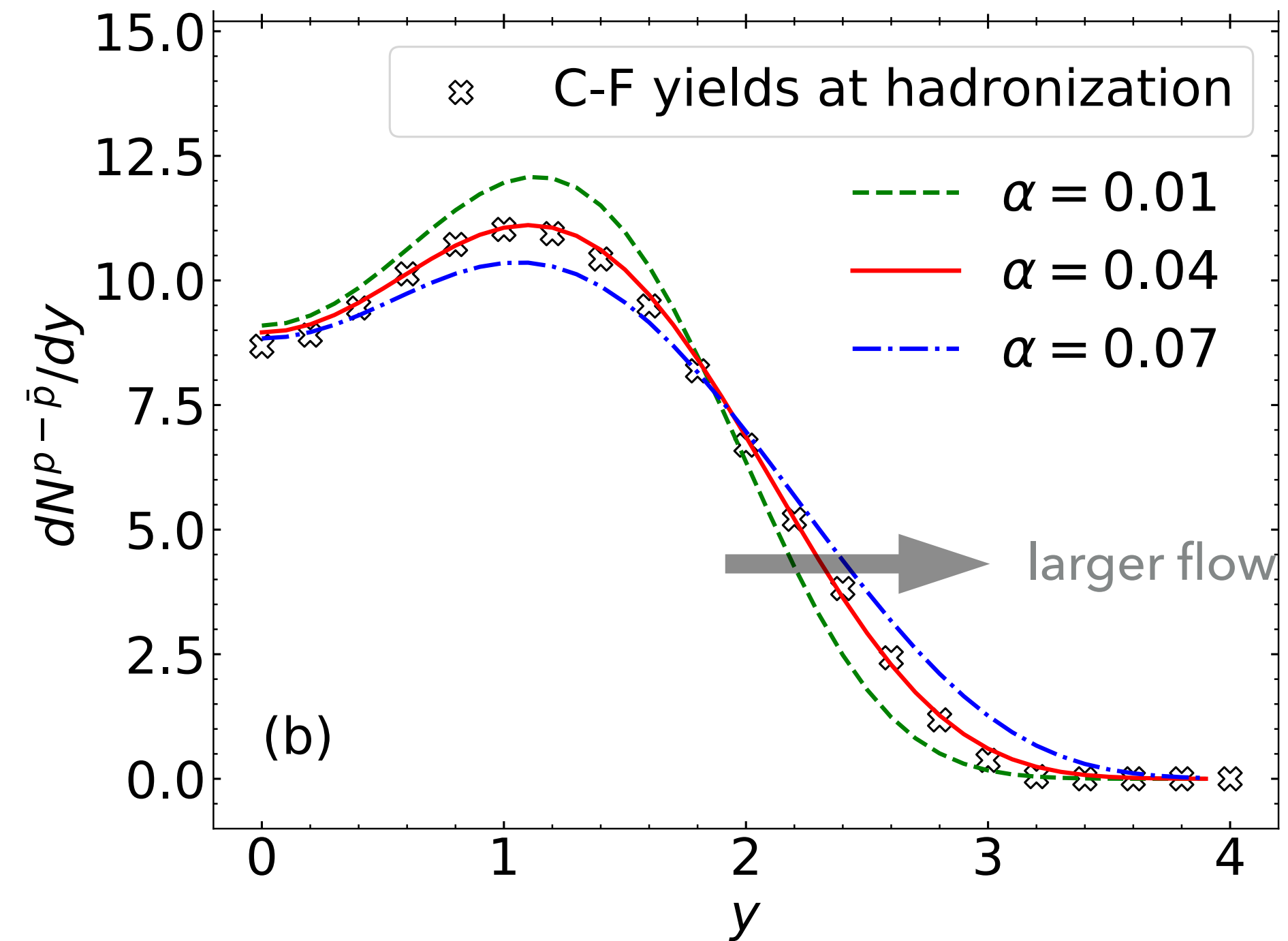
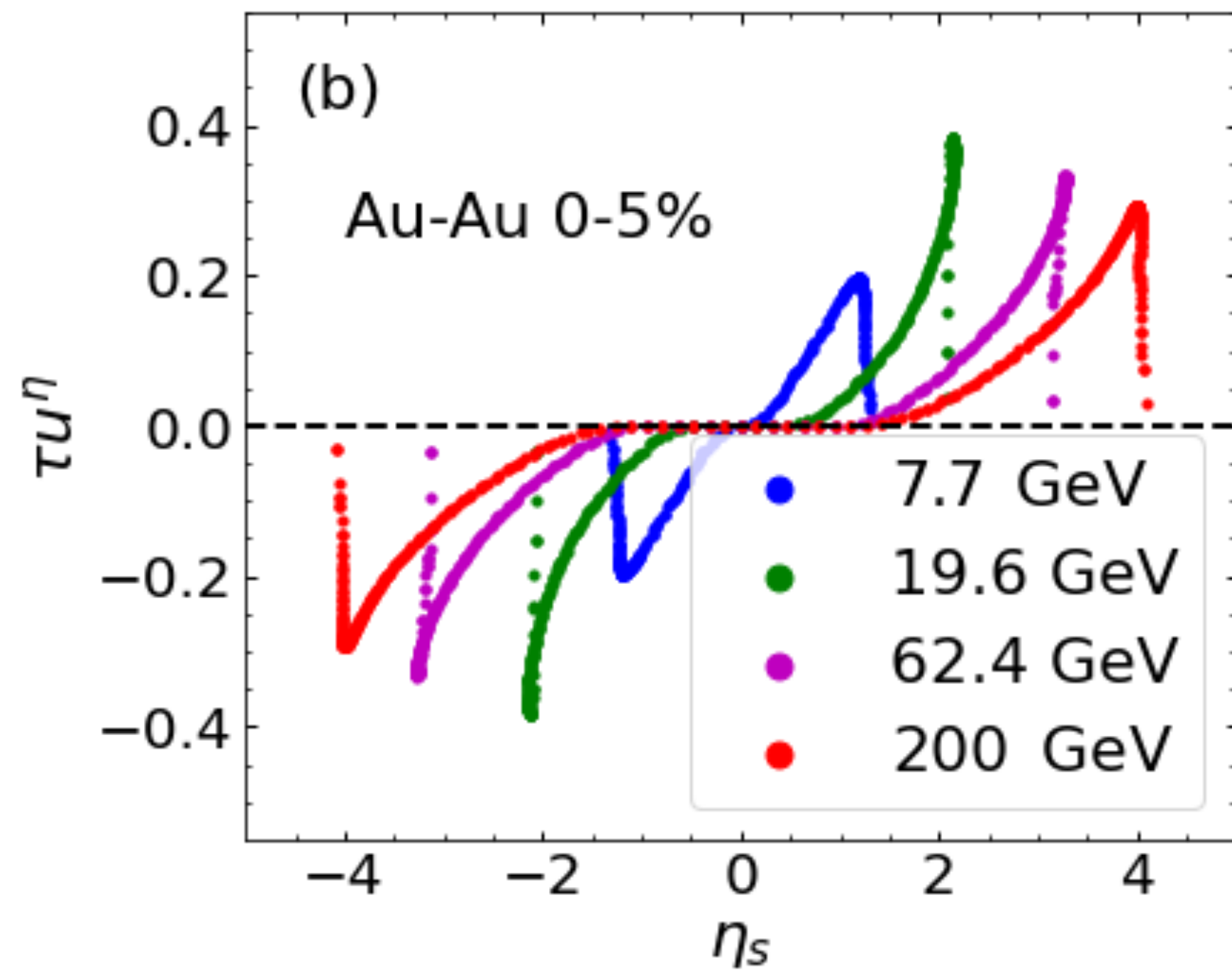




Lipei Du, arXiv: 2401.00596

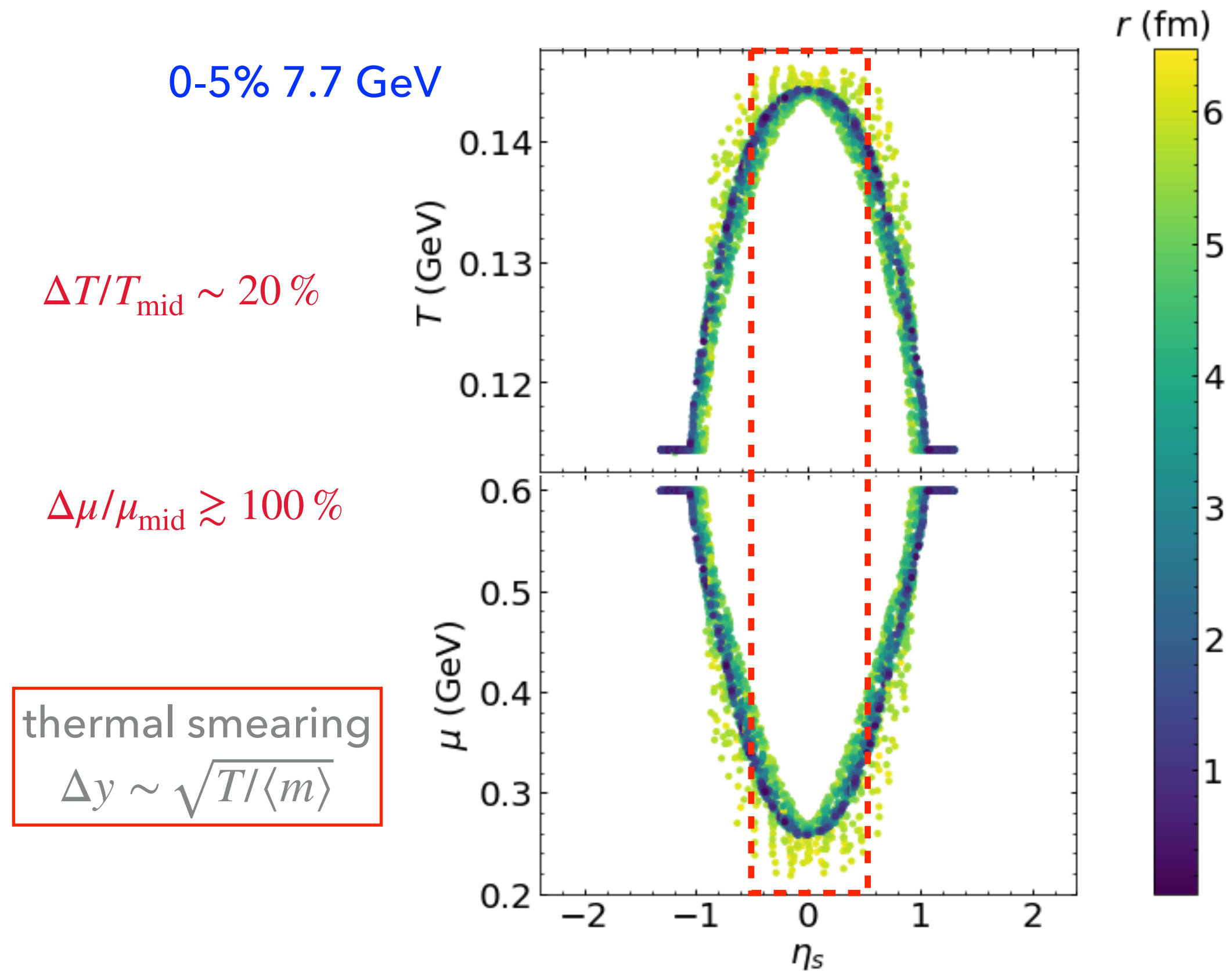


- ▶ Fit the net baryon rapidity density attributed to the projectile after subtraction of the target contribution.
- ▶ The reconstructed distributions can help constrain models at BES.

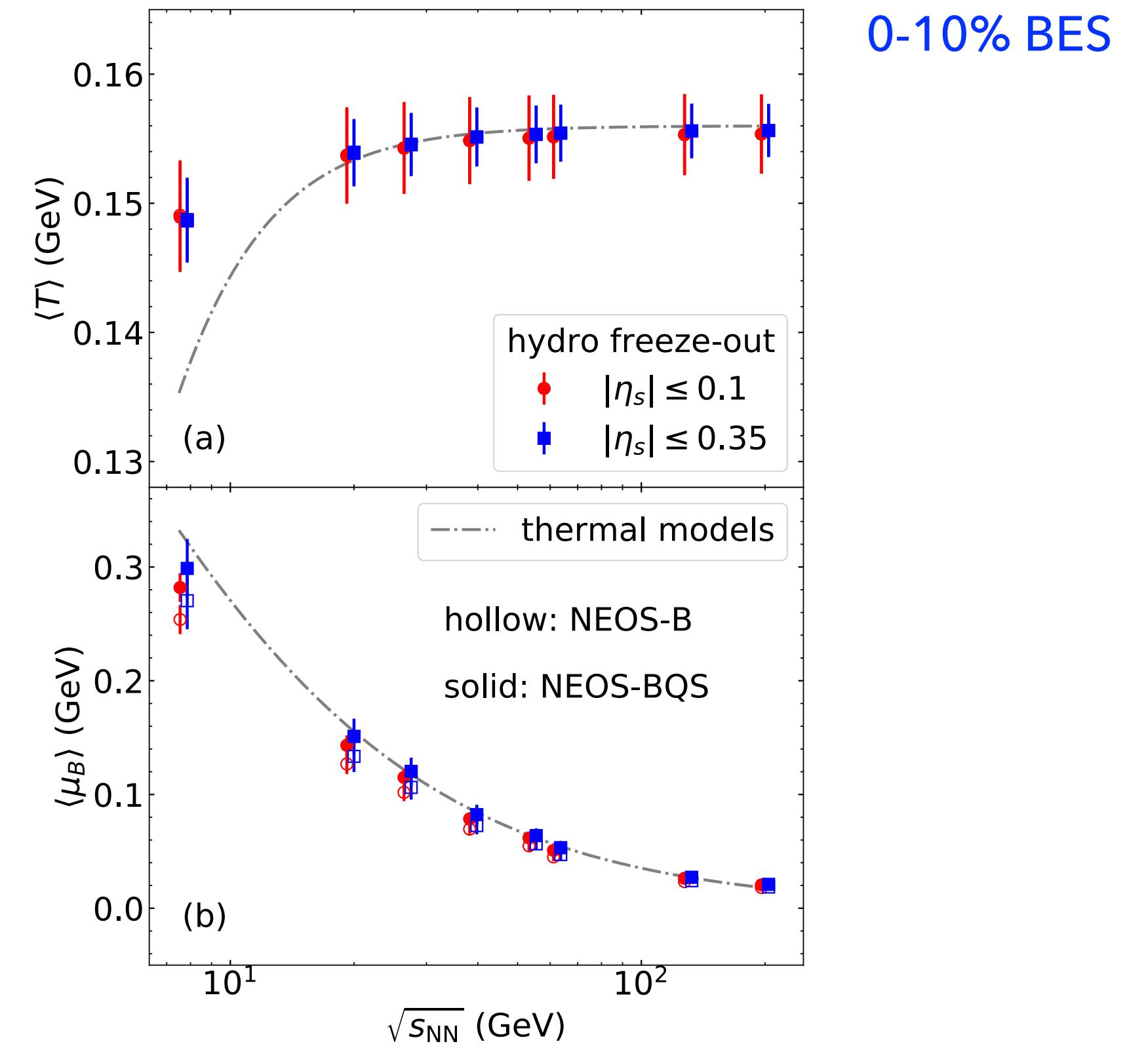


LD, H. Gao, S. Jeon & C. Gale, PRC 109, 014907 (2024)

- ▶ Boost invariance is strongly broken, especially at forward-/backward- rapidities;
- ▶ Starting from the same profiles, the rapidity distributions are stretched with increased longitudinal flow, with heavier particles experiencing greater stretching;
- ▶ Rapidity distributions of various species can be used to constrain the longitudinal flow. [H. Gao, LD, S. Jeon & C. Gale, 2312.09103](#)



LD, H. Gao, S. Jeon & C. Gale, PRC 109, 014907 (2024)



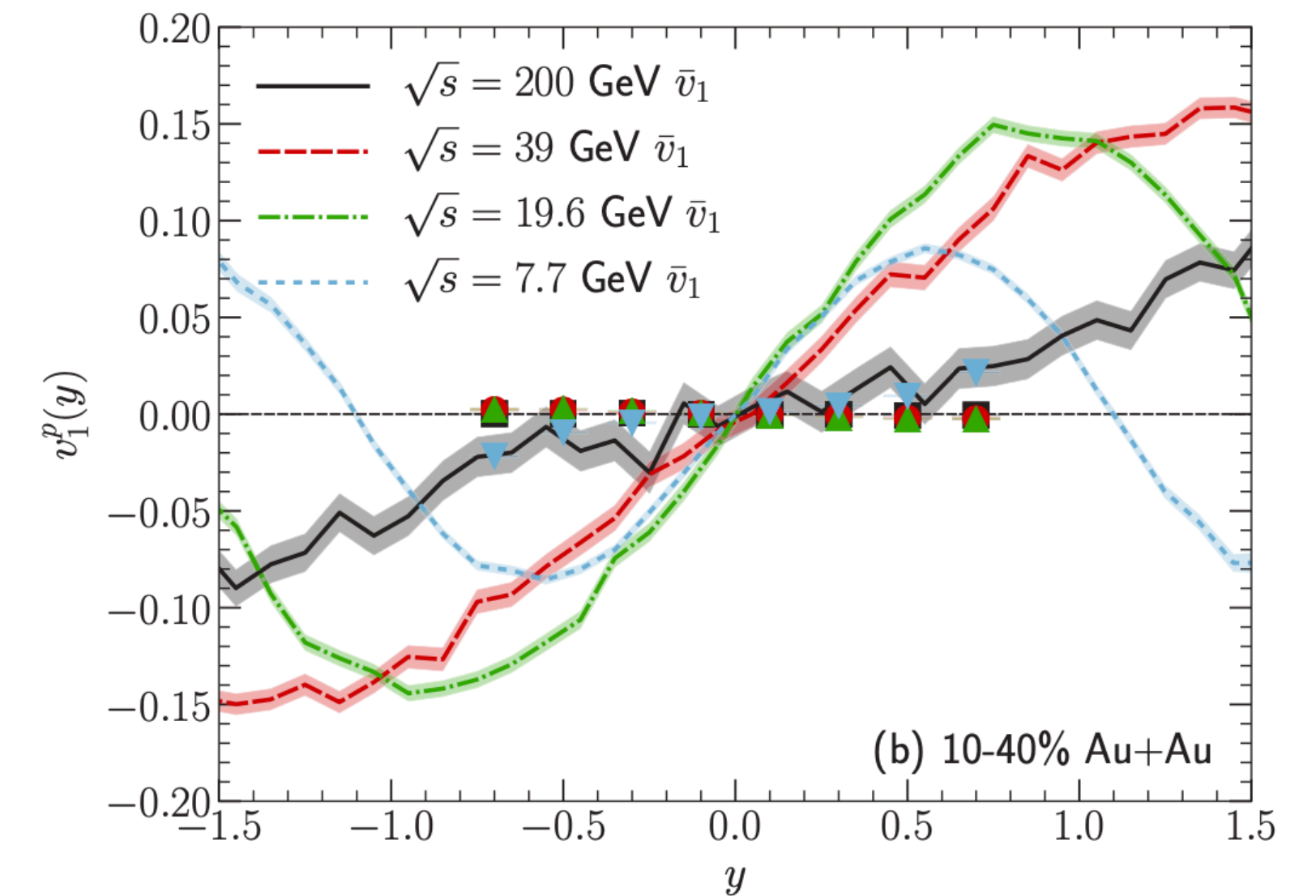
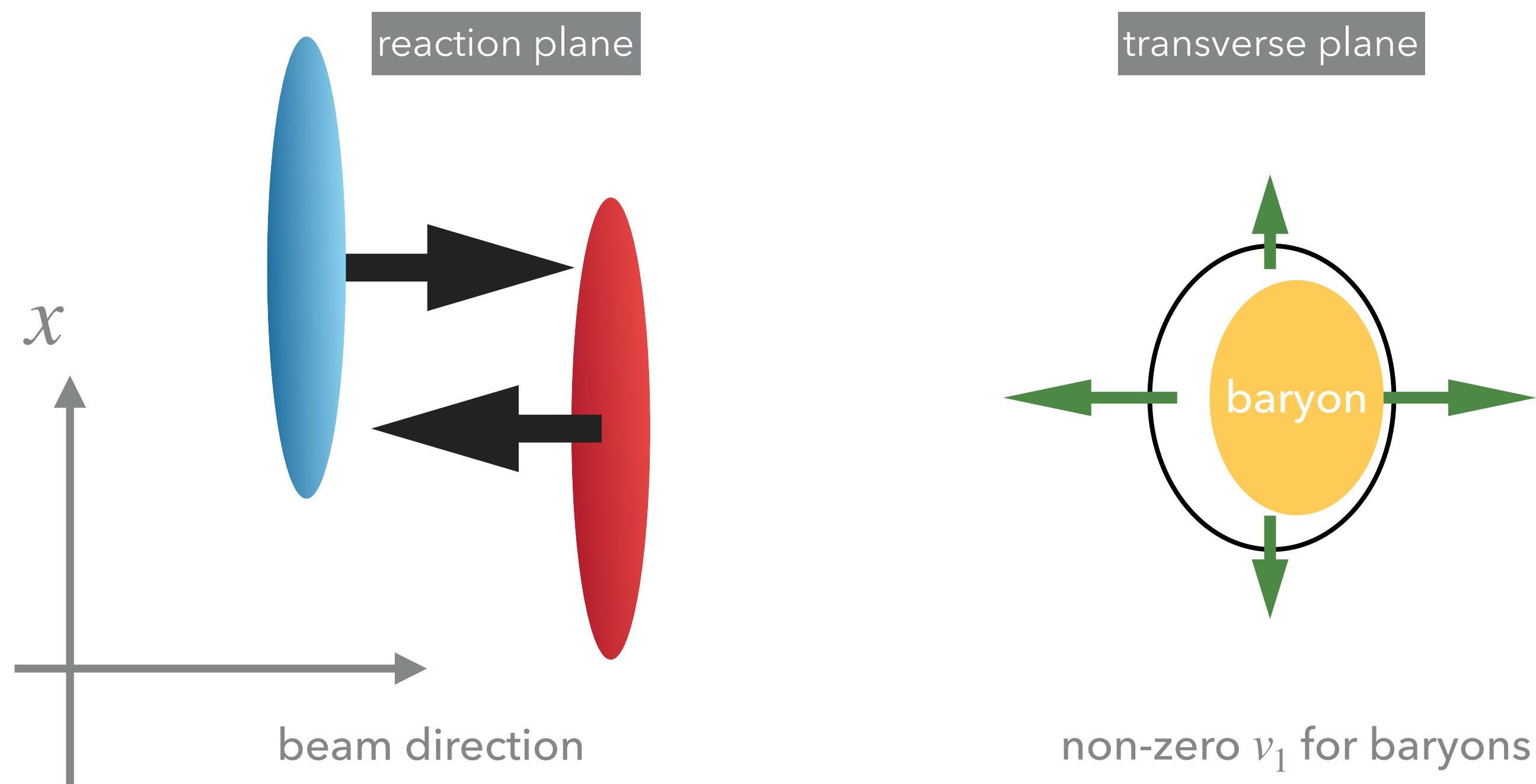
Lipei Du, arXiv: 2401.00596

- ▶ The variation in thermodynamic properties across spacetime rapidity is strong for collisions  $\lesssim 10$  GeV
- ▶ Due to thermal smearing, thermal models extract  $(T, \mu_B)$  averaged over a broader  $\eta_s$  window

---

# **PROBING INITIAL BARYON**

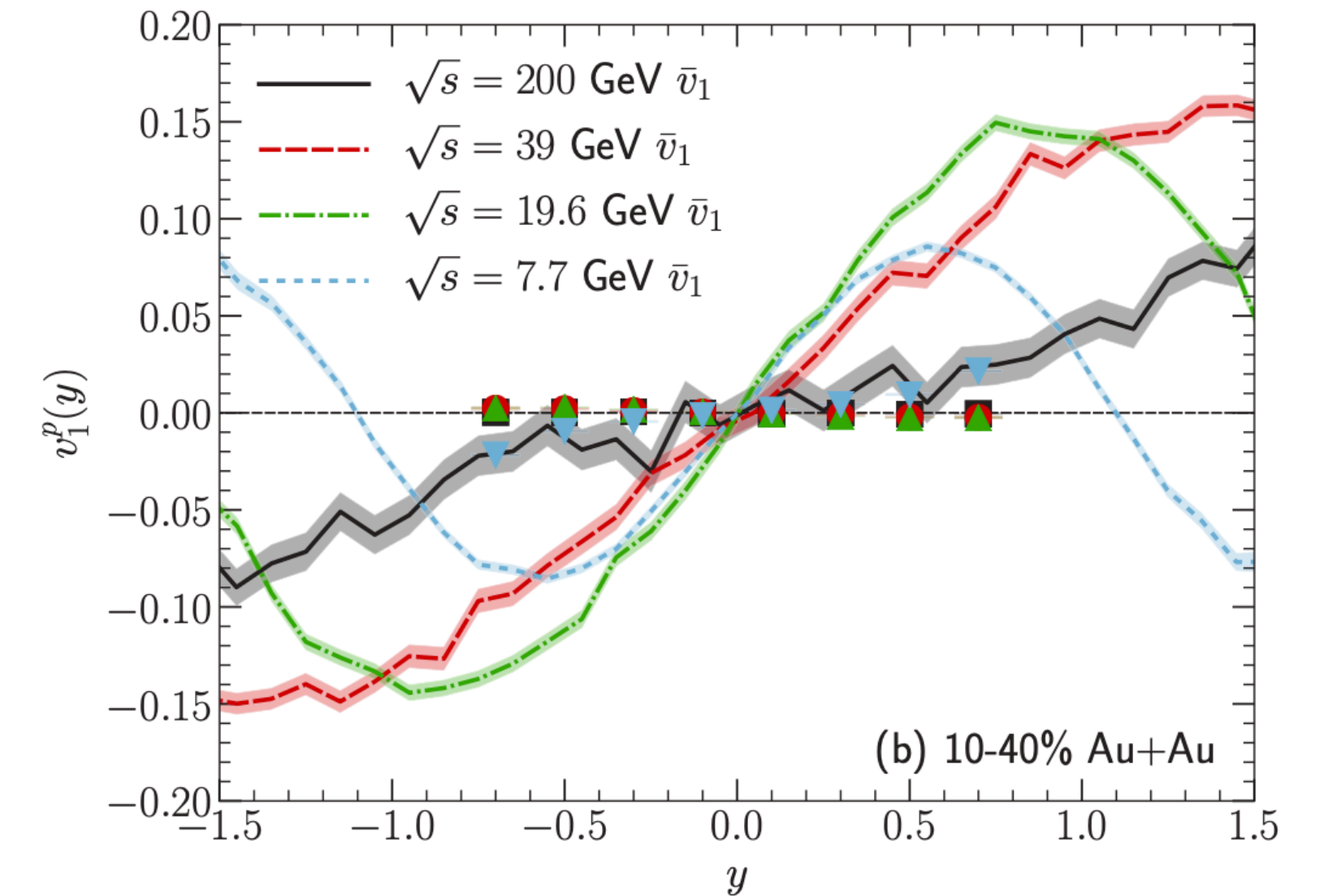
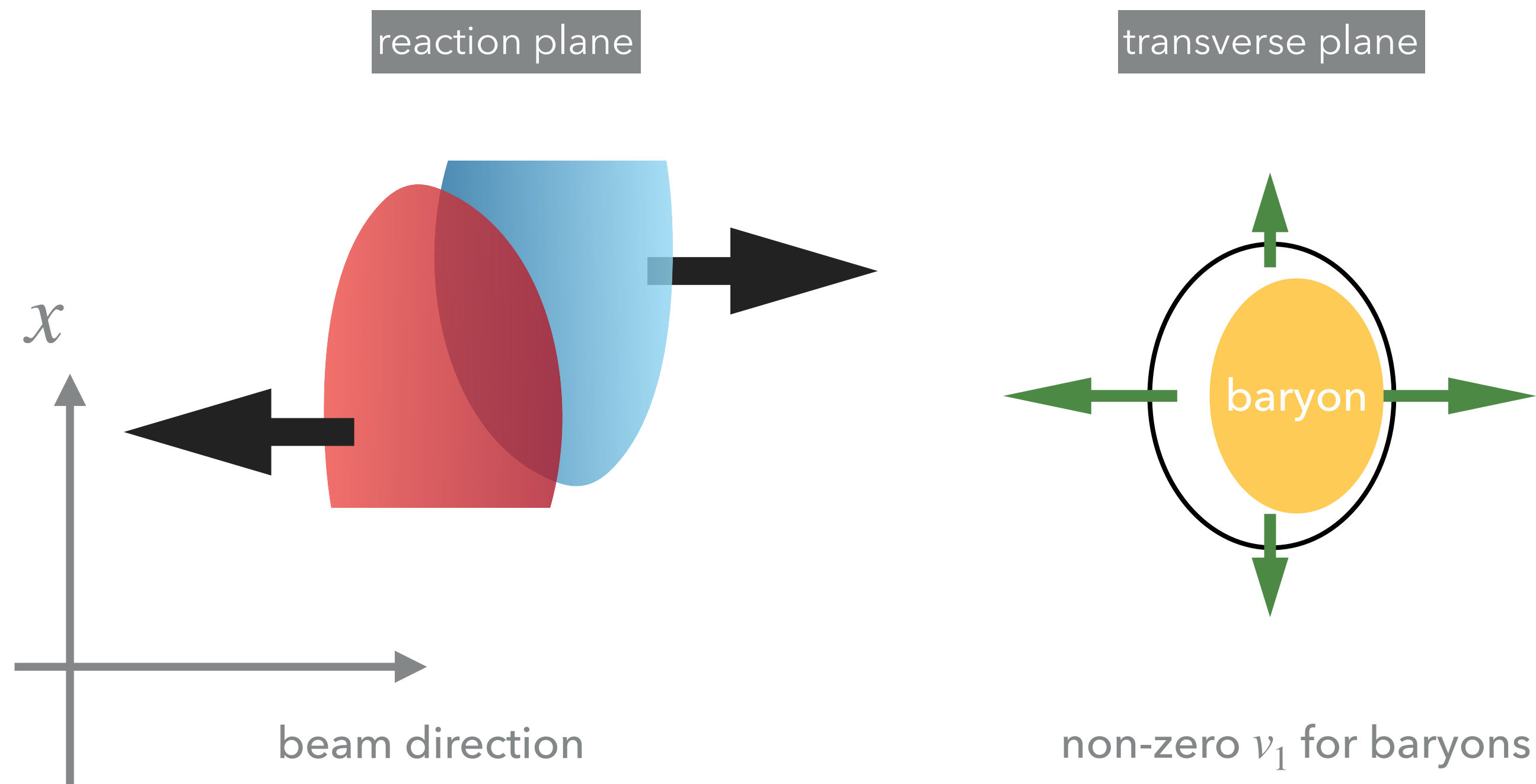
# DIRECTED FLOW $v_1(y)$ OF PROTONS



Shen and Alzhrani, PRC102, 014909 (2020)

- ▶  $v_1(y)$  of baryons is strongly driven by the asymmetric distribution of baryon density with respect to beam axis + transverse expansion;
- ▶ The widely used baryon-stopping picture results in  $v_1(y)$  significantly overshooting the experimental measurements for protons at all beam energies.

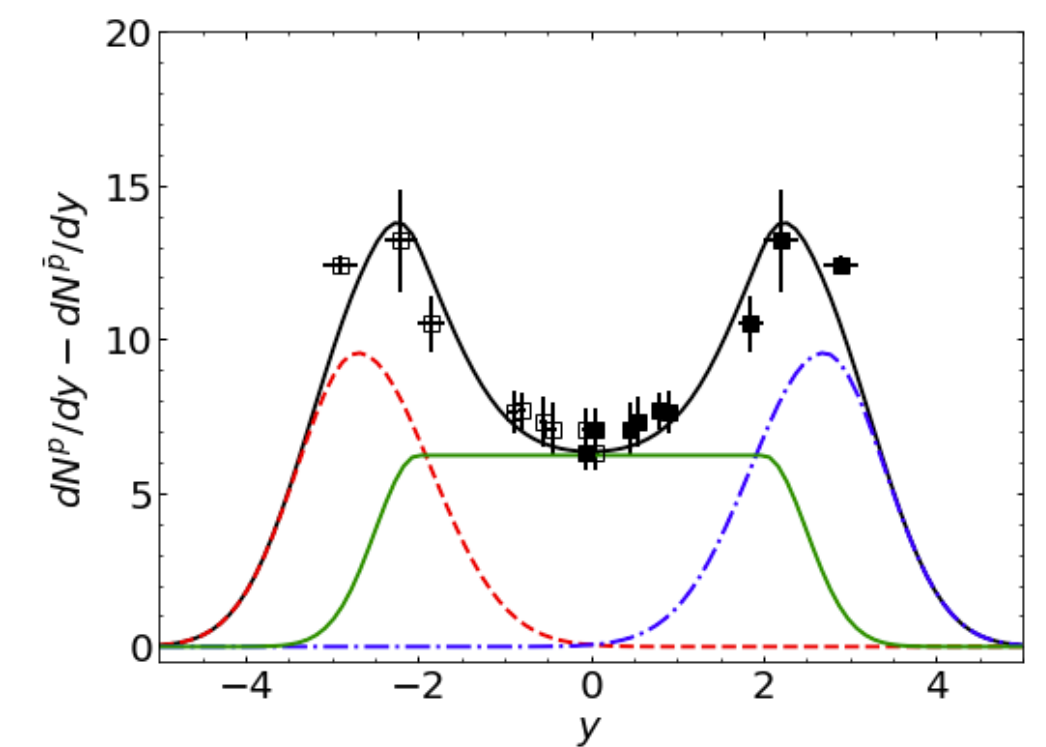
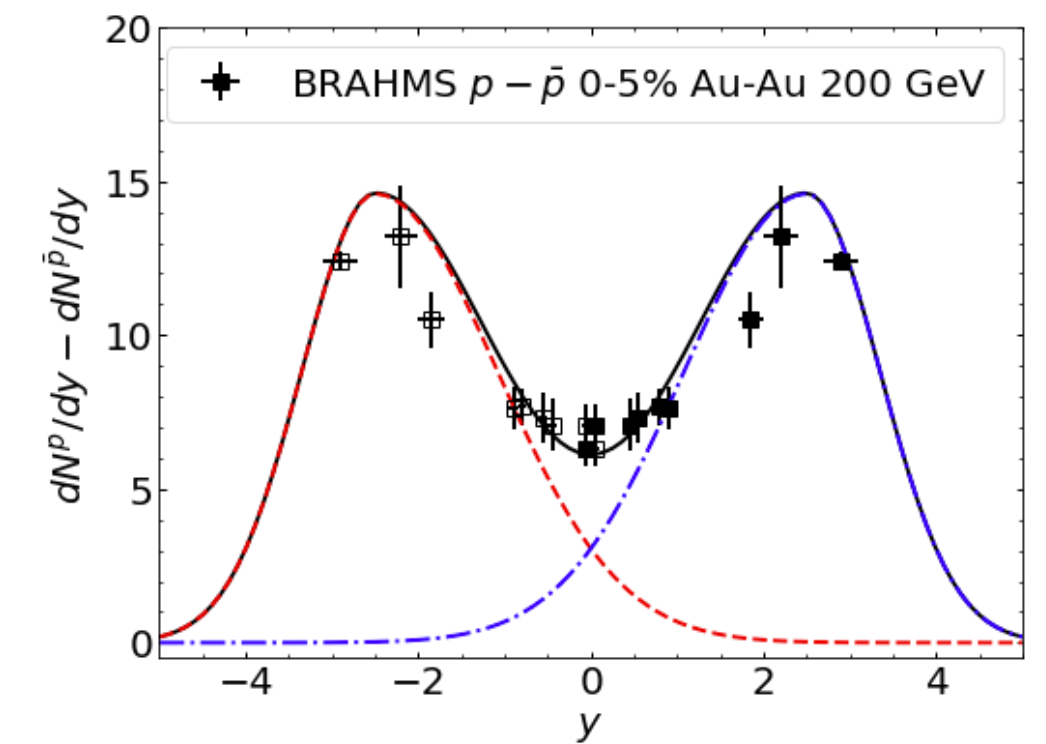
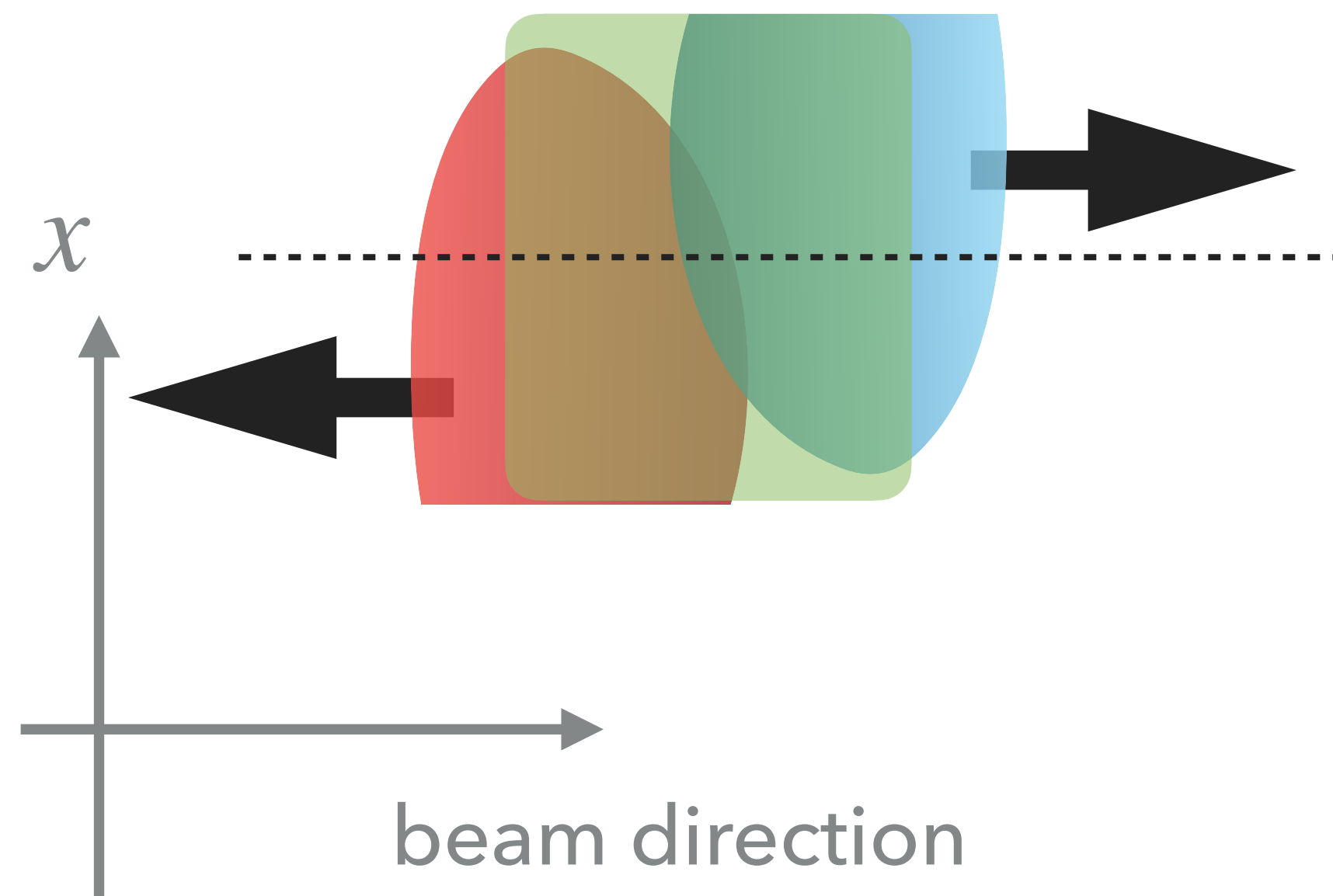
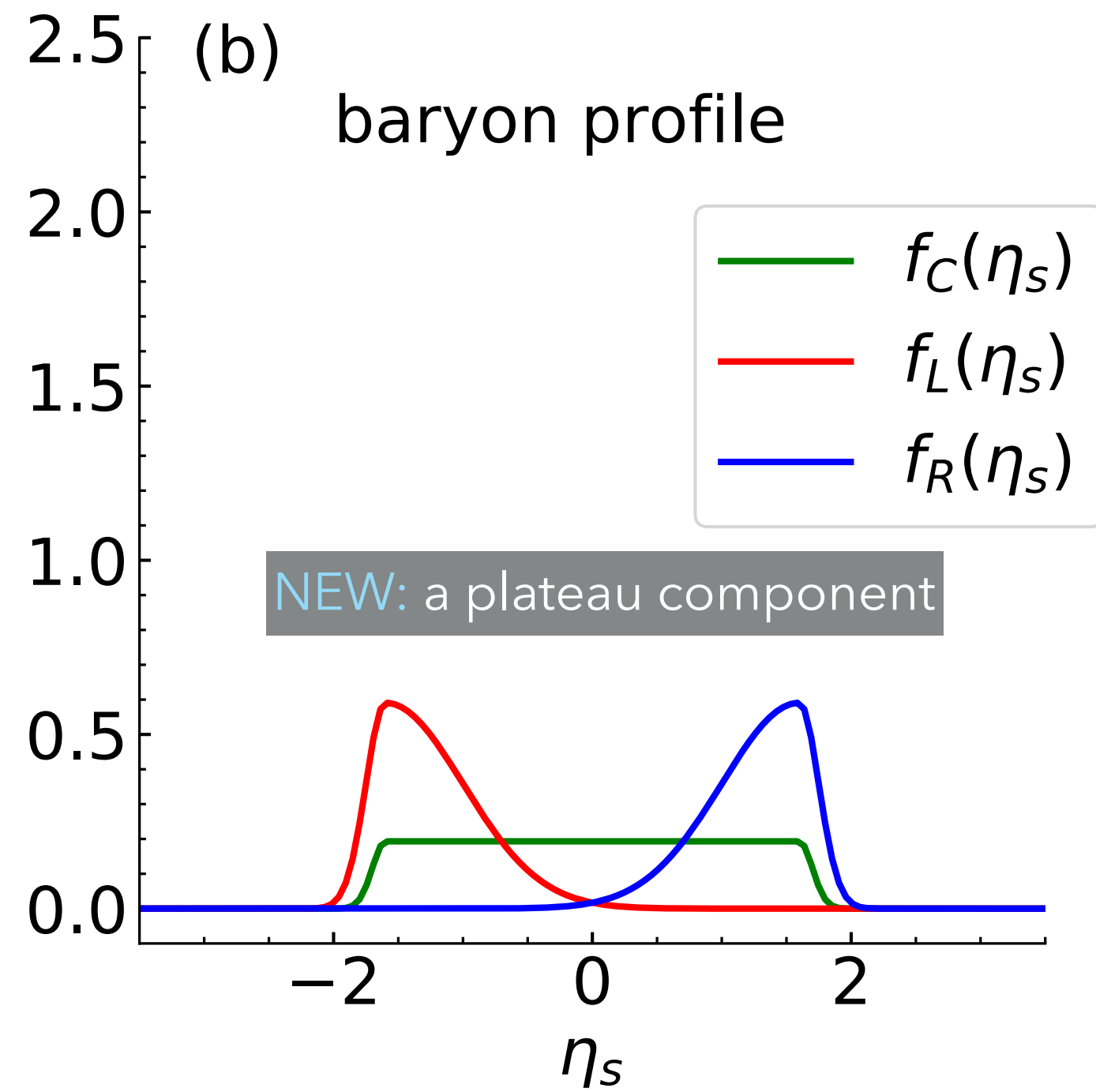




Shen and Alzhrani, PRC102, 014909 (2020)

- ▶  $v_1(y)$  of baryons is strongly driven by the asymmetric distribution of baryon density with respect to beam axis + transverse expansion;
- ▶ The widely used baryon-stopping picture results in  $v_1(y)$  significantly overshooting the experimental measurements for protons at all beam energies.

# NEW PARAMETRIC BARYON INITIAL CONDITION

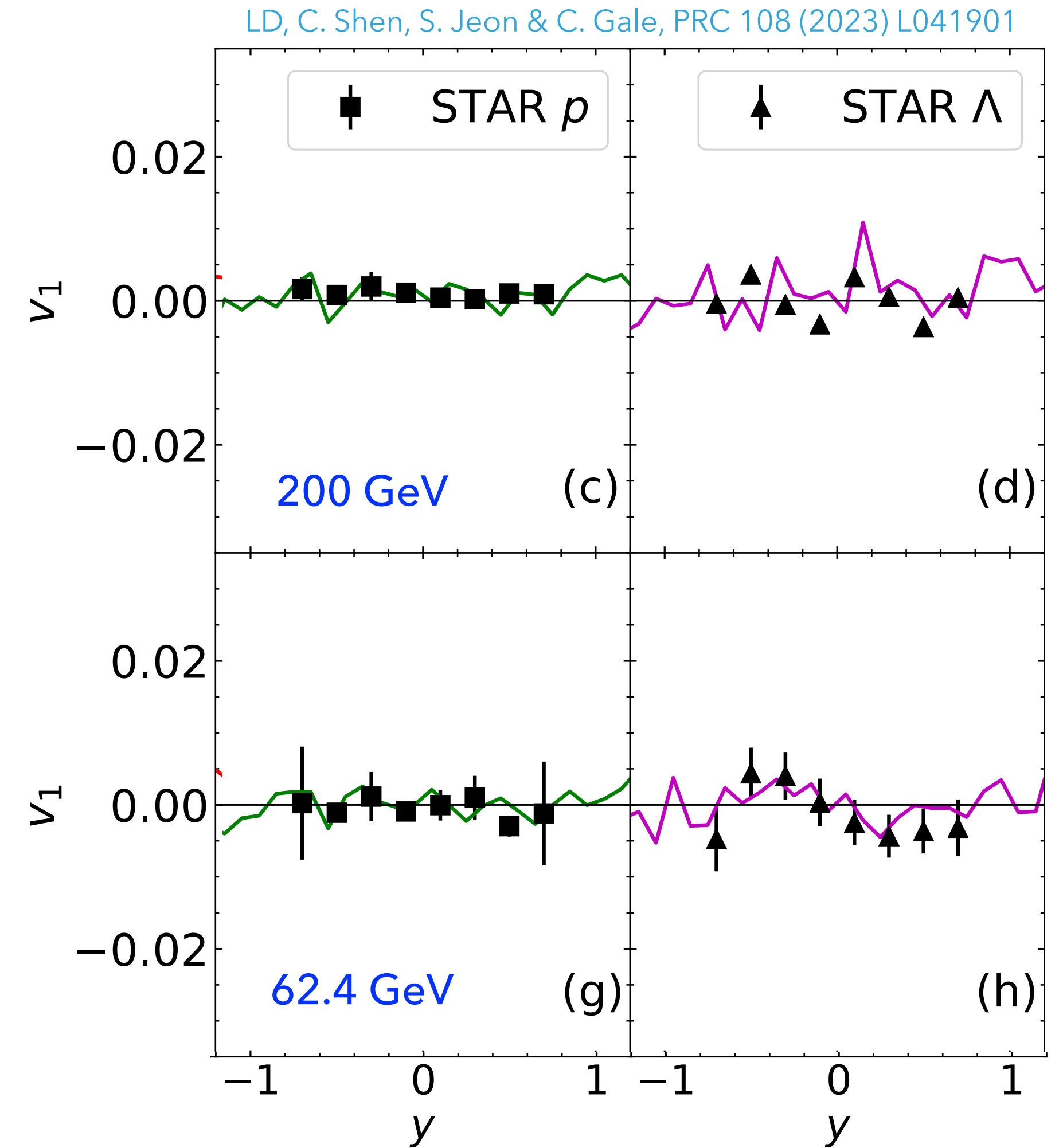
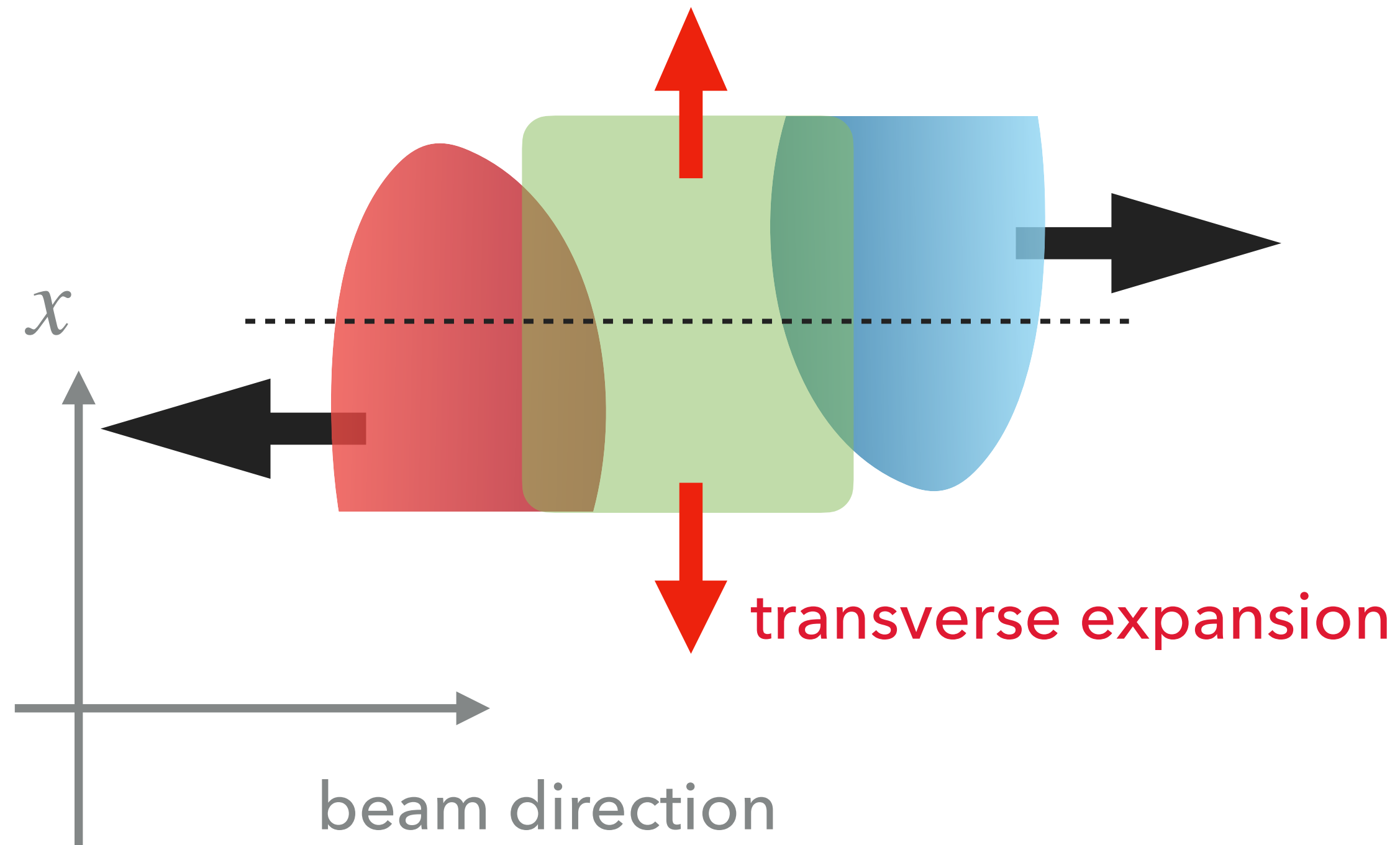


Only for illustration

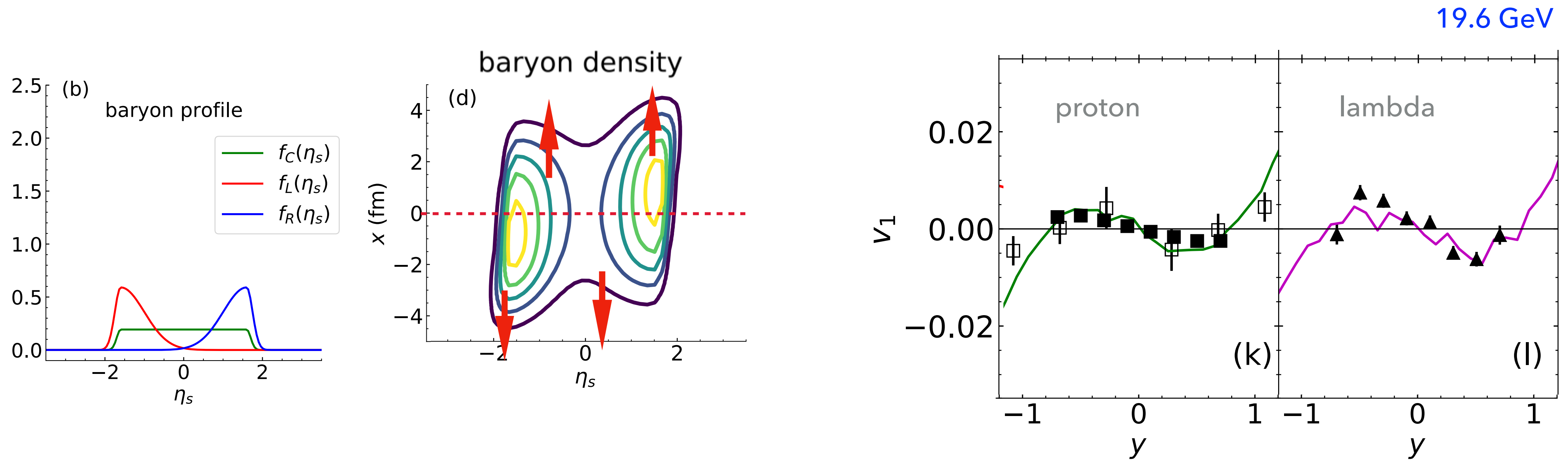
LD, C. Shen, S. Jeon & C. Gale, PRC 108 (2023) L041901

- ▶ To explain the rapidity distributions of net proton yields and baryons' directed flows simultaneously, a plateau component is favored

P. Tribedy, Wed. 11:50 am



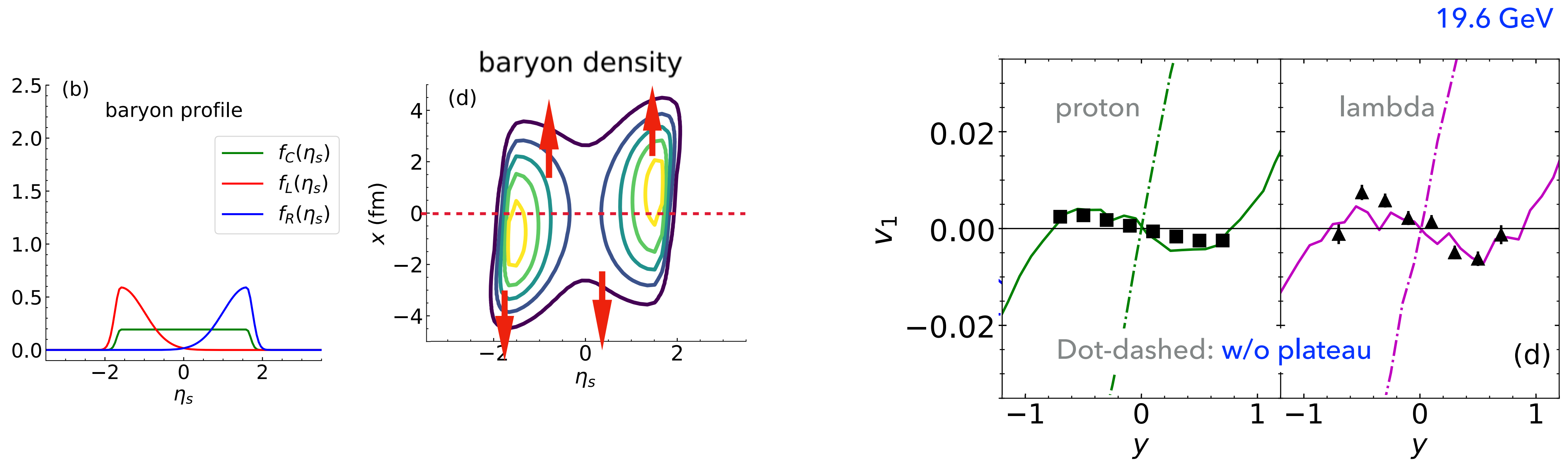
- ▶ At high beam energies with large beam rapidities, the plateau dominates around mid-rapidity and strongly reduces baryons'  $v_1(y)$ .



Initial baryon distributions in the reaction plane for 10-40% Au+Au@19.6 GeV

LD, C. Shen, S. Jeon & C. Gale, PRC 108 (2023) L041901

- ▶ Transverse expansion + asymmetric distribution of baryon density along  $x \implies$  double sign change in the slope of  $v_1(y)$  for baryons at 19.6 GeV, and positive slope at 7.7 GeV
- ▶ The sign change of  $dv_1(y)/dy|_{y=0}$  is naturally reproduced without a 1st-order phase transition.

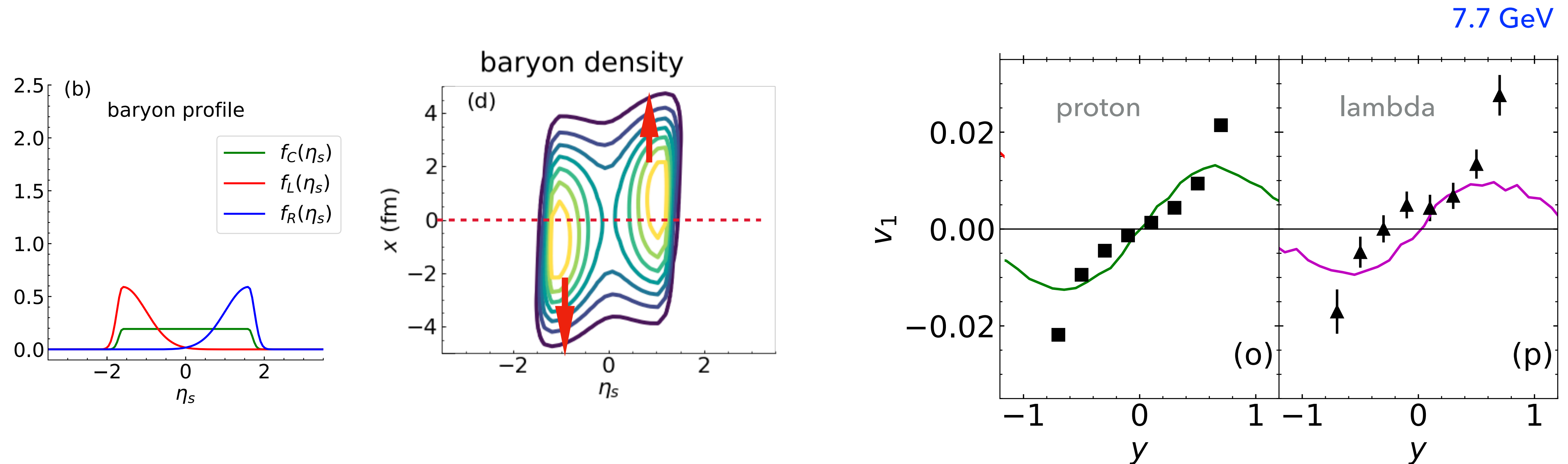


Initial baryon distributions in the reaction plane for 10-40% Au+Au@19.6 GeV

LD, C. Shen, S. Jeon & C. Gale, PRC 108 (2023) L041901

- ▶ Transverse expansion + asymmetric distribution of baryon density along  $x \implies$  double sign change in the slope of  $v_1(y)$  for baryons at 19.6 GeV, and positive slope at 7.7 GeV
- ▶ The sign change of  $dv_1(y)/dy|_{y=0}$  is naturally reproduced without a 1st-order phase transition.

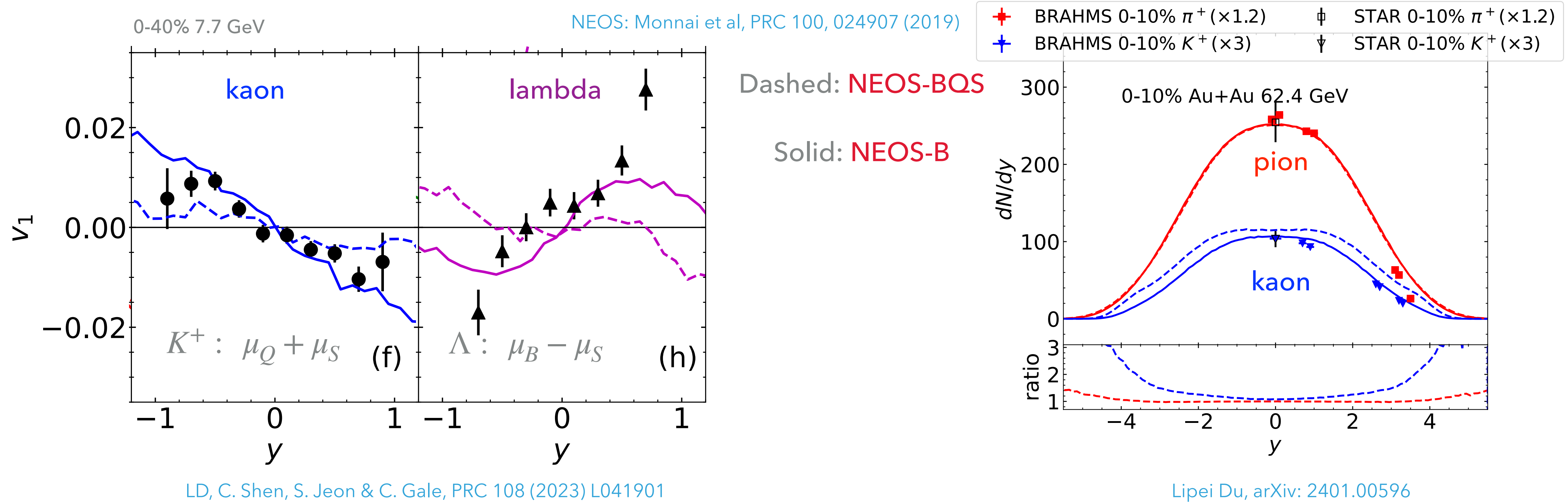




Initial baryon distributions in the reaction plane for 10-40% Au+Au@7.7 GeV

LD, C. Shen, S. Jeon & C. Gale, PRC 108 (2023) L041901

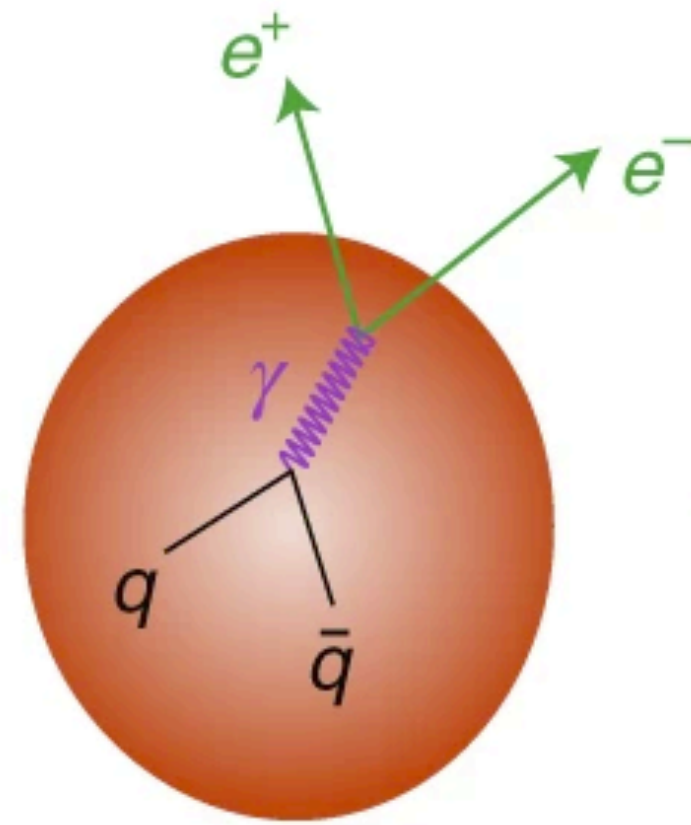
- ▶ Transverse expansion + asymmetric distribution of baryon density along  $x \implies$  double sign change in the slope of  $v_1(y)$  for baryons at 19.6 GeV, and positive slope at 7.7 GeV
- ▶ The sign change of  $dv_1(y)/dy|_{y=0}$  is naturally reproduced without a 1st-order phase transition.



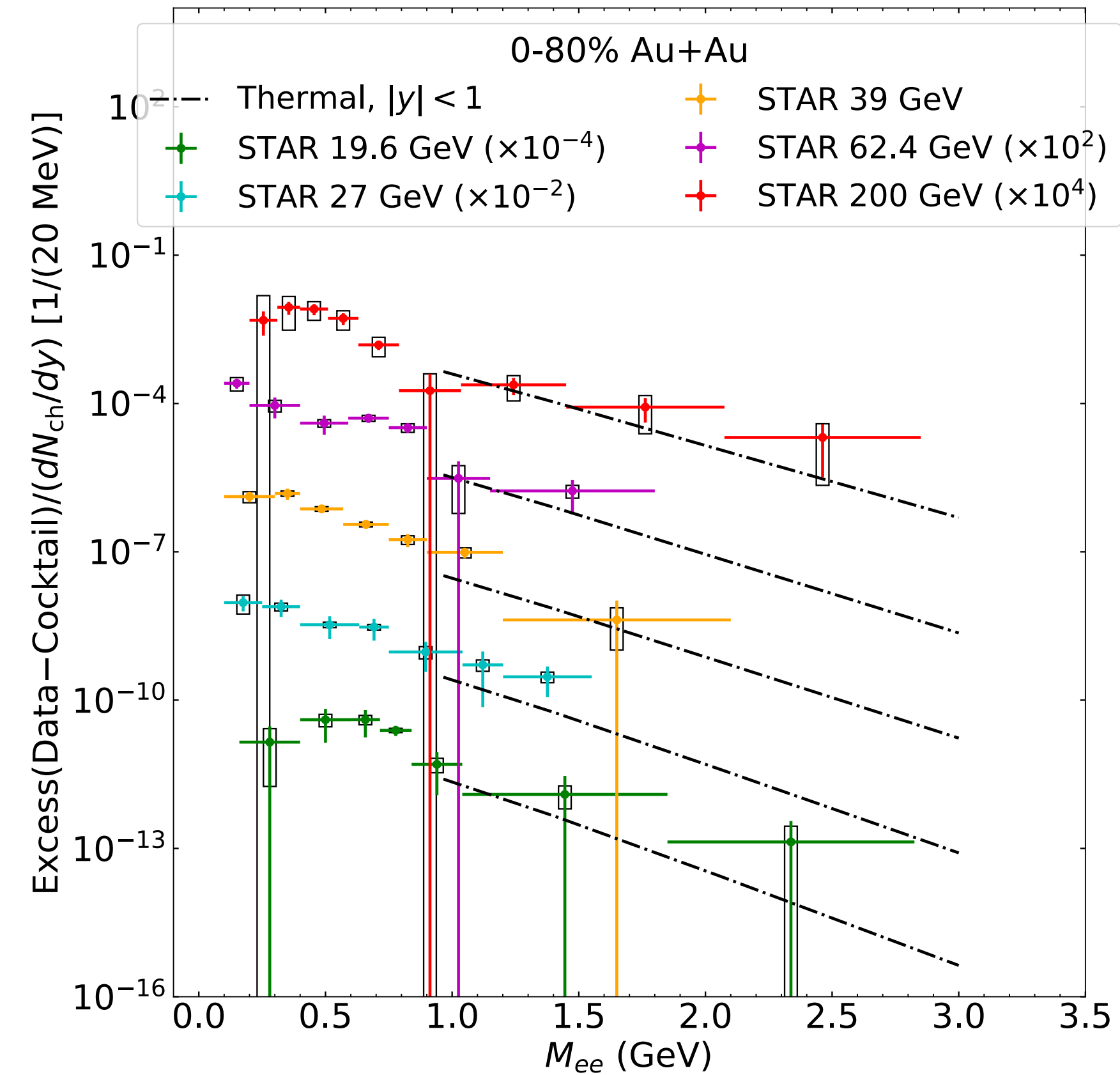
- ▶ Two limits of EoS: NEOS-B,  $\mu_S = \mu_Q = 0$  and NEOS-BQS,  $n_S = 0, n_Q = 0.4n_B$  (2D projection of a 4D EOS)
- ▶ Rapidity-dependent measurements of identified particles can be used to probe EoS at finite chemical potentials.

---

# **PROBING INITIAL TEMPERATURE**



- ▶ Dileptons & real photons: A penetrating, “clean” probe
  - ▶ emitted throughout the entire evolution of the medium
  - ▶ escape the strongly interacting medium with negligible interactions (“clean”)

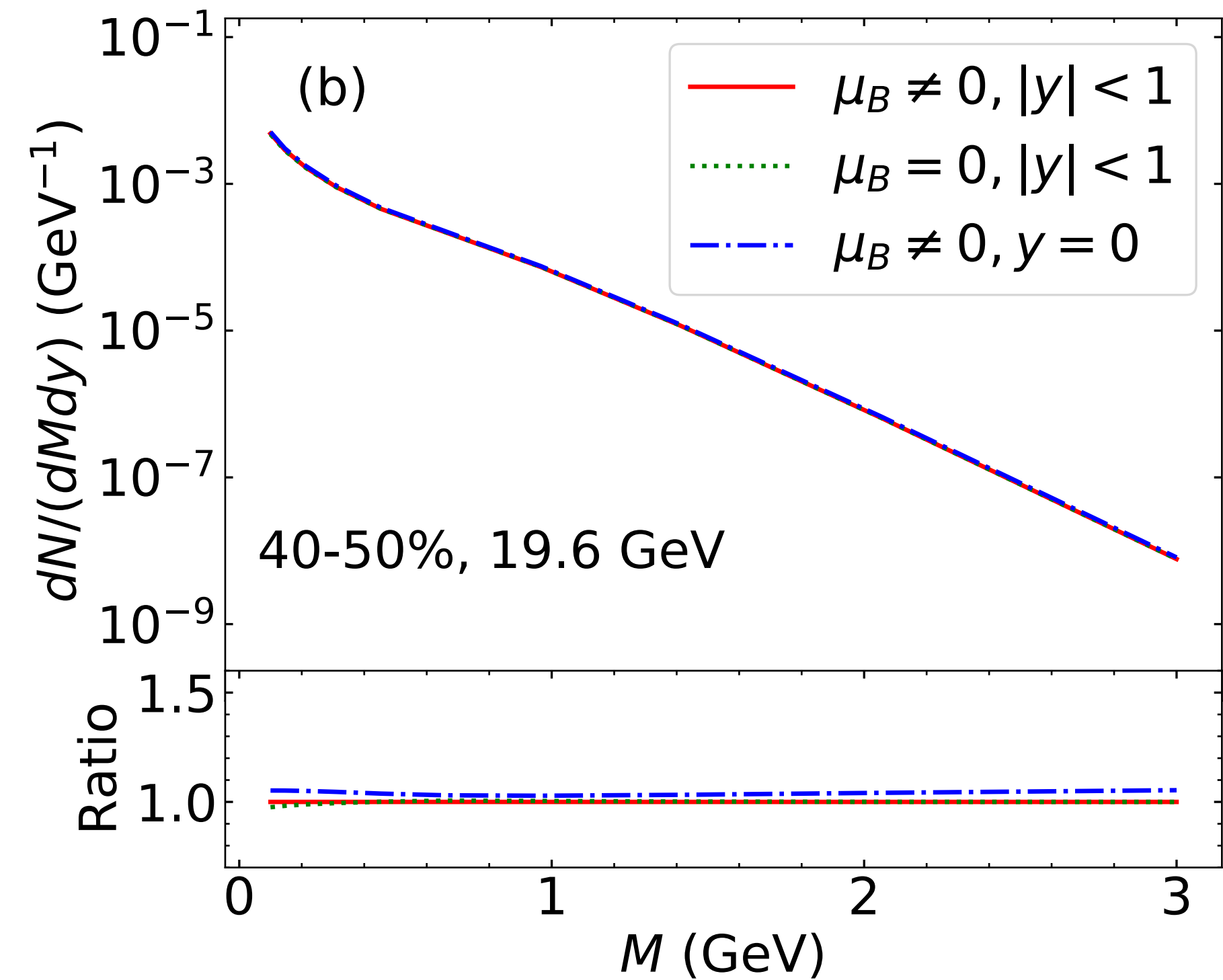
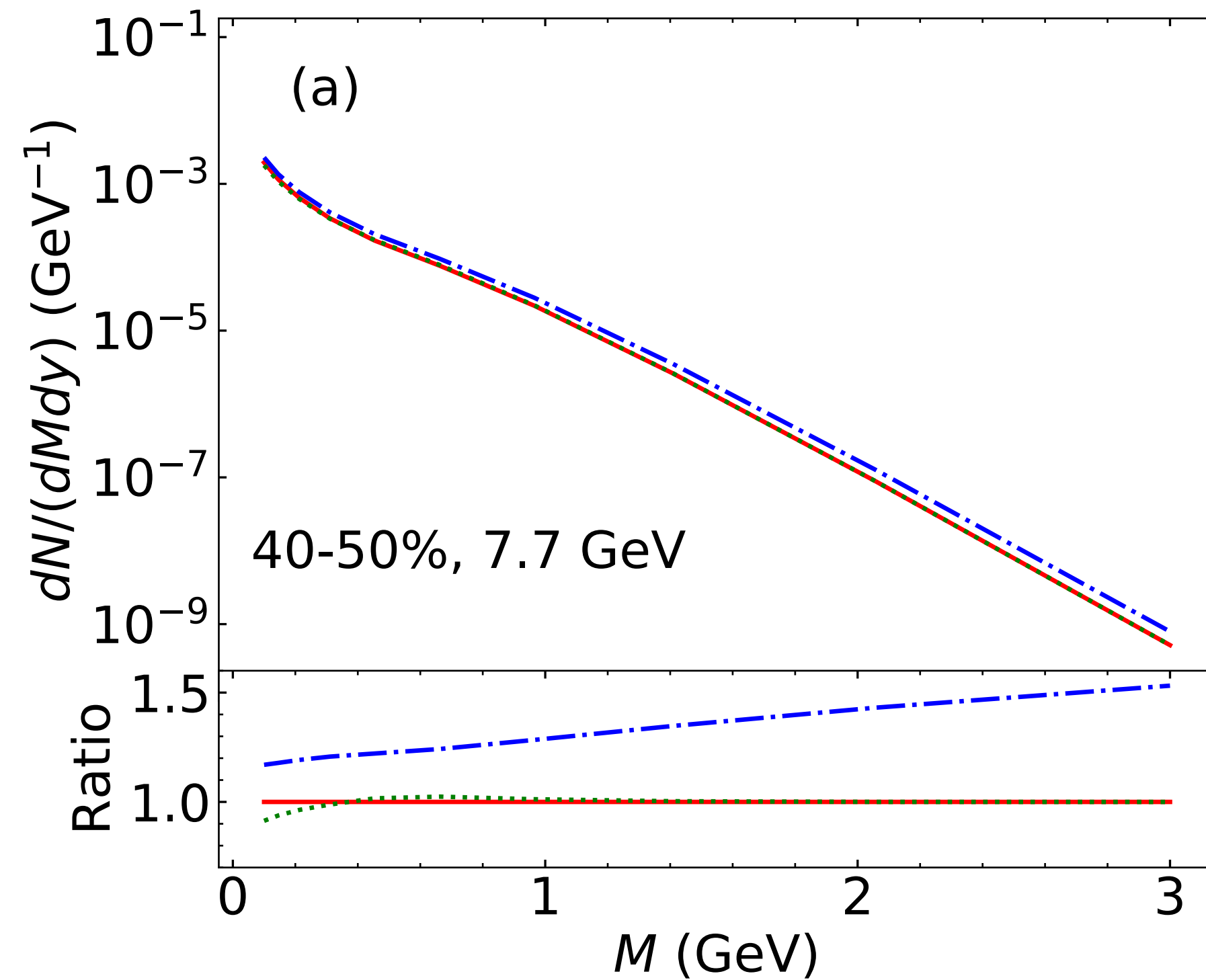


<https://github.com/LipeiDu/DileptonEmission>

J. Churchill, LD, C. Gale, G. Jackson & S. Jeon, PRC 109, 044915 (2024), PRL 132, 172301 (2024)

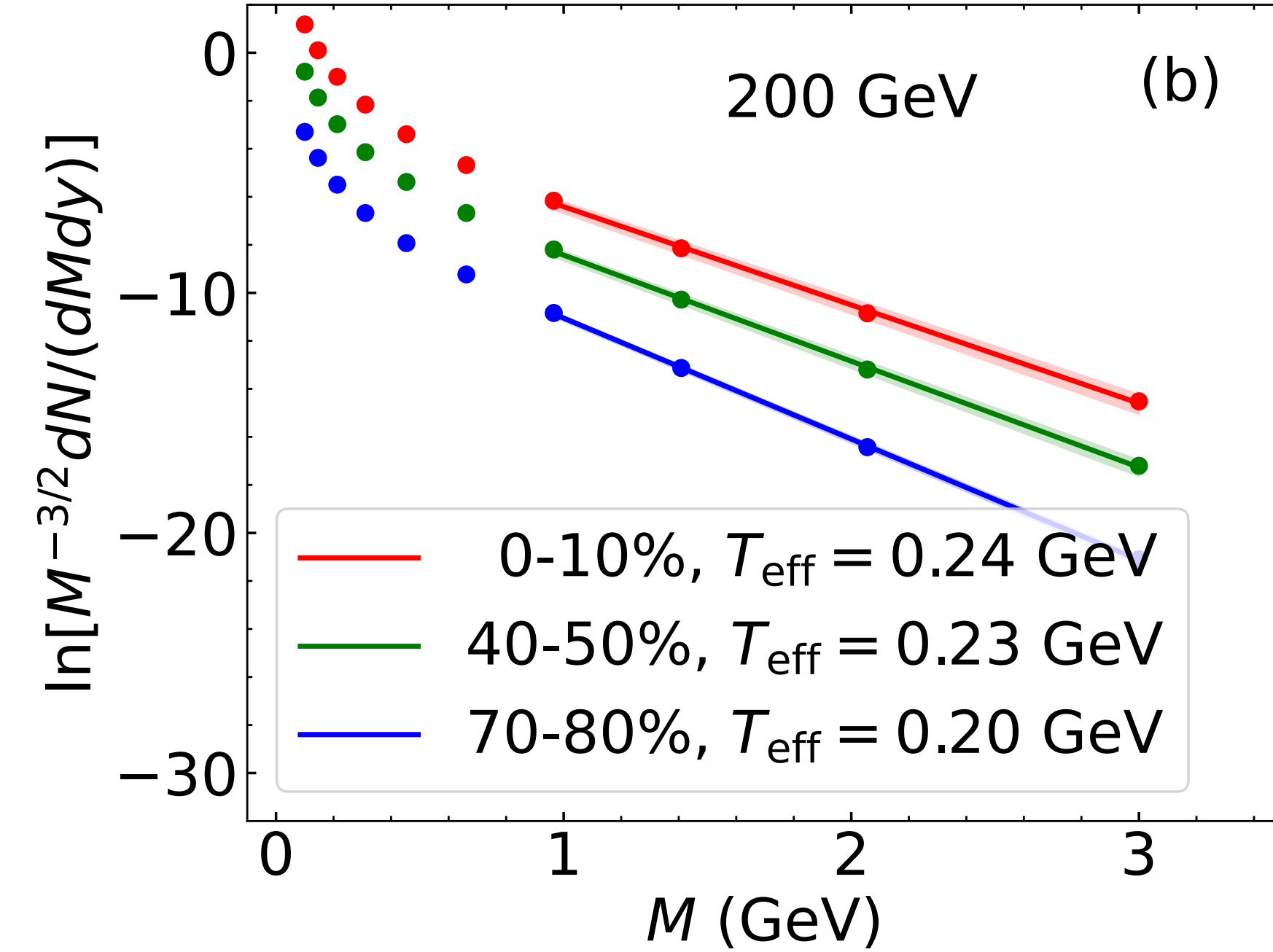
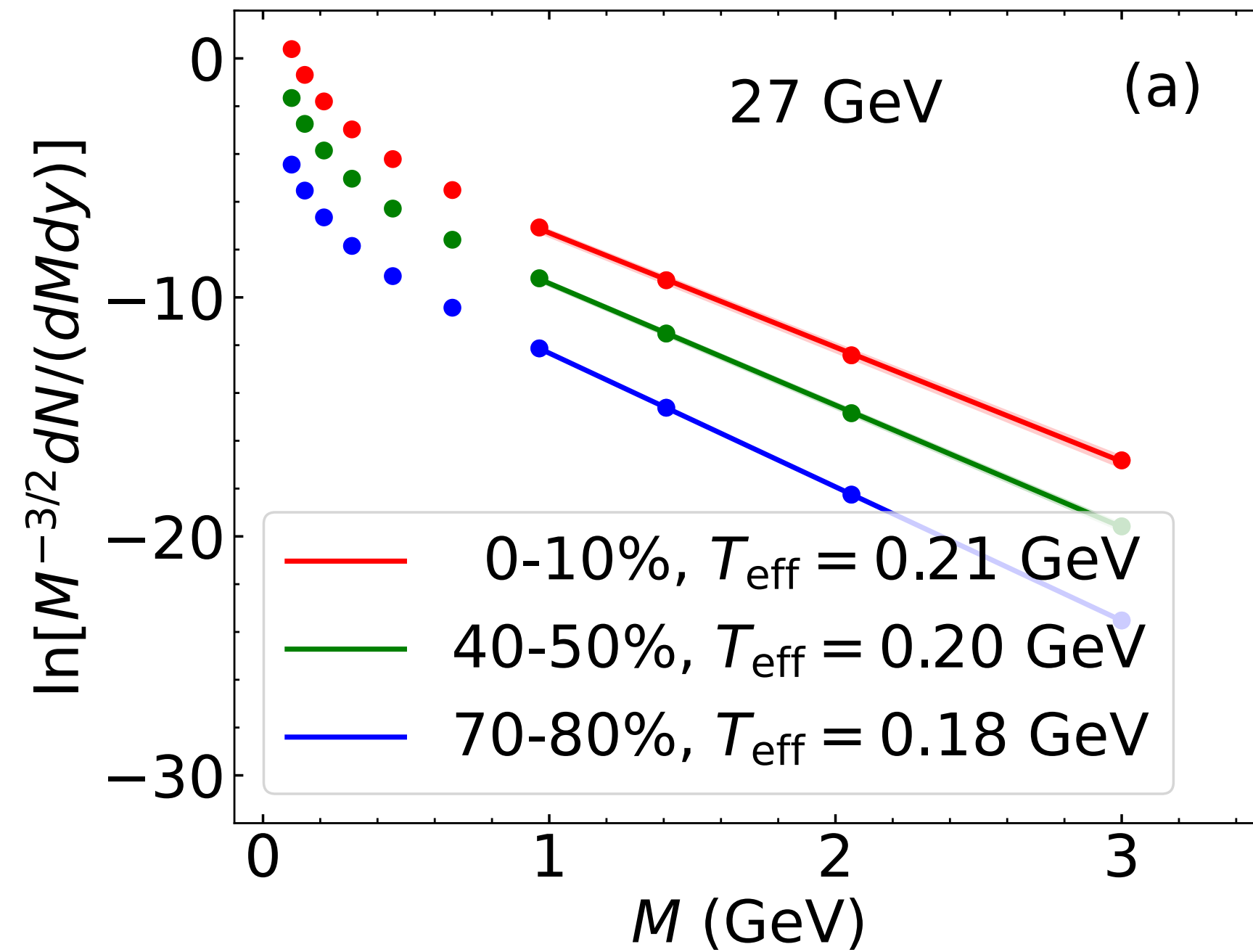
NA60, PRL 100, 022302 (2008); EPJC 59 607-623 (2009). STAR, PRL113, 022301 (2014); PRC 92, 024912 (2015); PLB 750 (2015) 64-71; PRC 107, L061901 (2023). HADES, Nat. Phys., 1040-1045 (2019).

- ▶ First estimate of NLO dilepton emission at nonzero  $\mu_B$  with hydrodynamics

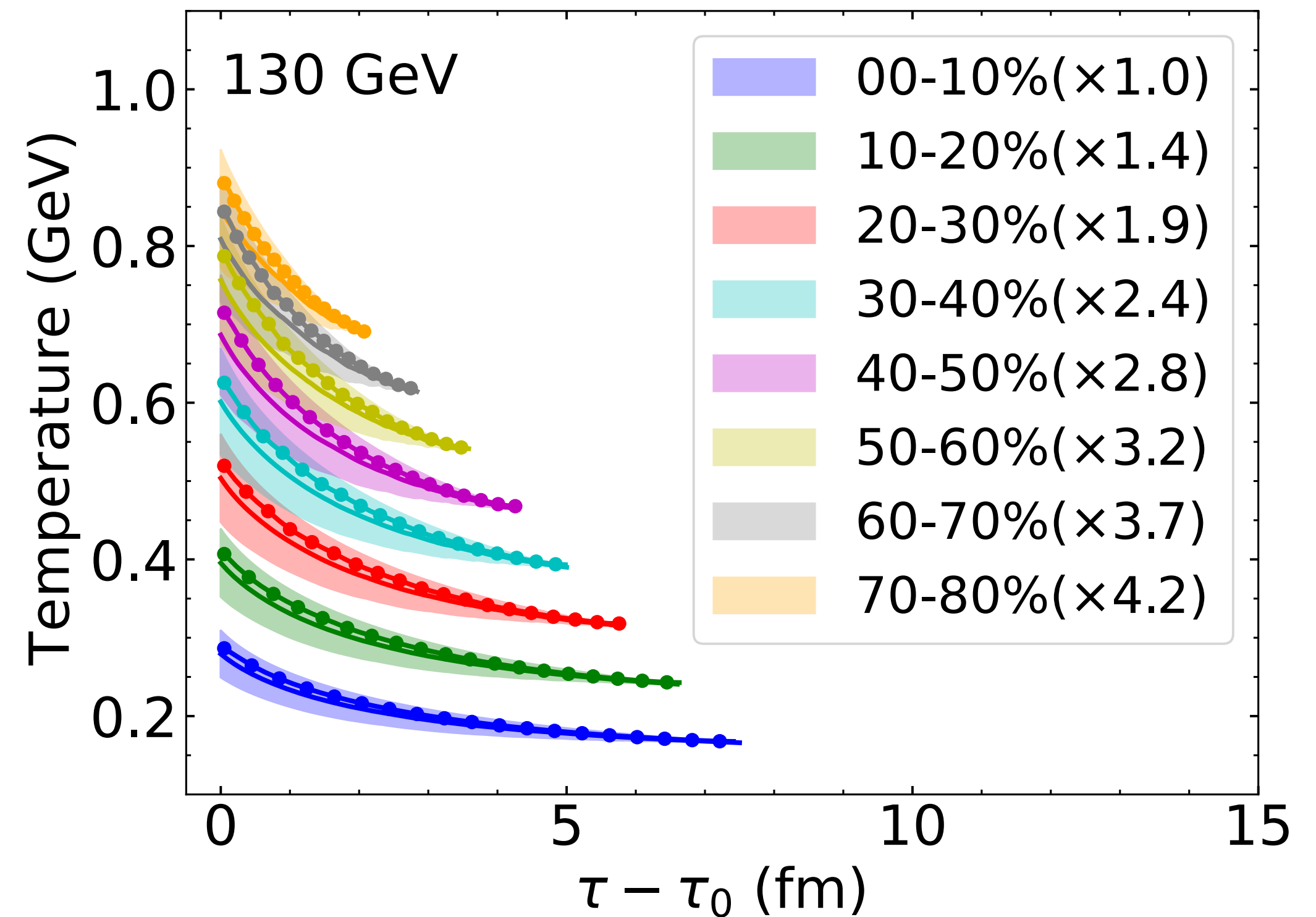
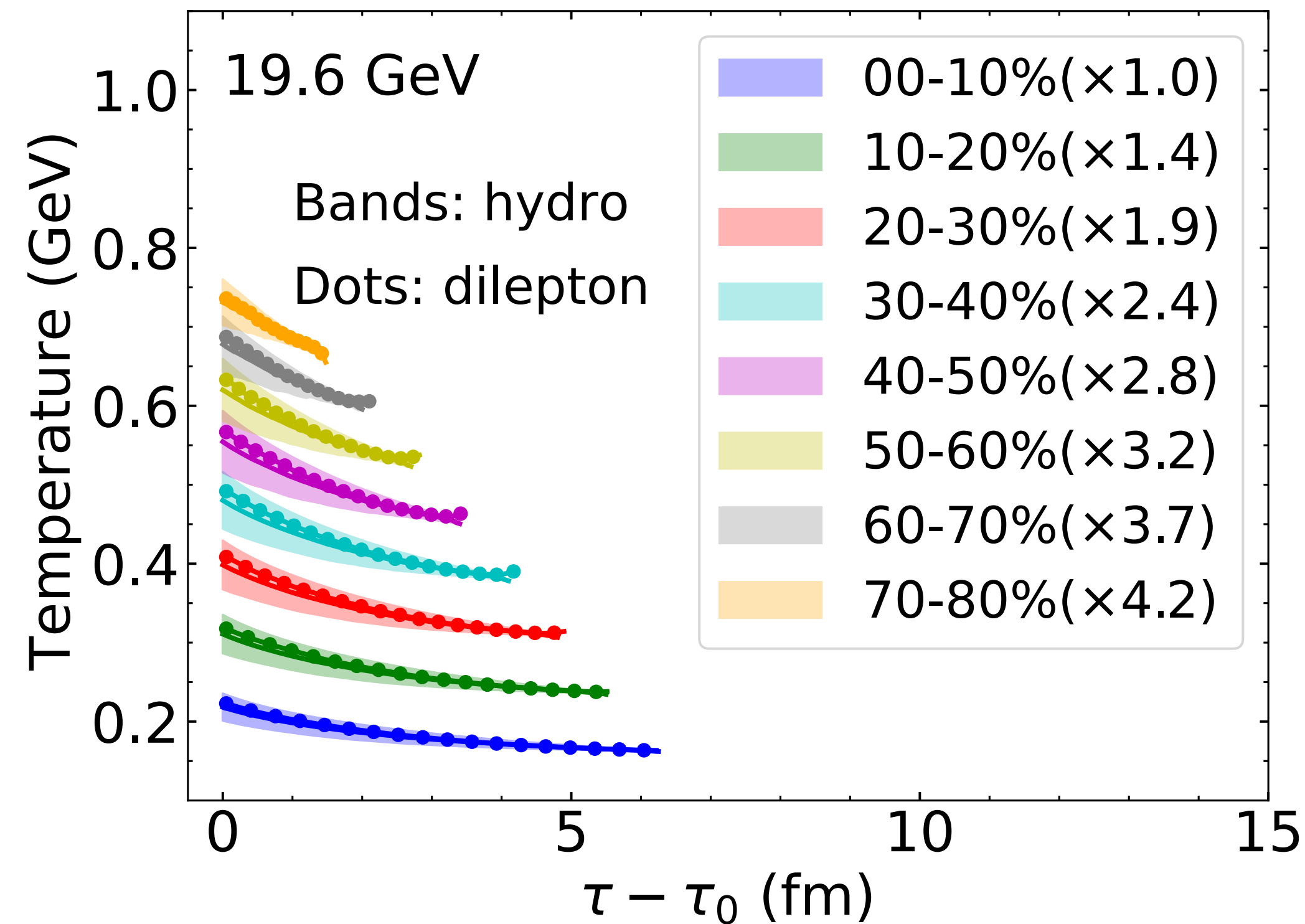


- ▶  $\mu_B$ -dependence is not significant for 7.7 GeV and higher beam energies
- ▶ At 7.7 GeV, a strong boost-non-invariant effect is observed

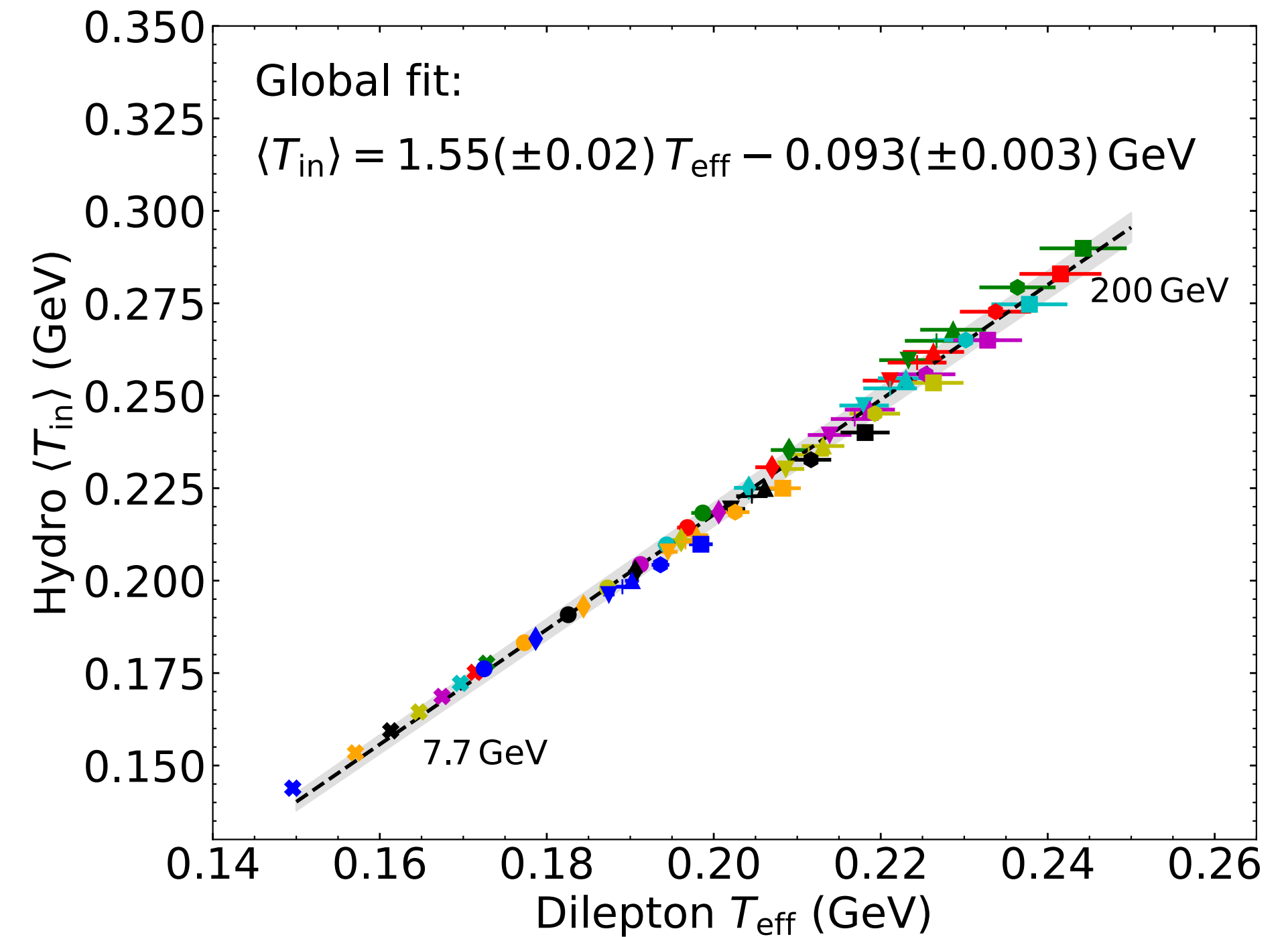
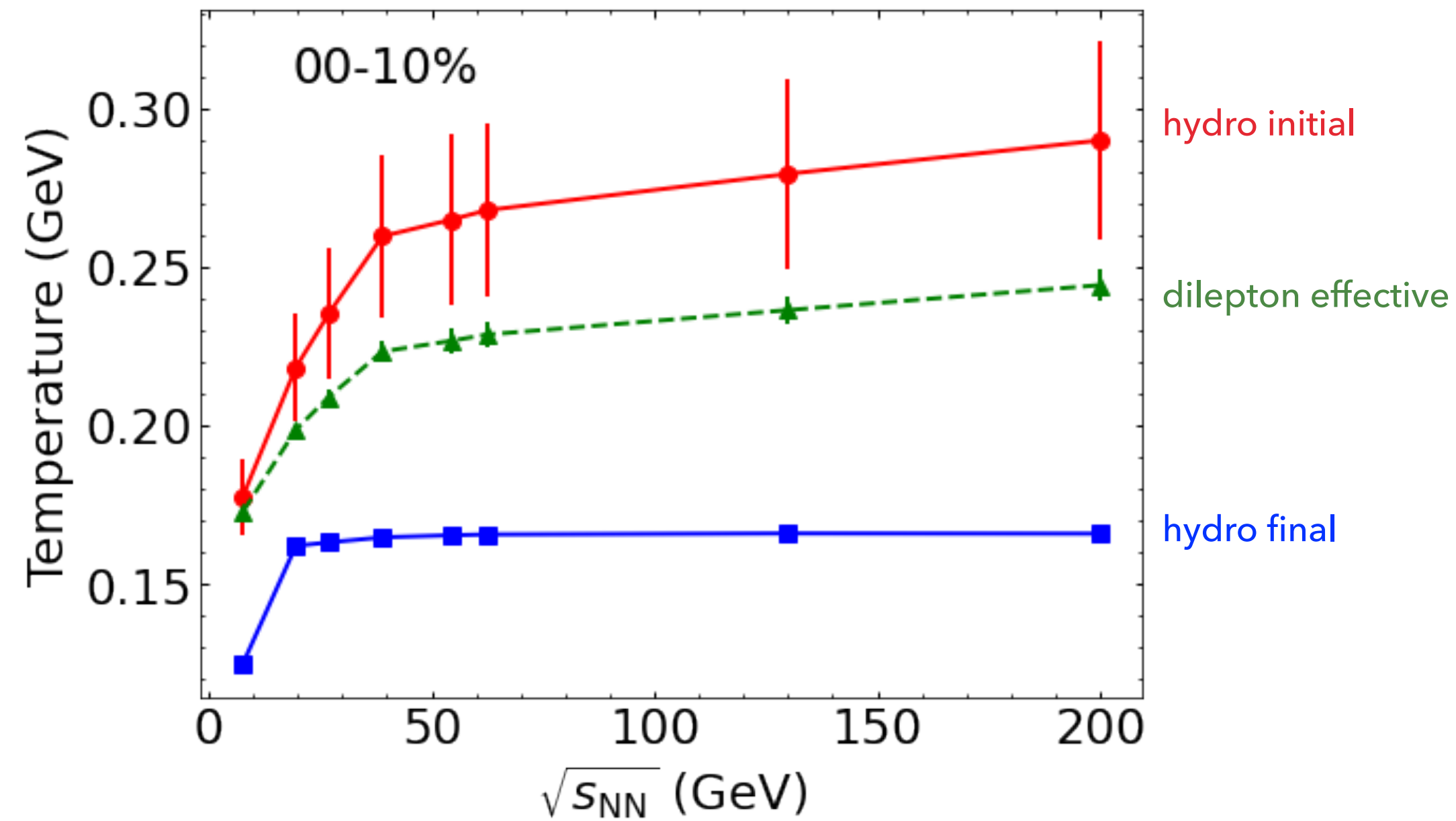




- ▶ In non-relativistic approximation, the emission rate  $\frac{dR}{dM} \propto (MT)^{3/2} e^{-M/T}$
- ▶ Thermal dileptons within  $1\text{GeV} \lesssim M \lesssim 3\text{GeV}$  for temperature extraction



- ▶ Curves & bands: hydrodynamic temperature. curve: mean temperature; band: standard deviation
- ▶ Dots: effective temperature extracted from dilepton spectra at various time steps



<https://github.com/LipeiDu/DileptonEmission>

J. Churchill, LD, C. Gale, G. Jackson & S. Jeon, PRC 109, 044915 (2024), PRL 132, 172301 (2024)

- ▶ Combining all energies and centralities, a strong correlation is observed between the initial hydro temperature and the effective temperature extracted from the dilepton spectra
- ▶ Measure the temperature of the evolving QCD fireball in a way that is unaffected by dynamical distortions

---

## **SUMMARY AND OUTLOOK**

## ▶ Physics Complexity:

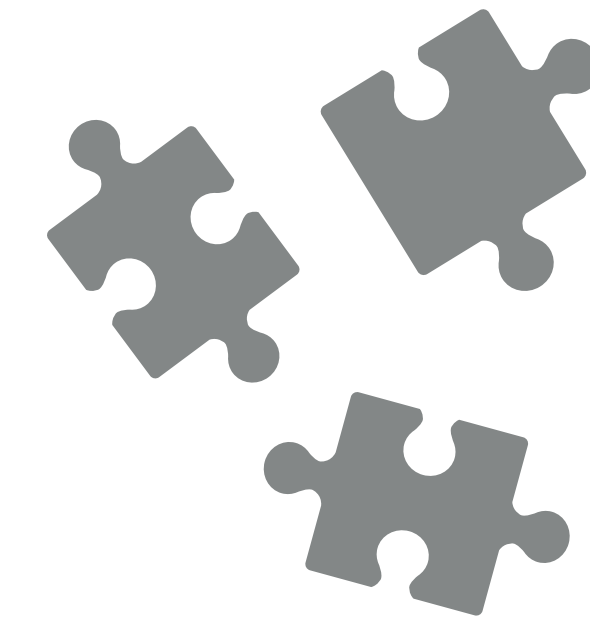
- ▶ Complicated longitudinal dynamics
- ▶ Transport of conserved charges (baryon, electric and strangeness)
- ▶ Critical effects

## ▶ Computational Demands:

- ▶ More physics ingredients
- ▶ (3+1)-dimensional simulations
- ▶ A broad range of beam energies

## ▶ Limitations in Rapidity-dependent Measurements:

- ▶ Detector coverage
- ▶ Scheduled shutdown of RHIC





## ▶ Physics Complexity:

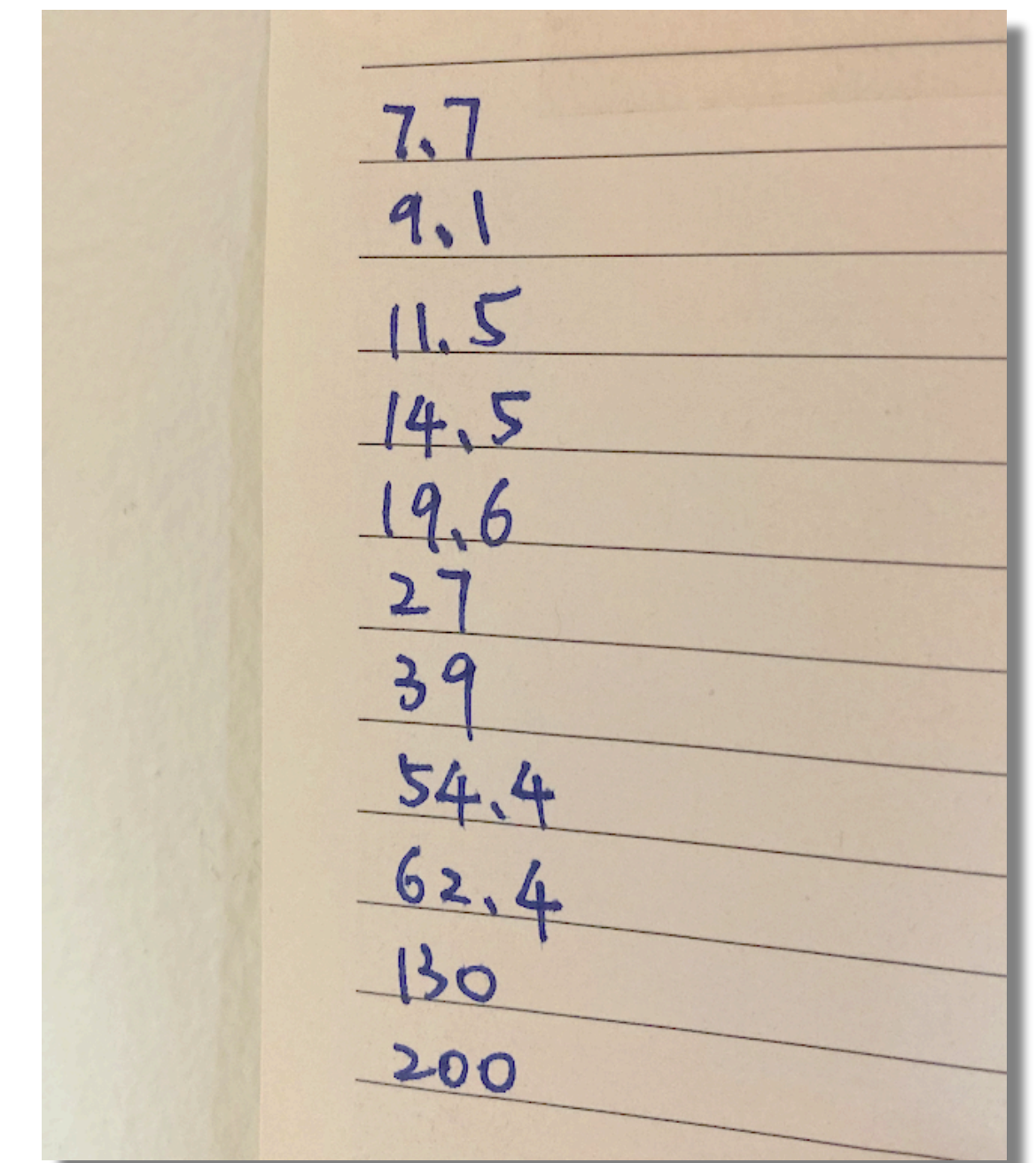
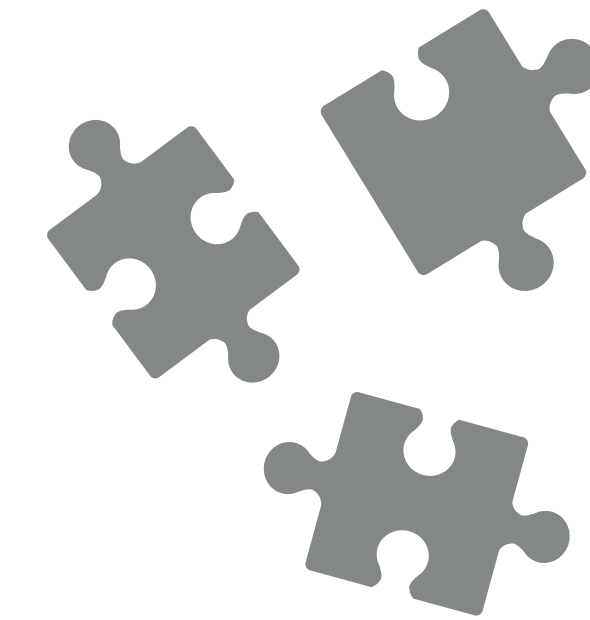
- ▶ Complicated longitudinal dynamics
- ▶ Transport of conserved charges (baryon, electric and strangeness)
- ▶ Critical effects

## ▶ Computational Demands:

- ▶ More physics ingredients
- ▶ (3+1)-dimensional simulations
- ▶ A broad range of beam energies

## ▶ Limitations in Rapidity-dependent Measurements:

- ▶ Detector coverage
- ▶ Scheduled shutdown of RHIC



## ▶ Unique Physics:

- ▶ Region to search for the QCD critical point
- ▶ QCD at high baryon density (especially, multi-messenger at  $\mu_B \neq 0$ )
- ▶ Connection to neutron star physics
- ▶ Stronger constraints from rapidity-dependent measurements
  - ▶ EOS, baryon stopping, energy deposition, etc.



## ▶ Urgent Questions:

- ▶ Constraining the longitudinal flow (both initial and final)
- ▶ Transport coefficients of charges
- ▶ Quantitative studies with limited rapidity data



## Chapter 1

### The QCD phase diagram and Beam Energy Scan physics: a theory overview

Lipei Du,<sup>1,2\*</sup> Agnieszka Sorensen,<sup>3†</sup> and Mikhail Stephanov<sup>4,5‡</sup>

<sup>1</sup>*Department of Physics, McGill University, Montreal, Quebec H3A 2T8,  
Canada*

<sup>2</sup>*Nuclear Science Division, Lawrence Berkeley National Laboratory,  
Berkeley, CA 94270, USA*

<sup>3</sup>*Institute for Nuclear Theory, University of Washington, Seattle, WA  
98195, USA*

<sup>4</sup>*Department of Physics and Laboratory for Quantum Theory at the  
Extremes, University of Illinois, Chicago, IL 60607, USA*

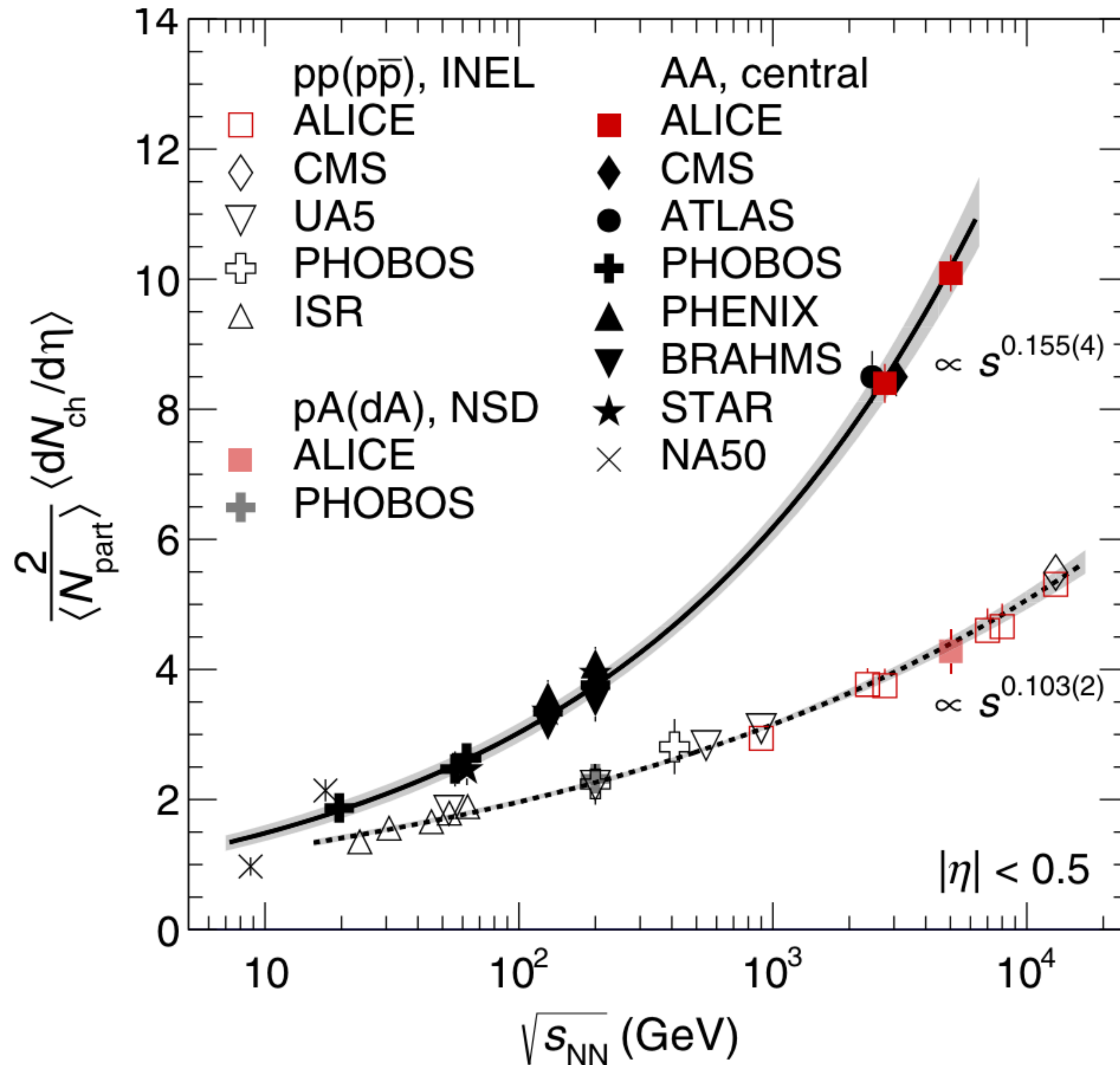
<sup>5</sup>*Kadanoff Center for Theoretical Physics, University of Chicago, Chicago,  
Illinois 60637, USA*

---

**THANK YOU FOR YOUR ATTENTION!**

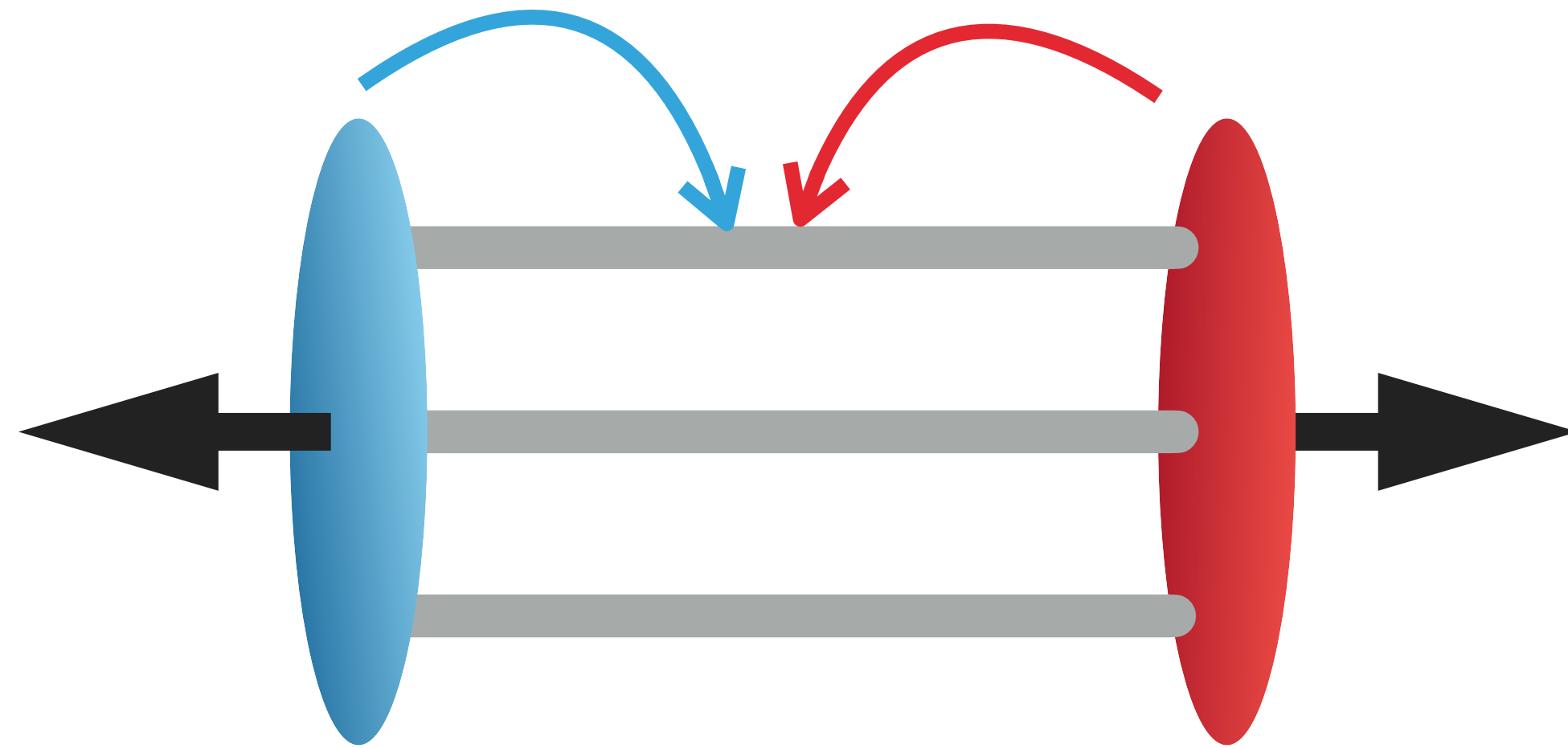


# CHARGED MULTIPLICITY SCALING

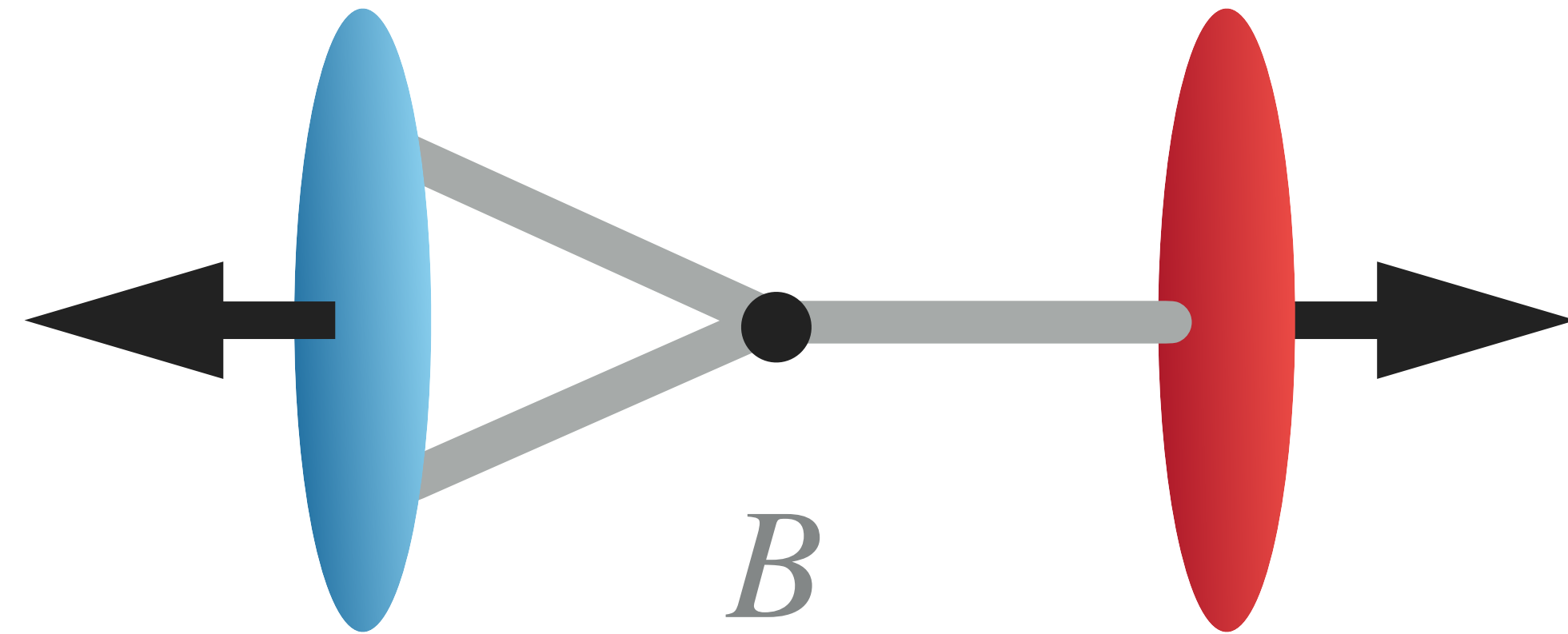




## INITIAL BARYON "STOPPING"



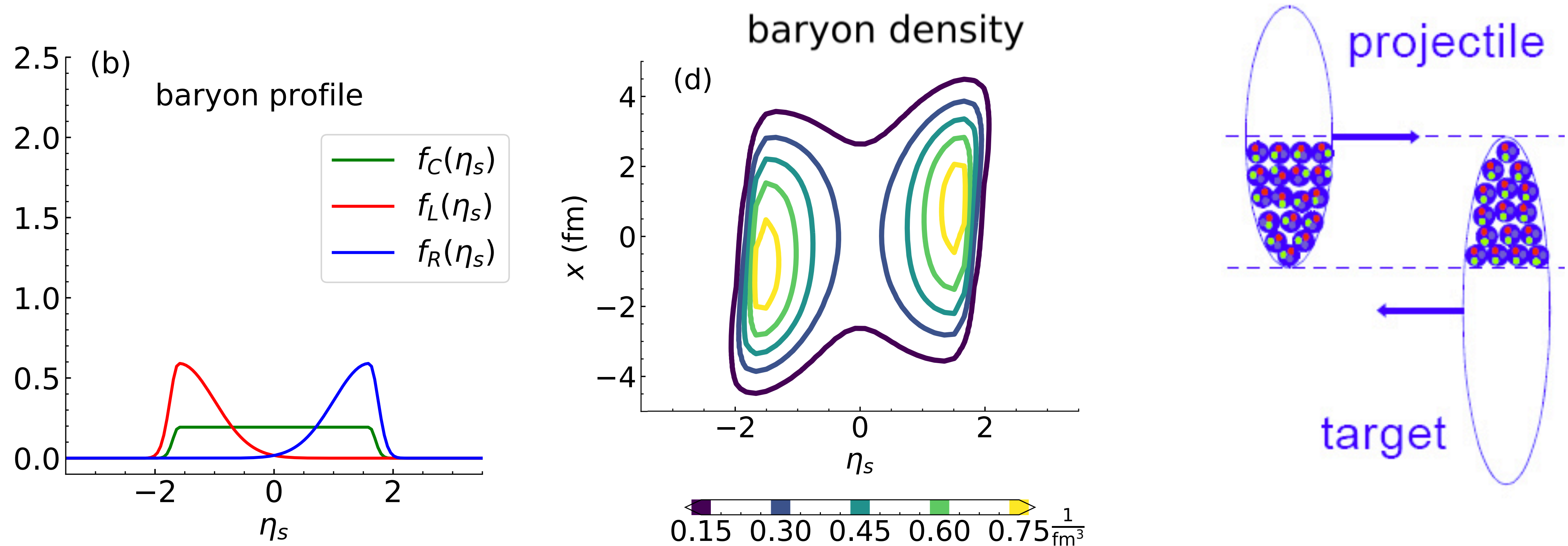
Baryons get distributed in rapidity by deceleration of the incoming nucleons



Baryons get distributed in rapidity through string junction breaking

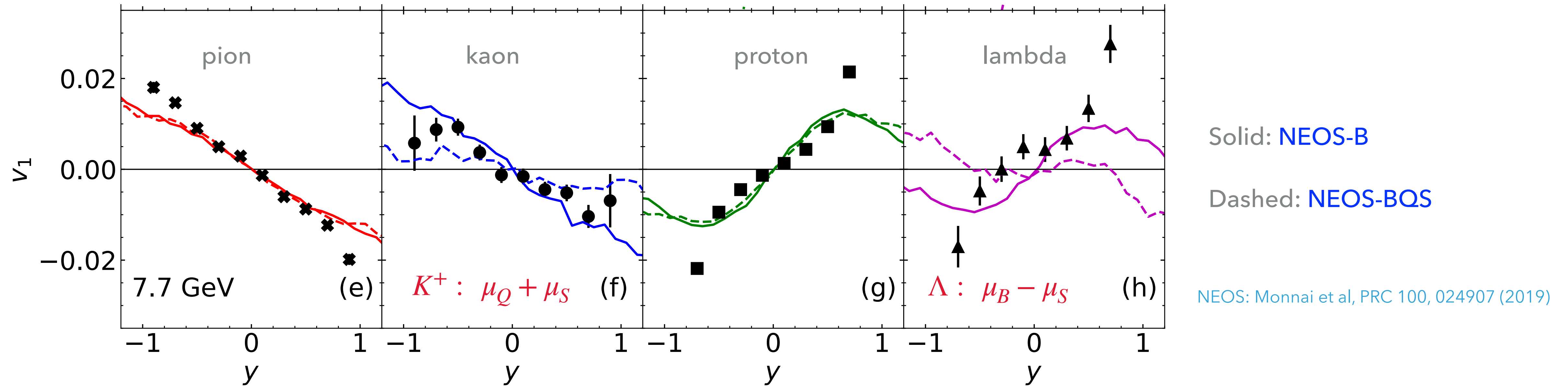
- ▶ Profound impact on understanding initial baryon distribution and energy loss
- ▶ How to differentiate "baryon deceleration" and "string junction breaking" in the initial baryon distribution?

# NEW PARAMETRIC BARYON INITIAL CONDITION




- ▶ A rapidity-independent “plateau” component in initial baryon profile & tilted baryon peaks describing the varying baryon stopping in the transverse plane

# PROBING EOS AT FINITE CHEMICAL POTENTIALS




- ▶ Two limits of EoS: **NEOS-B**,  $\mu_S = \mu_Q = 0$  and **NEOS-BQS**,  $n_S = 0, n_Q = 0.4n_B$  (2D projection of a 4D EOS)
- ▶ Local strangeness neutrality suppresses the  $v_1(y)$  of  $K^+$  and  $\Lambda$  around midrapidity, and even alters the sign of  $\Lambda$ 's  $v_1(y)$  beyond  $|y| \gtrsim 0.6$
- ▶ The  $v_1(y)$  of identified particles can be used to probe **EoS at finite chemical potentials**.

# APPLICATION OF PERTURBATIVE QCD

$$\begin{aligned}
 |\sum \mathcal{M}|^2 &= \left| \text{Drell-Yan} \right|^2 && \text{Drell-Yan} \\
 &+ \left| \text{Compton, annihilation, ...} \right|^2 + \dots && \text{Compton, annihilation, ...} \\
 &+ \left[ \text{Drell-Yan} \right] \left[ \text{Compton, annihilation, ...} \right]^* + \text{c.c.} && \text{interference} \\
 &+ \dots
 \end{aligned}$$


$$\text{Im} \left[ \text{self-energy diagrams} + \dots \right]$$

self-energy,  $\Pi_{\mu\nu}$



[Weldon (1990)] , [Bödeker, Sangel, Wörmann (2015)]

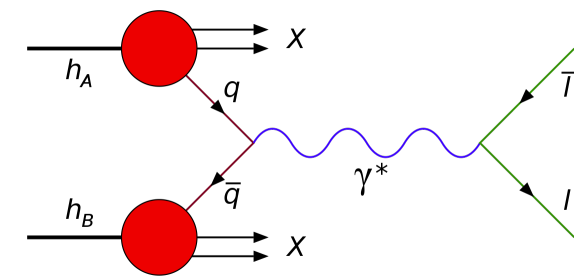


# DILEPTON SPECTRA

STAR, PLB 750 (2015) 64-71

## High-mass region (HMR)

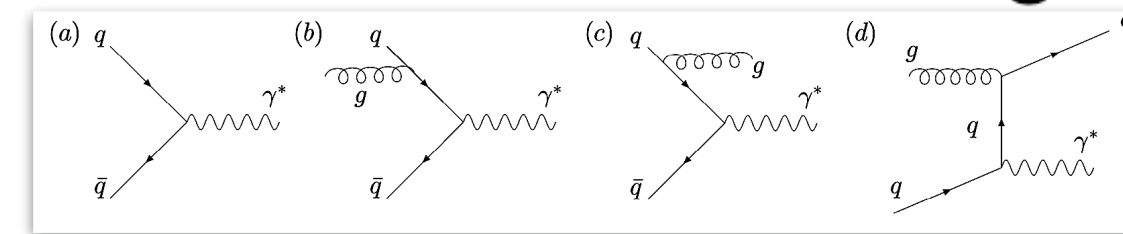
▶ Drell-Yan process



▶ decays of  $J/\psi$

## Intermediate-mass region (IMR)

▶ thermal emission from QGP



▶ semileptonic decays from open heavy flavor-antiflavor pair, e.g.  $D/\bar{D}$

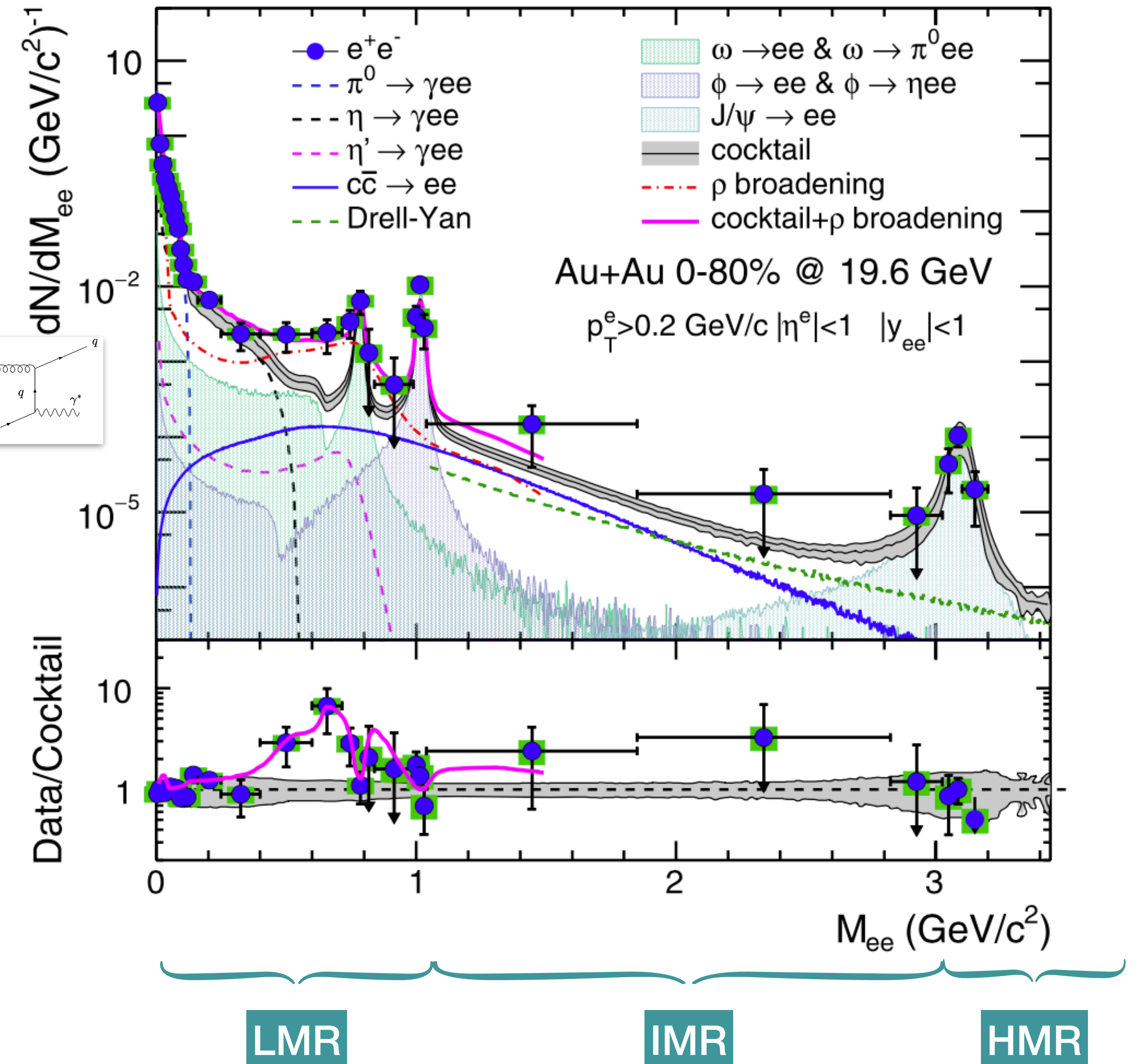
## Low-mass region (LMR)

▶ thermal emission from hadronic matter

▶ direct decays of  $\rho/\omega/\phi$  ( $\rho$  is short-lived)

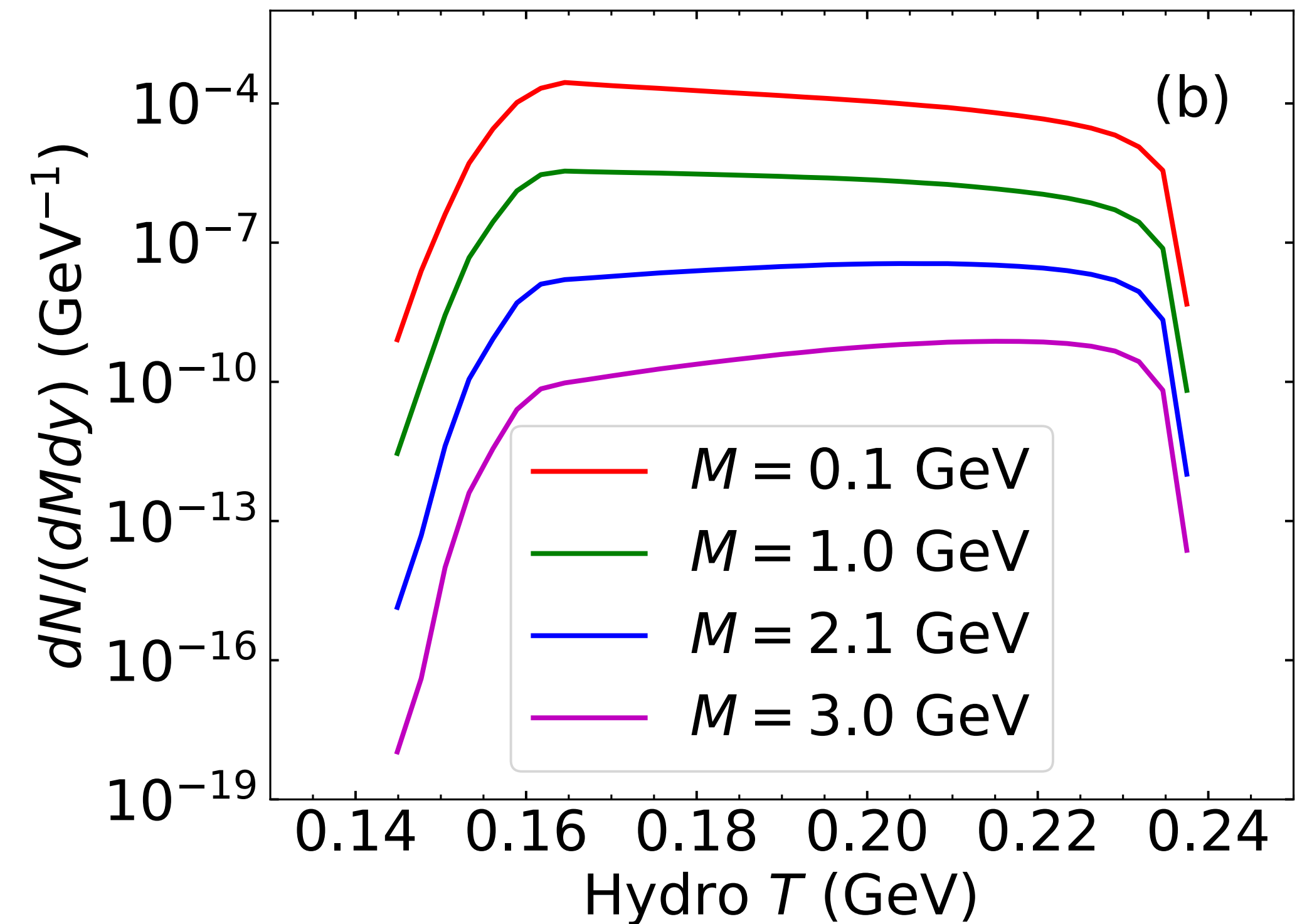
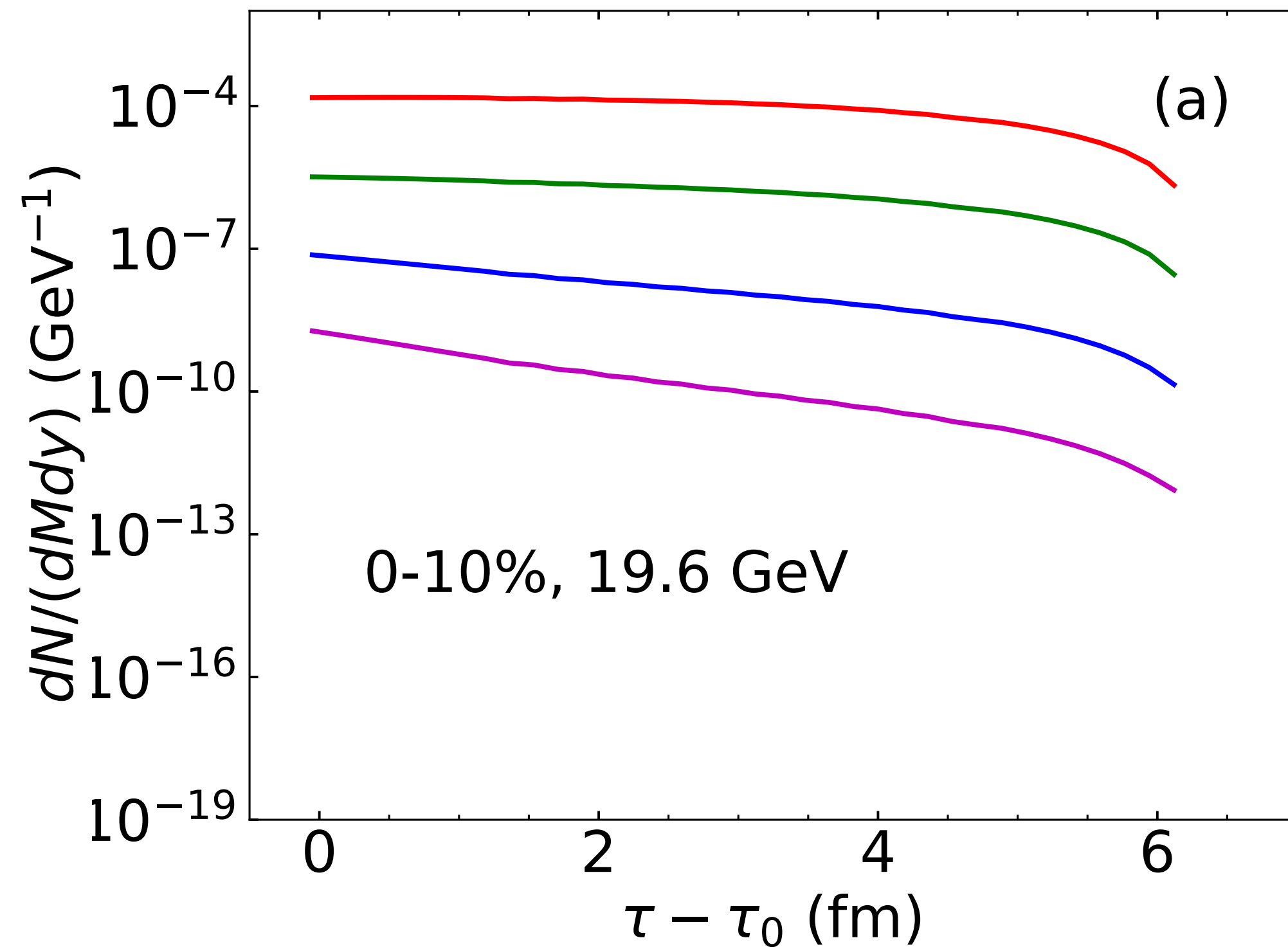
▶ Dalitz (three body) decays of  $\pi^0/\eta/\eta'$

Dilepton cocktail: late decays of hadrons





## DILEPTON PRODUCTION IN $T$ AND $\tau$

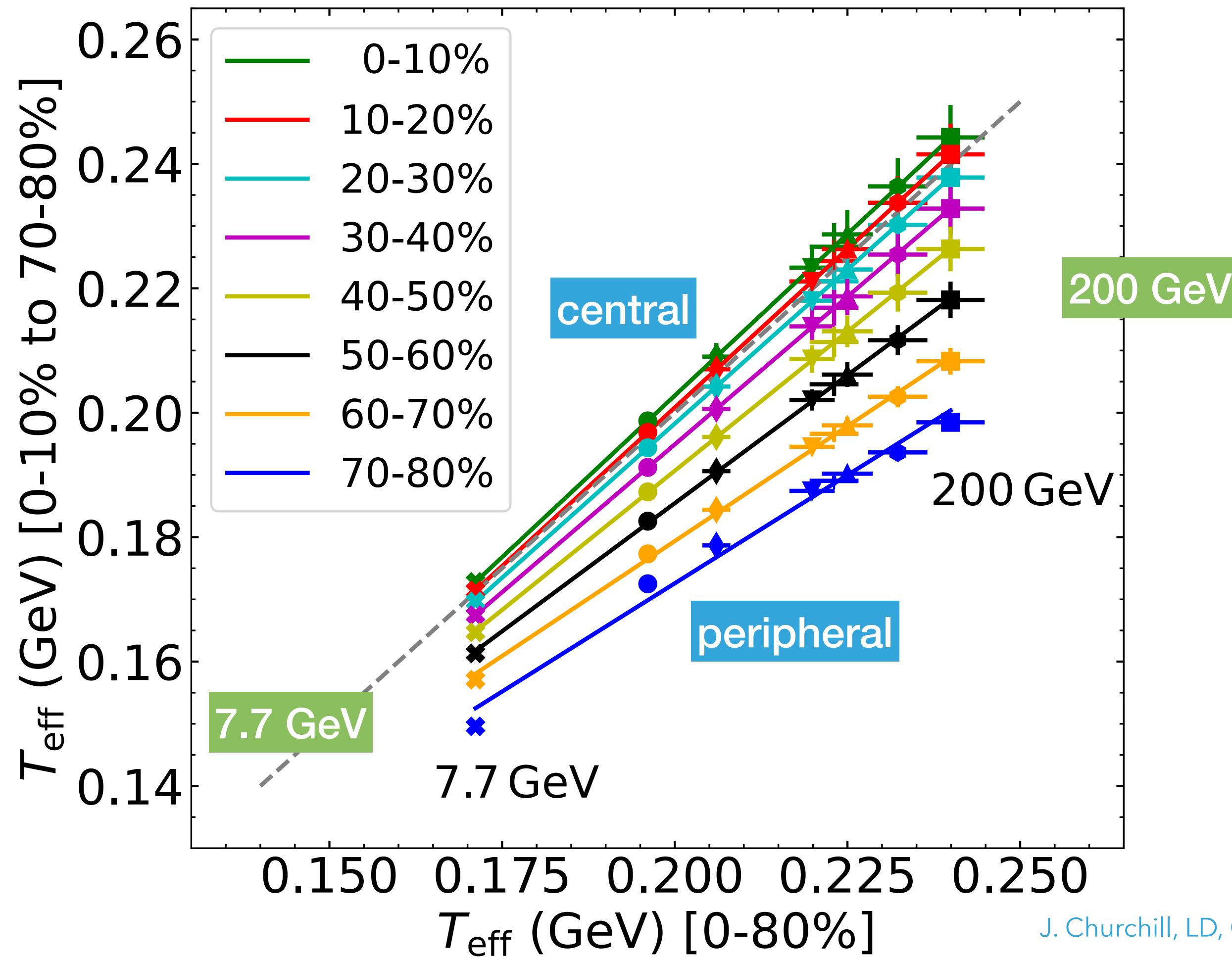


▶ Two effects at play:

- ▶ The emission rate decreases as the temperature decreases
- ▶ The volume of the system increases with time

J. Churchill, LD, C. Gale, G. Jackson & S. Jeon, PRC 109, 044915 (2024), PRL 132, 172301 (2024)

# THERMAL DILEPTON AS THERMOMETER



- ▶ The effective temperatures extracted from the dilepton spectra in 0-80% centrality are quite close to those in 10-20% centrality across all beam energies