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15<sup>th</sup> Workshop on Critical Point and Onset of Deconfinement  
LBL, Berkeley, California, USA  
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# Production of light- & hypernuclei in UrQMD

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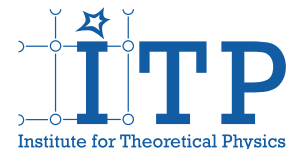
FIAS Frankfurt Institute  
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Stiftung  
Polytechnische  
Gesellschaft  
Frankfurt am Main

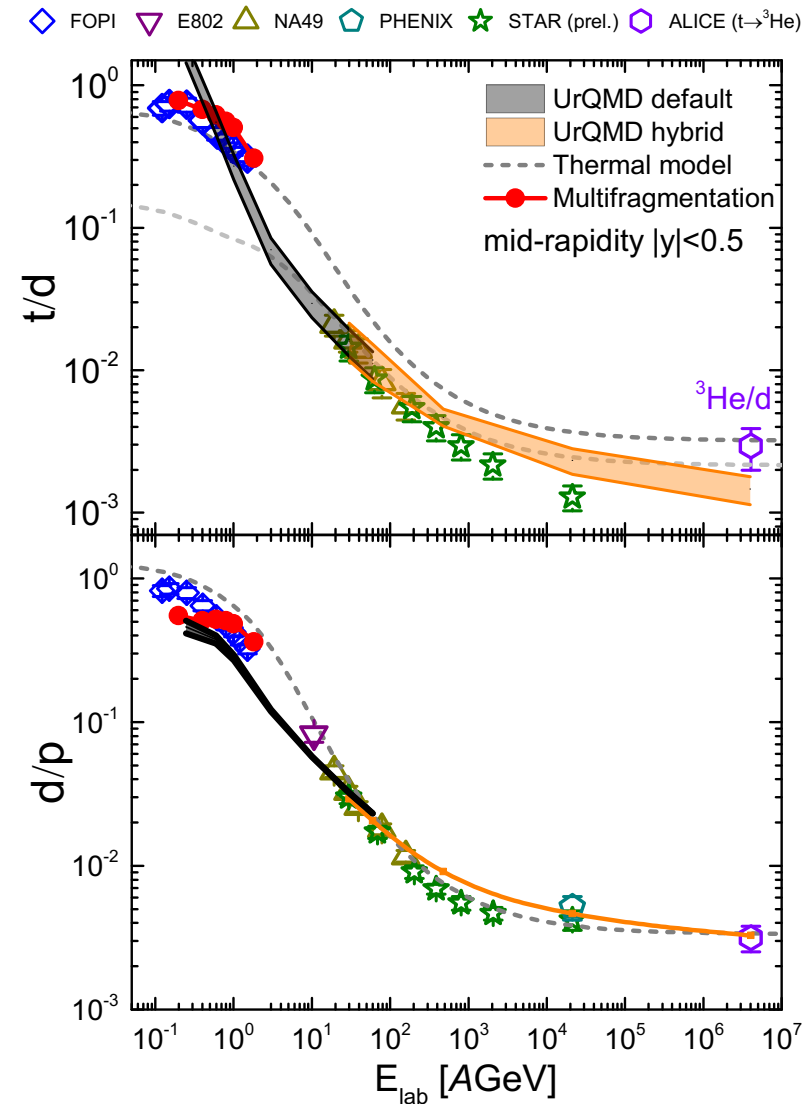
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# (Hyper-)Nuclei motivation

- Different models provide a good description of nuclei production in heavy ion collisions
- This is true over wide range of energies
- Despite the fact that nuclei are only weakly bound compared to the temperature of the system
- $B = 2 \text{ MeV}$ ,  $T = 100\text{-}150 \text{ MeV}$  ?



# Methods of cluster production

## Wigner functions

- Projection on Hulthen wave function
- No free parameters
- No orthogonality of states

M. Kachelriess et al. Eur.Phys.J.A 57 (2021)  
M. Gyulassi et al. Nucl.Phys.A 402 (1983)

## Kinetic production

- Introduce explicit processes, e.g.  $n\rho\pi \rightarrow d\pi$
- Dynamical treatment
- Mimic 3-body interactions

J. Staudenmaier et al. Phys.Rev.C 104 (2021) 3, 034908  
D. Oliinychenko et al. Phys.Rev.C 99 (2019) 4, 044907

## Potential

- Hamiltonian which binds cluster
- Might involve complicated forces
- Difficult for small systems

J. Aichelin, et al. Phys.Rev.C 101 (2020) 4, 044905  
S. Gläsel, et al. Phys.Rev.C 105 (2022) 1, 014908

## Coalescence

- Employ cut-off parameters
- Event-by-event possible
- 2 free, energy-independent parameters

S. Butler, C. Pearson. Phys.Rev. 129 (1963) 836-842  
S. Sombun et al. Phys.Rev.C 99 (2019) 1, 014901

## Thermal emission

- Clusters in partition sum
- No free parameter

P. Braun-Munzinger, et al. Phys.Lett.B 344 (1995) 43-48  
A. Andronic, et al. Nature 561 (2018) 7723, 321-330  
V. Vovchenko, et al. Phys.Lett. B (2020) 135746

## Multifragmentation

- Break up of thermal nuclear system
- Microcanonical ensembles
- Deexcitation via Fermi break up

Bondorf et al. Phys.Rept. 257 (1995) 133-221  
Steinheimer et al. Phys.Lett.B 714 (2012) 85-91

# Coalescence

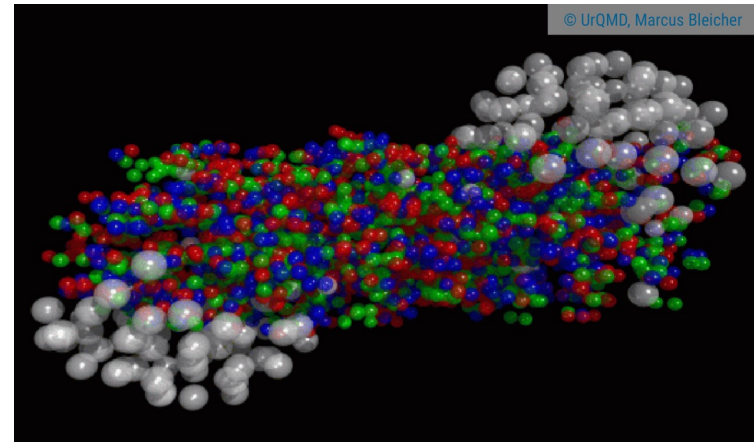
- Clusters are weakly bound compared to momentum transfer (temperature)
- Clusters are formed after kinetic freeze-out
- Coalescence: Cluster is formed if correct constituents occupy certain phase space volume

$$\frac{dN}{d^3k} = g \int dp_1^3 dp_2^3 dx_1^3 dx_2^3 f_A(p_1, x_1) f_B(p_2, x_2) \rho_{AB}(\Delta x, \Delta p) \delta(k - (p_1 + p_2))$$

- Need realistic phase space distribution functions of nucleons  
→ Use microscopic transport model keeping all n-body correlations

# Ultra-relativistic Quantum Molecular Dynamics

- Hadron/String transport approach
- Based on propagation of hadrons
- Rescattering among hadrons fully included
- String excitation and decay (LUND model, PYTHIA)
- Solution for the time dependent n-body distribution of hadrons
- Collision term includes more than 100 hadrons up to 4 GeV in mass
- Soft/Hard Skyrme or CMF EoS can be switched on



# Box-Coalescence

1. Boost into local rest frame of each possible nucleon+nucleon pair with the correct isospin combination at kinetic freeze-out. If relative distance  $\Delta x < \Delta x_{max}$  and relative momentum  $\Delta p < \Delta p_{max}$  the two-nucleon system is marked a deuteron candidate.
2. Boost into local rest frame of deuteron+nucleon and check again if  $\Delta x < \Delta x_{max}$  and  $\Delta p < \Delta p_{max}$ . A triton or  ${}^3\text{He}$  is then formed with a probability of 1/12 at the position  $r_{NNN} = (r_1 + r_2 + r_3)/3$  and with momentum  $p_{NNN} = p_1 + p_2 + p_3$

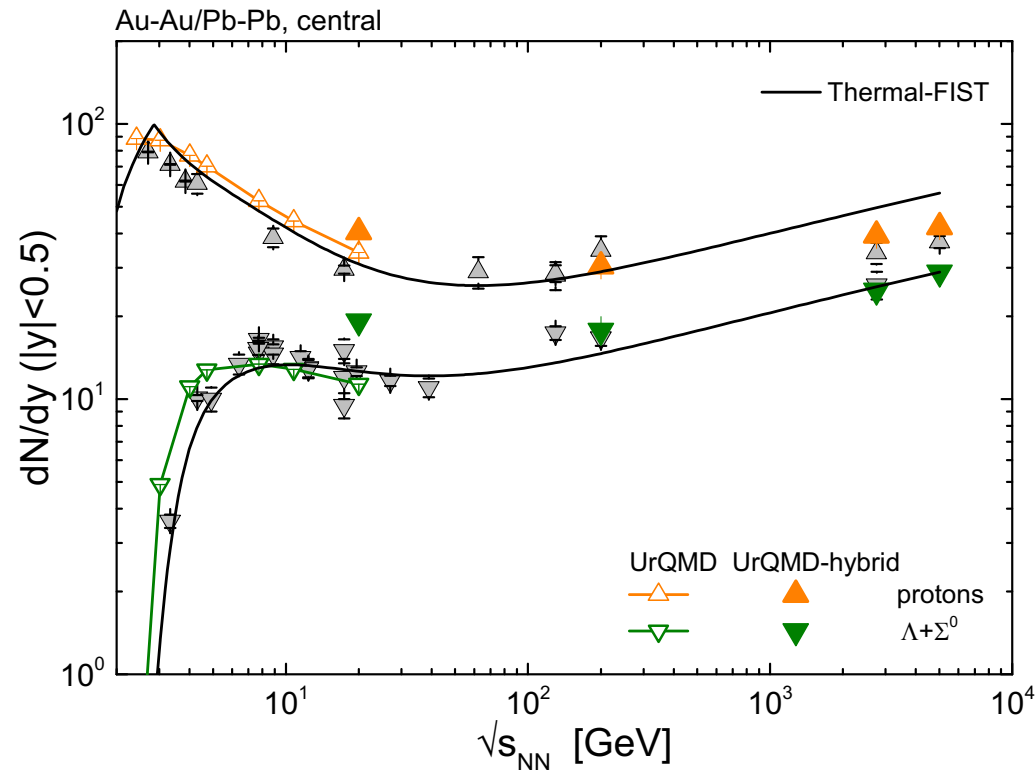
→ Straight forward extension to hypernuclei

	deuteron	${}^3\text{H}$ or ${}^3\text{He}$	${}^4\text{He}$	${}^3_{\Lambda}\text{H}$
spin-isospin	3/8	1/12	1/96	1/12
$\Delta r_{max}$ [fm]	4.0	3.5	3.5	9.5
$\Delta p_{max}$ [GeV]	0.25	0.32	0.41	0.15

S. Sombun et al. Phys.Rev.C 99 (2019) 1, 014901  
 P. Hillmann et al. J.Phys.G 49 (2022) 5, 055107  
 T. Reichert et al. Phys.Rev.C 107 (2023) 1, 014912

# Stable hadron multiplicities

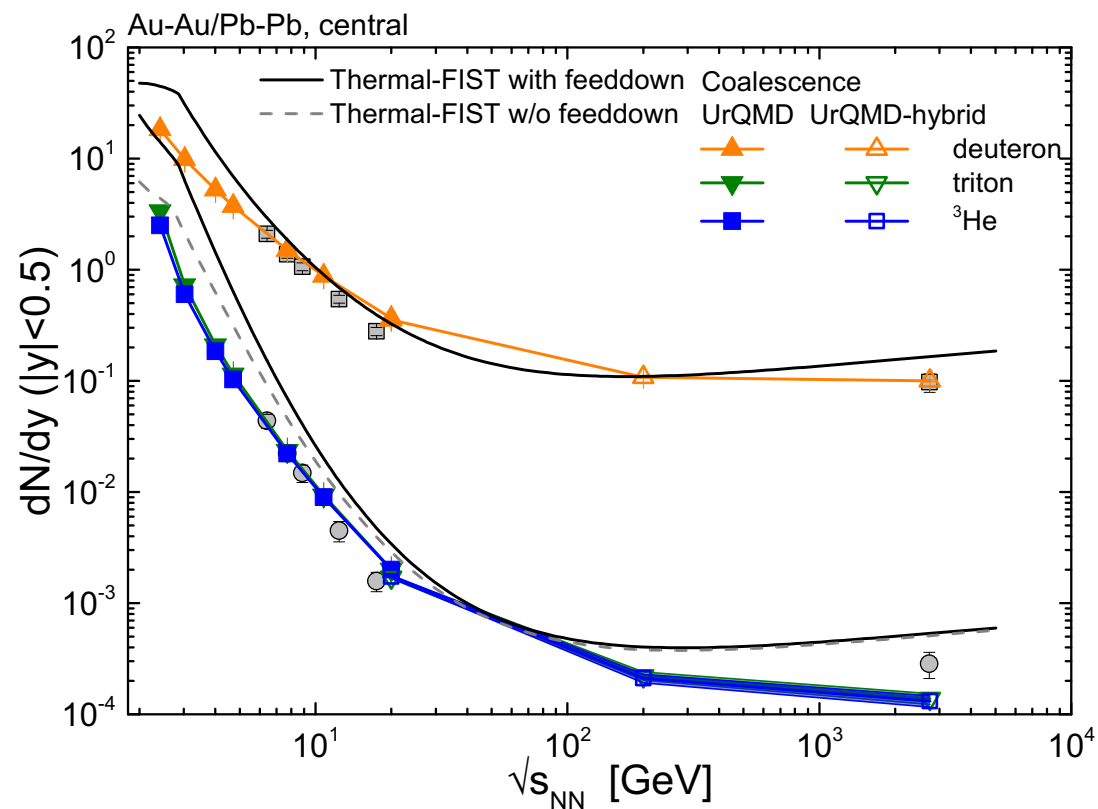
- Good description of baryon multiplicities over wide range of energies
- Too much proton stopping at intermediate energies
- Cascade model gives too much strangeness at low beam energies and too little at high energies
- Hybrid models include GC strangeness production



Reichert et al. Phys.Rev.C 107 (2023) 1, 014912

# Light nuclei multiplicities

- d, t and  $^3\text{He}$  are well reproduced
- Differences between t and  $^3\text{He}$  at low beam energies due to isospin asymmetry
- Slightly too much stopping at intermediate energies
- ALICE: d well described,  $^3\text{He}$  seems underestimated



Reichert et al. Phys.Rev.C 107 (2023) 1, 014912

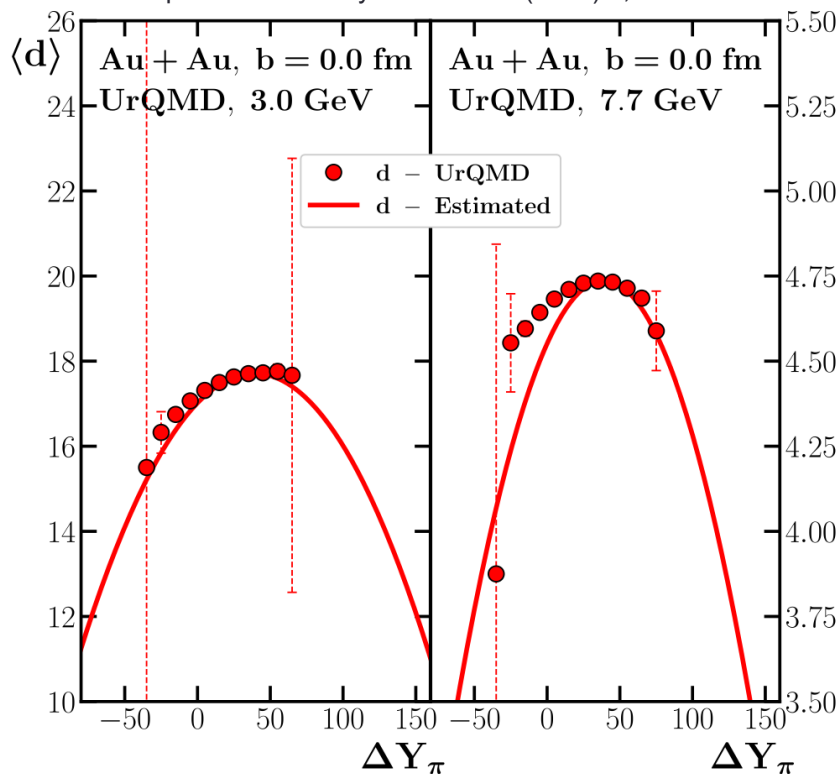
→ Clusters probe interesting physics across all energies



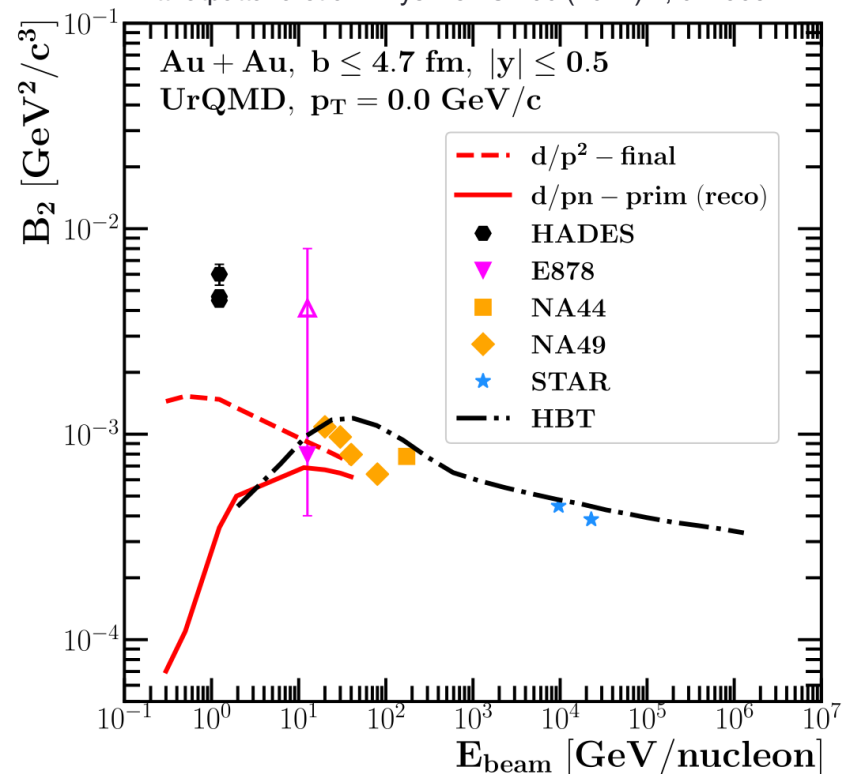
# Light nuclei multiplicities vs. net-isospin

- Nuclei yields are sensitive to net-isospin (here:  $\Delta\pi = \pi^- - \pi^+$ )
- Allows to distinguish from (grand-canonical) thermal emission
- Has to be taken into account to correct  $B_2$  at low energies

Kittiratpattana et al. Phys.Rev.C 107 (2023) 4, 044911

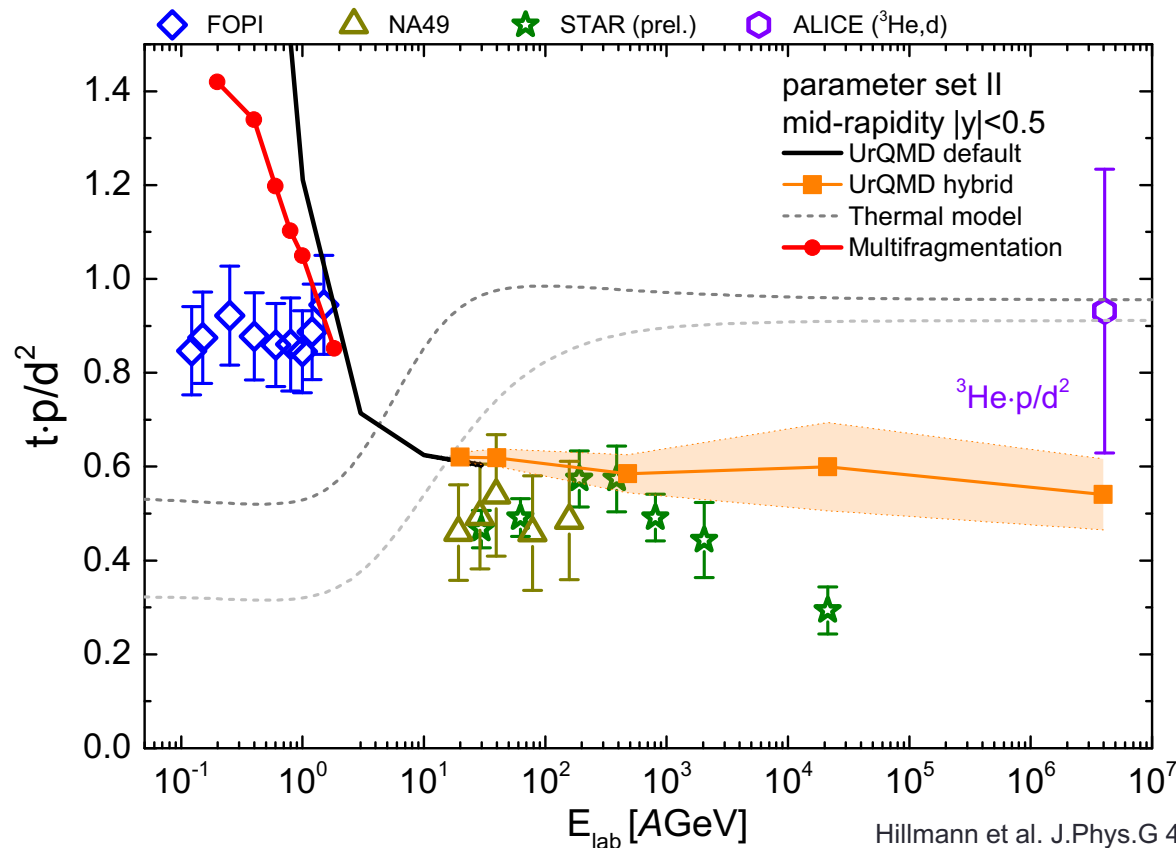


Kittiratpattana et al. Phys.Rev.C 106 (2022) 4, 044905



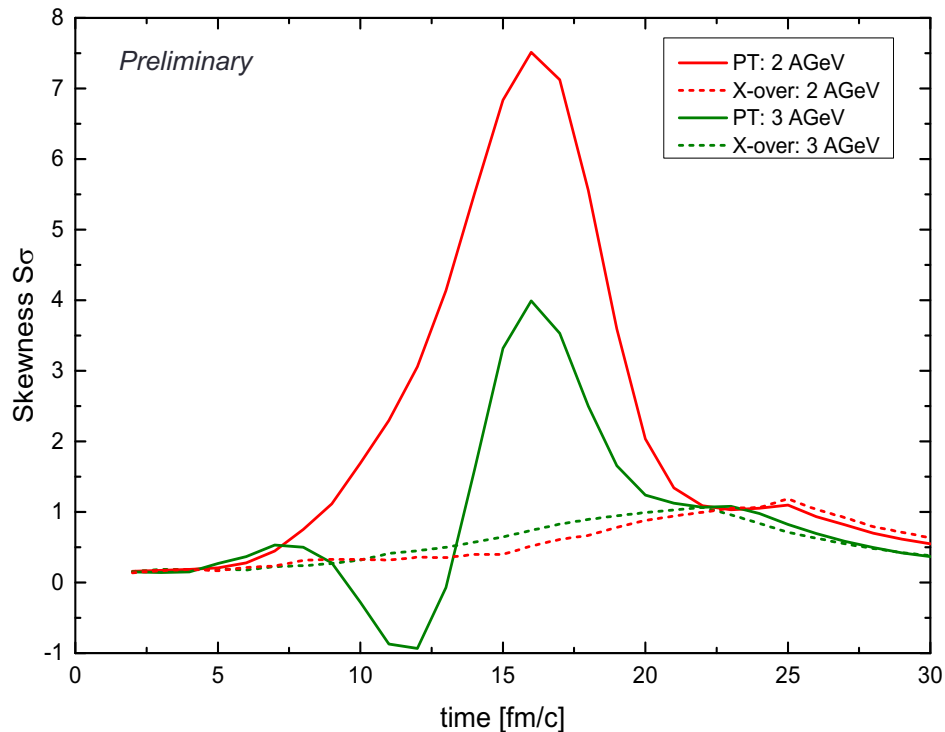
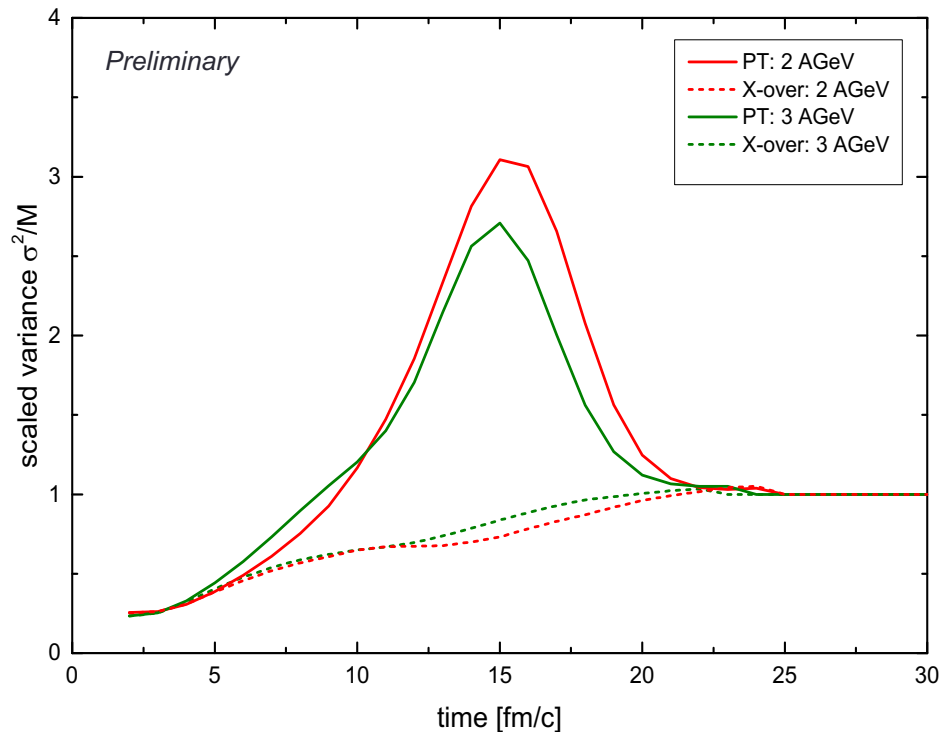
# The $t \cdot p/d^2$ ratio

- The double ratio  $t \cdot p/d^2$  is proposed to be sensitive to spatial baryon fluctuations at freeze-out Sun et al. Phys.Lett.B 781 (2018) 499-504



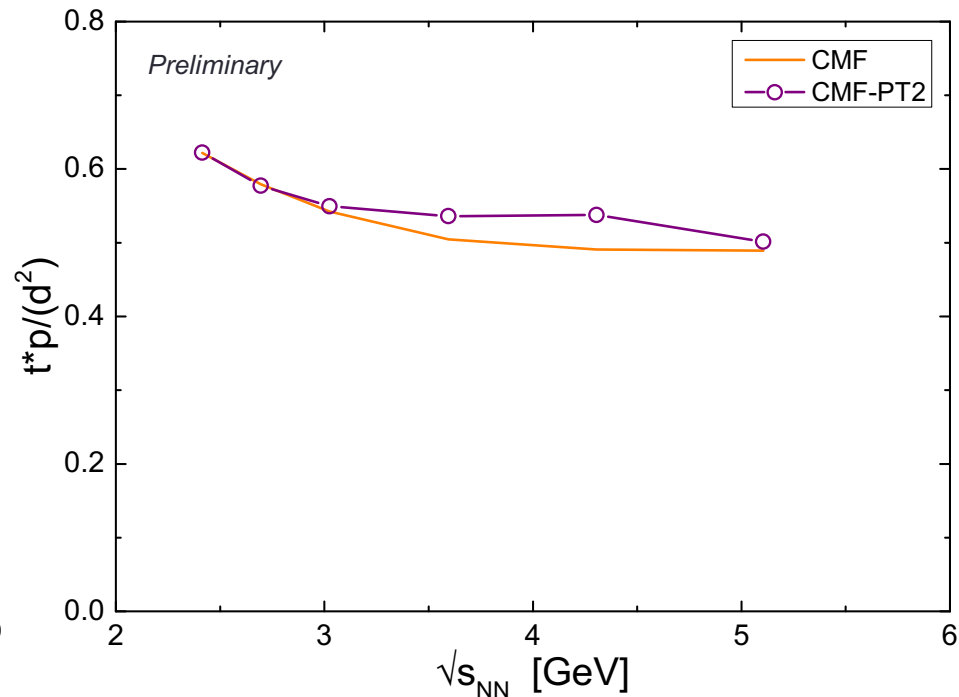
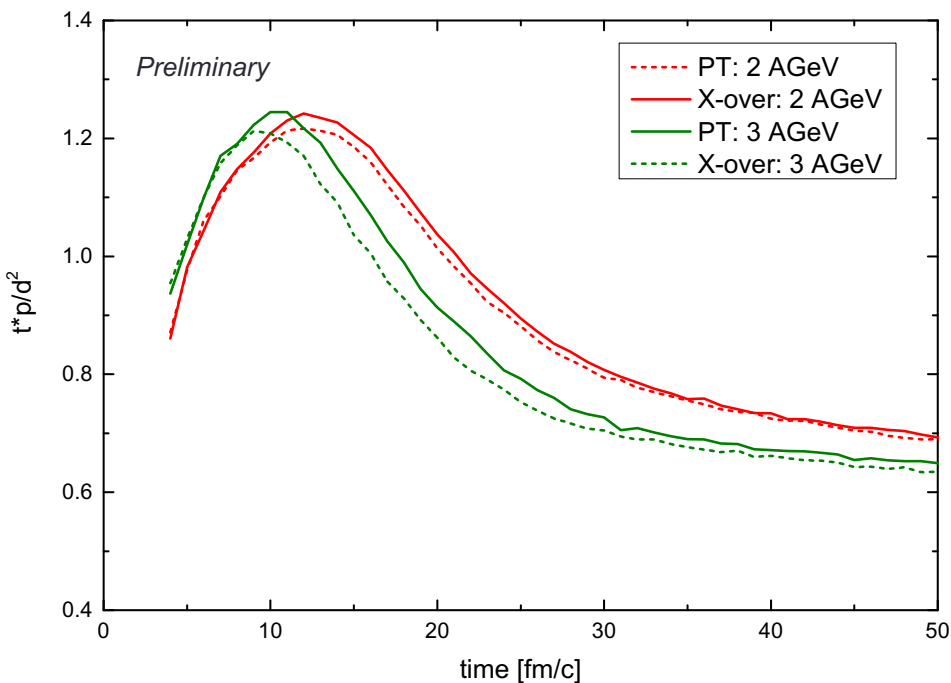
# Light nuclei fluctuations

- The double ratio  $t \cdot p/d^2$  is proposed to be sensitive to spatial baryon fluctuations at freeze-out
- Can be checked in UrQMD as a function of time
- Both  $\sigma^2/M$  and  $S\sigma$  show clear signal in coordinate space



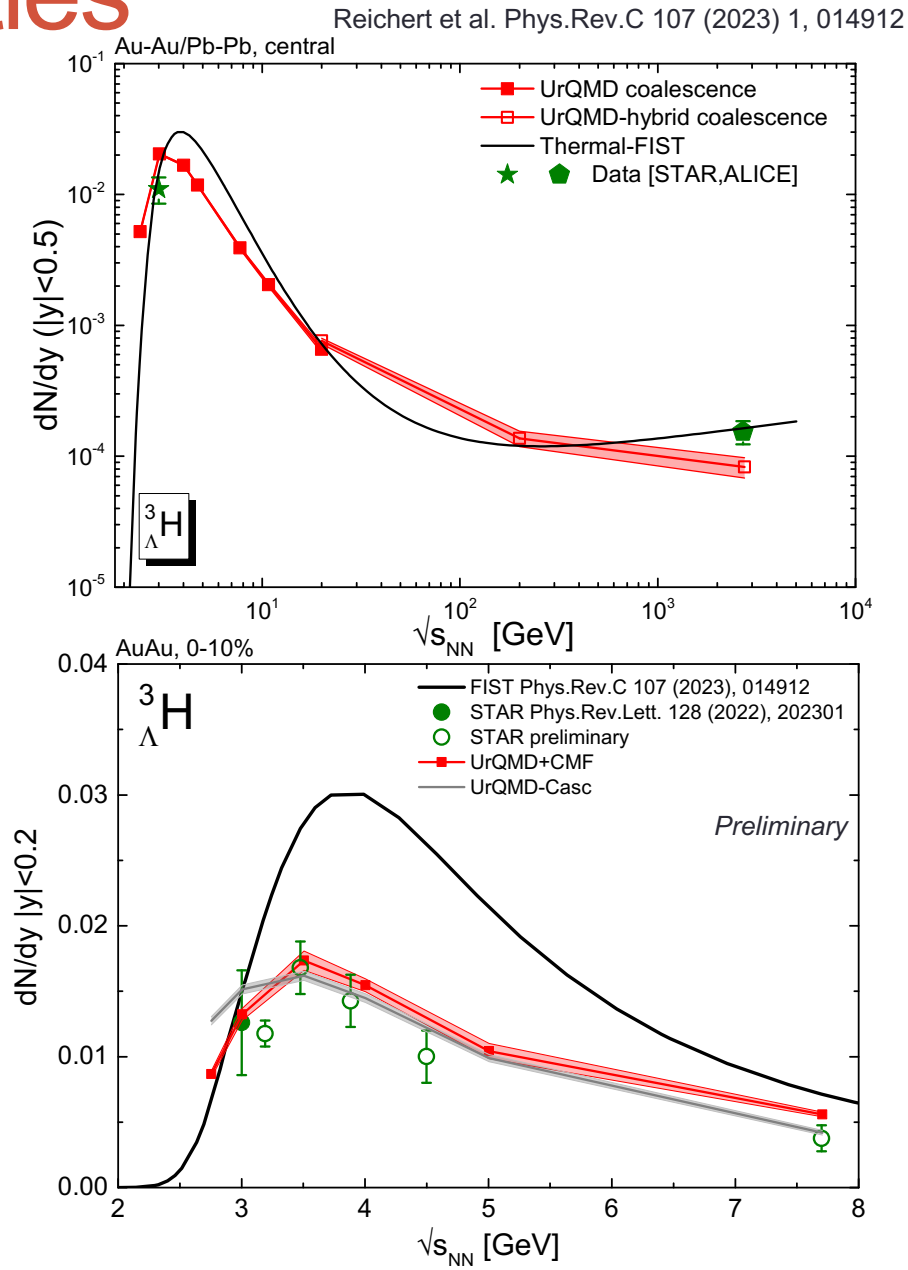
# Light nuclei fluctuations

- Only small enhancement in time dependence of  $t \cdot p/d^2$  even with strong fluctuations
- Only small enhancement at freeze-out in the scenario with phase transition



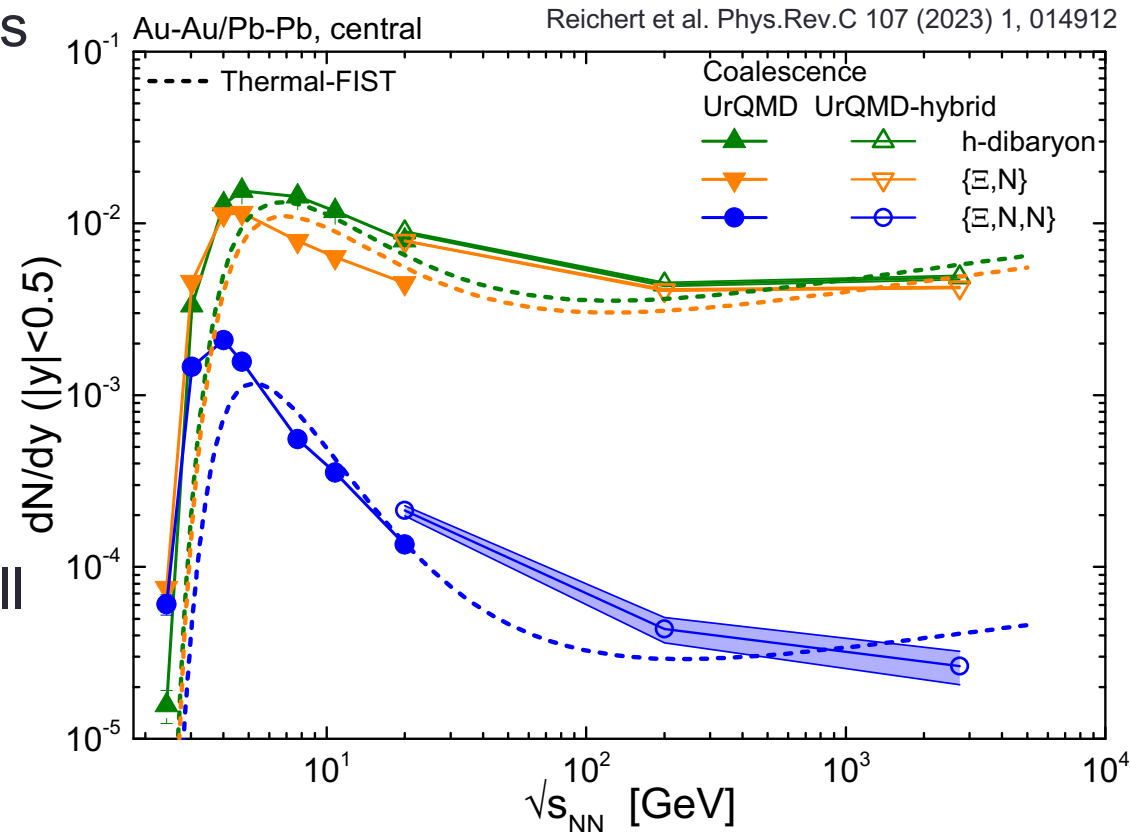
# Hypernuclei multiplicities

- Data on  ${}^3_{\Lambda}\text{H}$  multiplicities is scarce
- Strangeness at very low energies is overestimated (potential effects)
- Strangeness at intermediate energies is underestimated (the horn)
- Similar to the  ${}^3\text{He}$ ,  ${}^3_{\Lambda}\text{H}$  seems underestimated compared to ALICE data



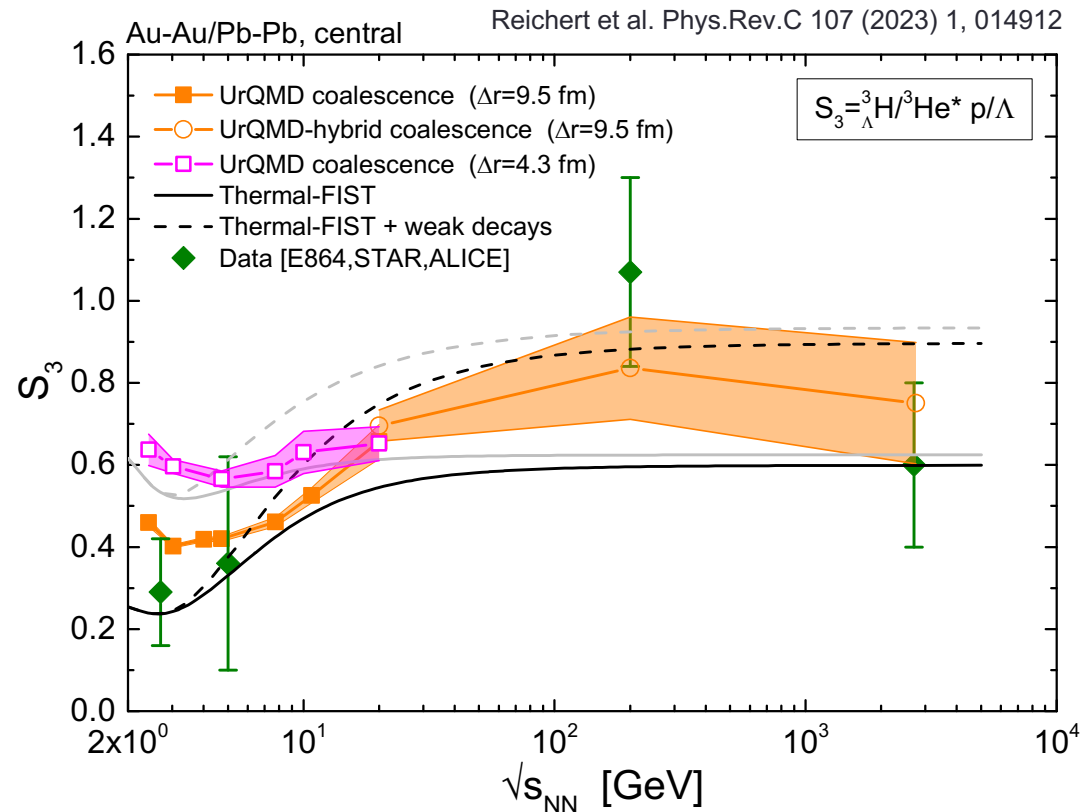
# Hypernuclei multiplicities

- Using the same parameters as for hypertriton we can predict multi-hypernuclear objects
- Most are unlikely to be bound?
- Note: shown is sum over all possible isospin combinations
- Results consistent with previous estimates



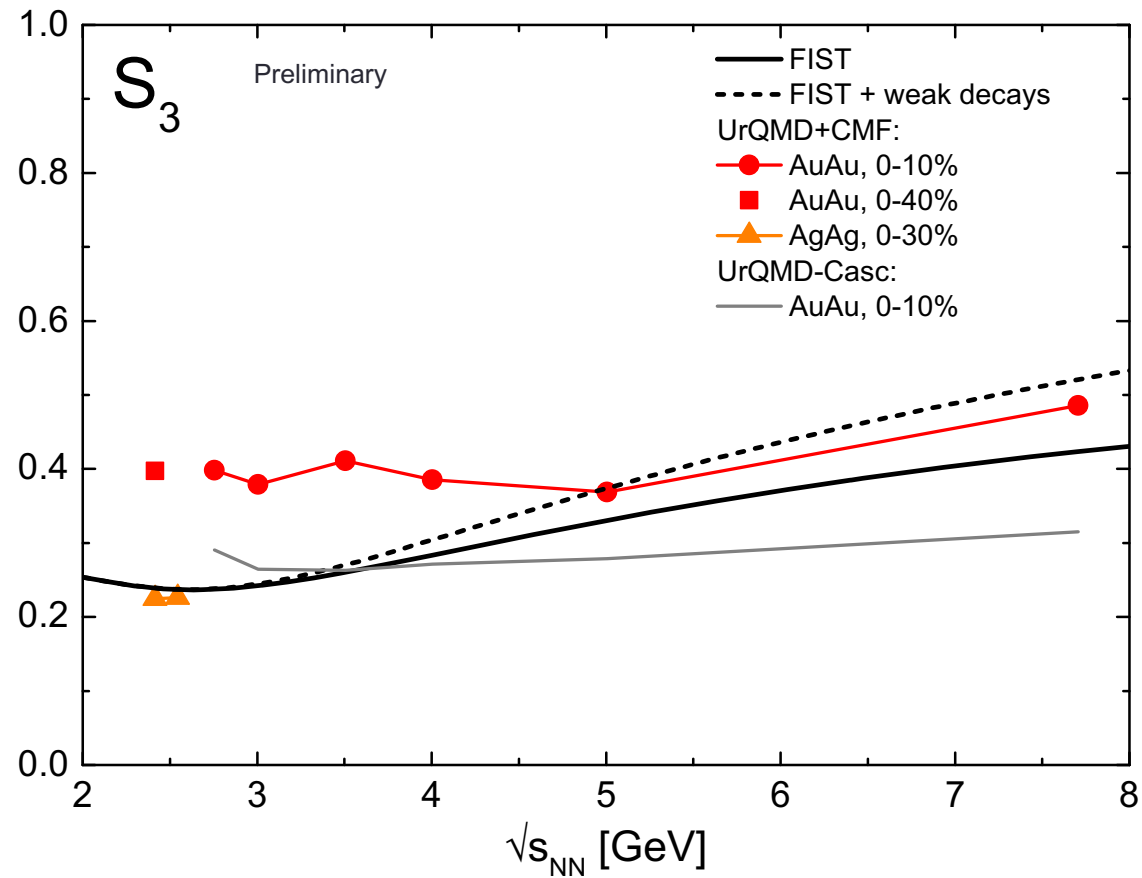
# Another special ratio $S_3$

- $S_3$  is thought to be sensitive to baryon-strangeness correlation
- Thermal model and coalescence show similar behavior
- Unfortunately, error bars are large and there is few data available
- Dependence on coalescence source size observed



# System size dependence at low energies

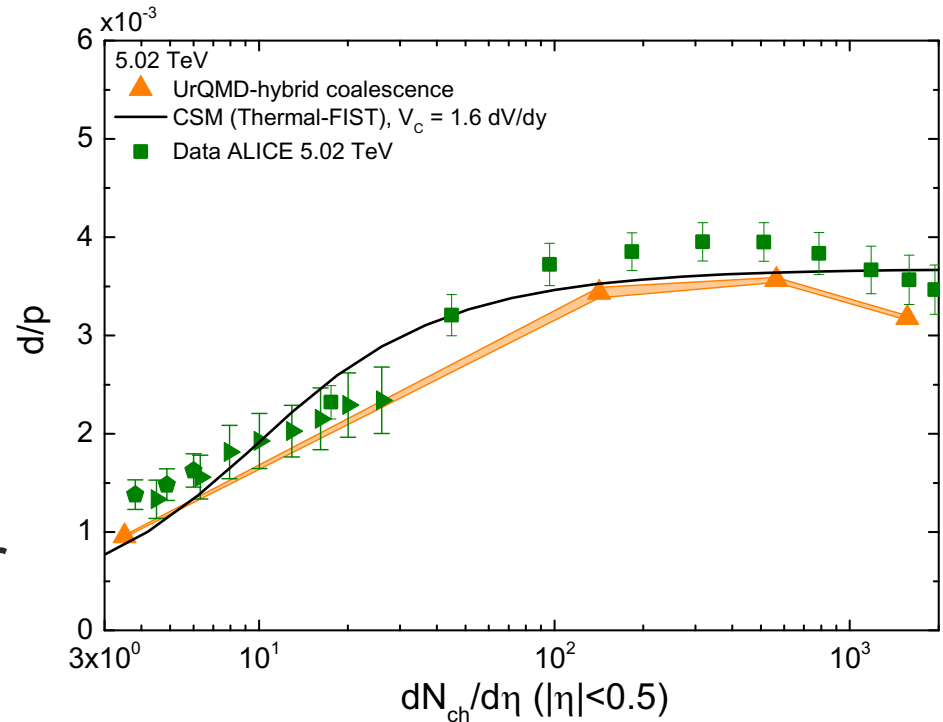
- HADES studied different systems at the same energy
- A comparative study of Ag+Ag versus Au+Au might reveal a system size dependence
- Suppression of  $S_3$  in smaller Ag+Ag system





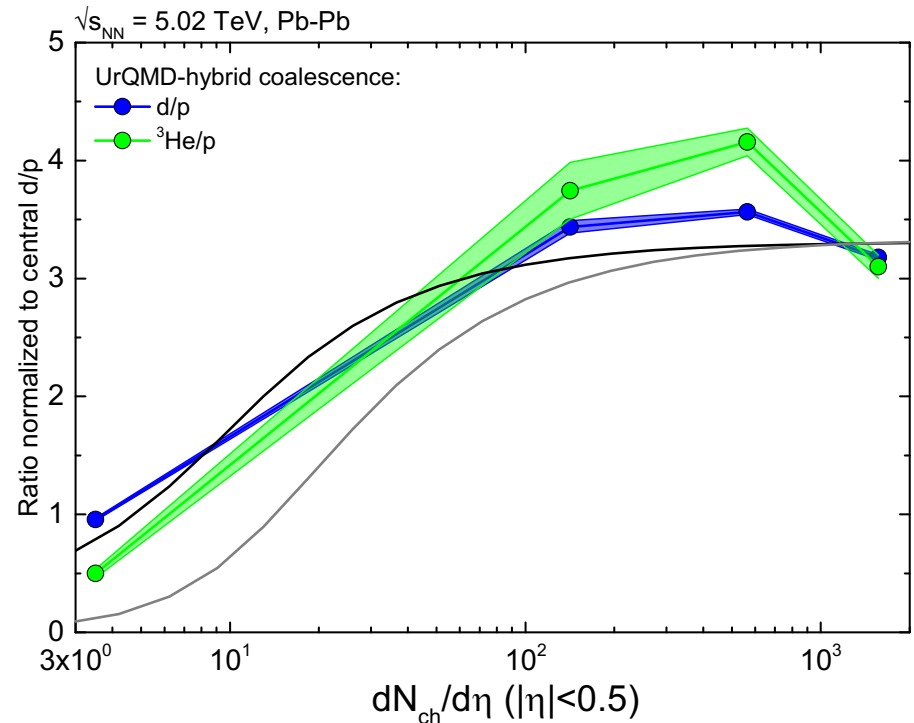
# Light nuclei to proton ratio $d/p$

- $d/p$  of UrQMD+coalescence and Thermal-FIST within exp. Uncertainties
- Centrality dependence well reproduced
- Small increase due to annihilation, then drop-off for small systems



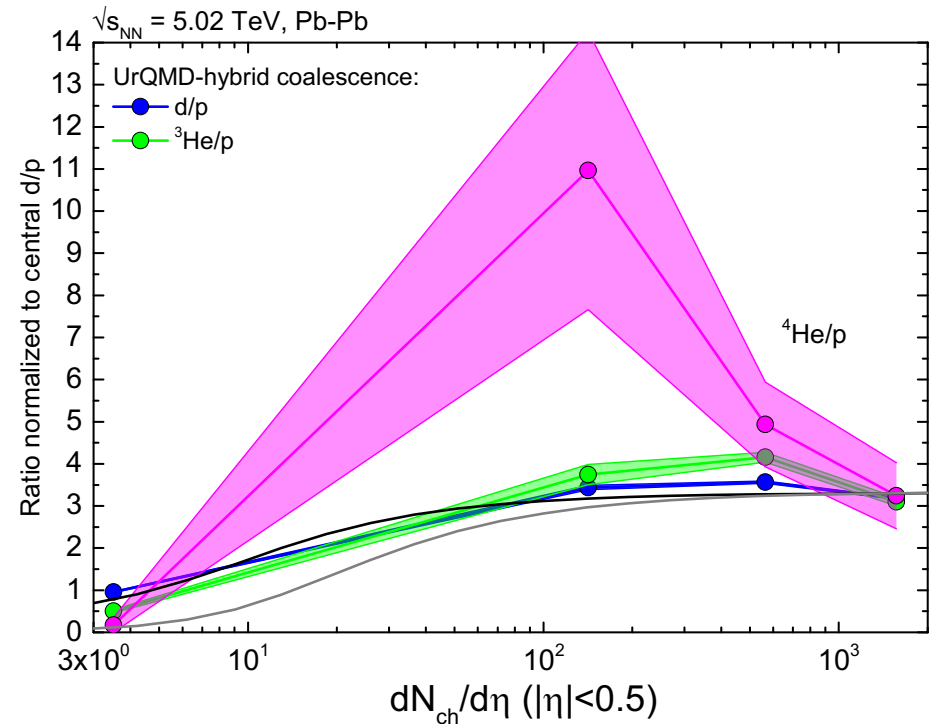
# Light nuclei to proton ratio ${}^3\text{He}/p$

- $d/p$  of UrQMD+coalescence and Thermal-FIST within exp. Uncertainties
- Centrality dependence well reproduced
- Small increase due to annihilation, then drop-off for small systems
- Same systematic observed for  ${}^3\text{He}/p$



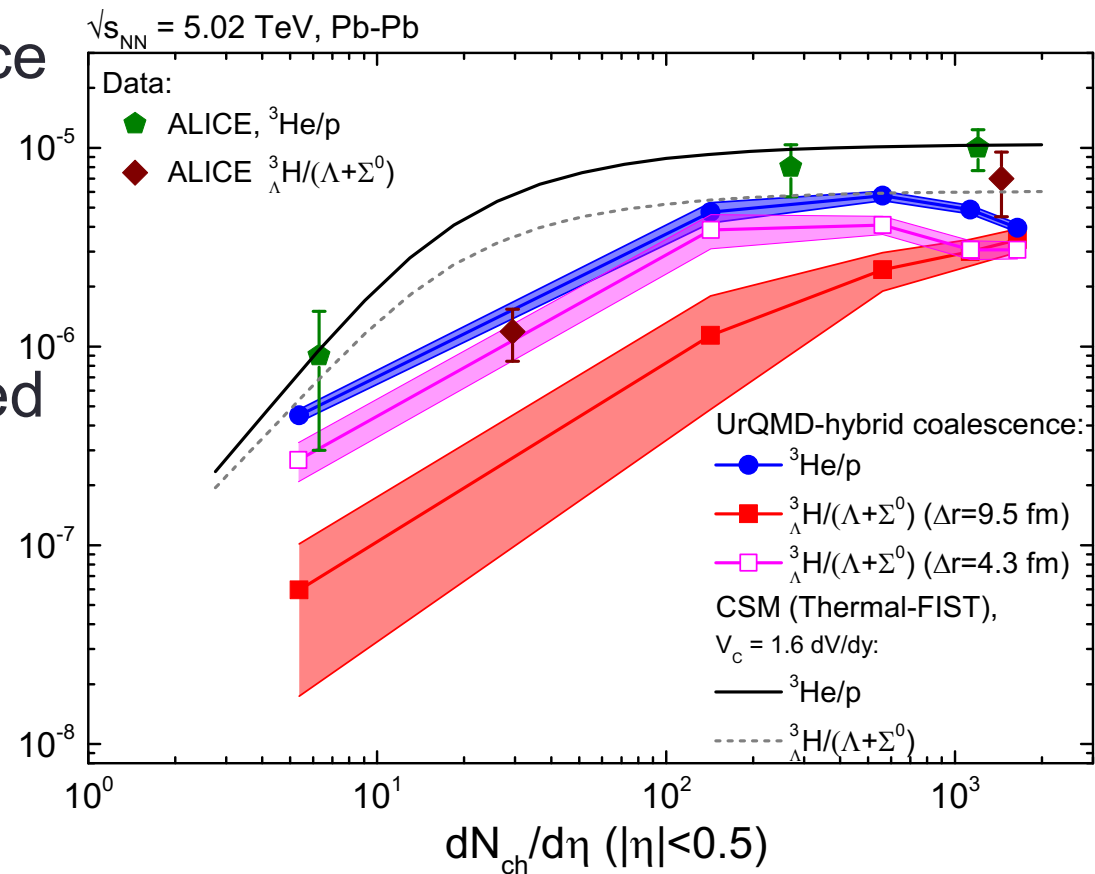
# Light nuclei to proton ratio ${}^4\text{He}/p$

- $d/p$  of UrQMD+coalescence and Thermal-FIST within exp. Uncertainties
- Centrality dependence well reproduced
- Small increase due to annihilation, then drop-off for small systems
- Same systematic observed for  ${}^3\text{He}/p$
- Huge effect seen in  ${}^4\text{He}/p$



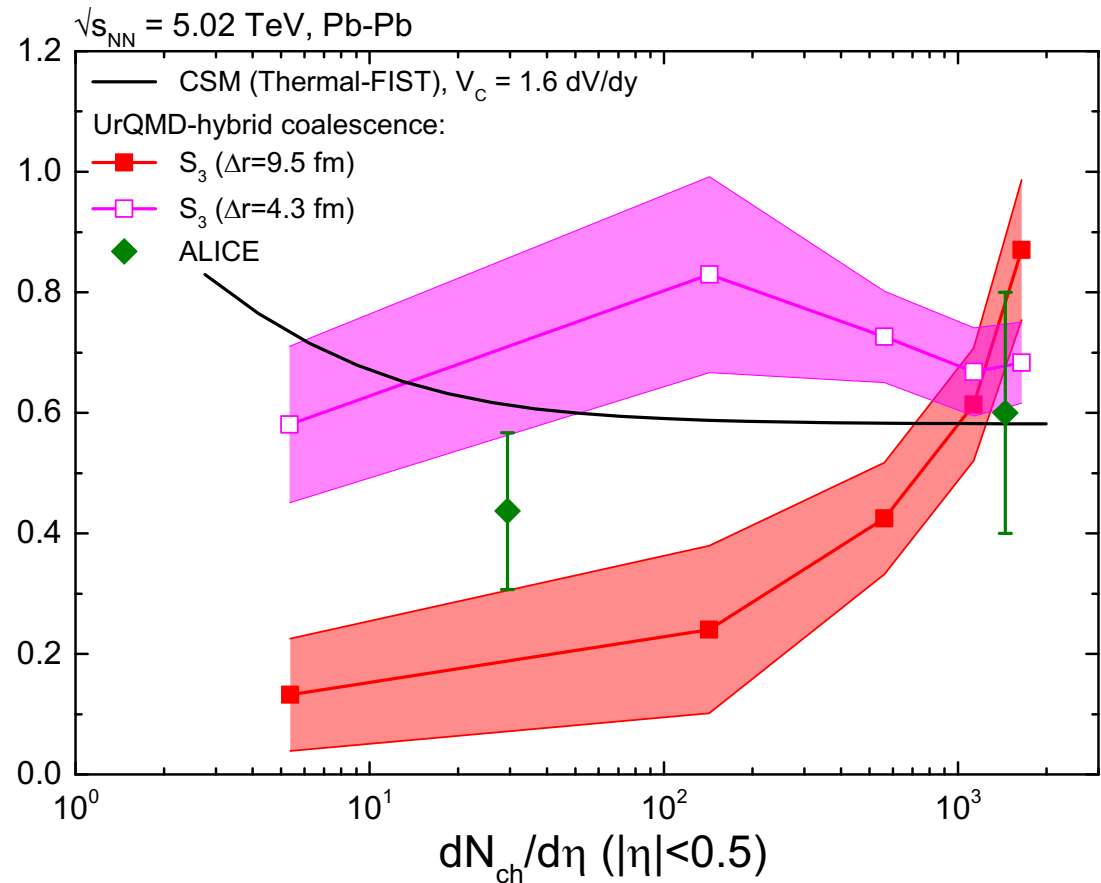
# Centrality dependence of hypernuclei

- We can change the source size  $\Delta r$  for the  ${}^3_{\Lambda}\text{H}$  to be the same as for  ${}^3\text{He}$
- $\Delta p$  thus has to be adjusted to give a similar value in central collisions
- Centrality dependence is changed as expected



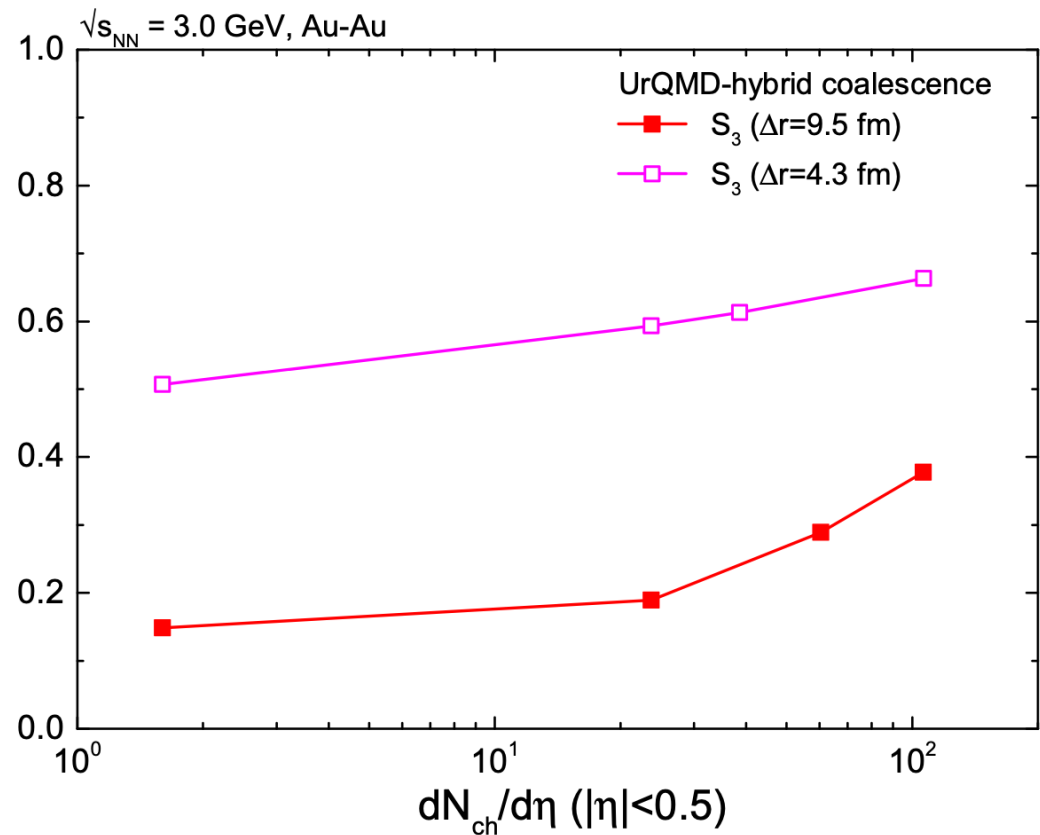
# Centrality dependence of $S_3$

- Similar behavior is observed for the double ratios
- Different source sizes give different behavior
- Note that in pp also canonical effects are naturally included
- Experimental situation is not yet conclusive



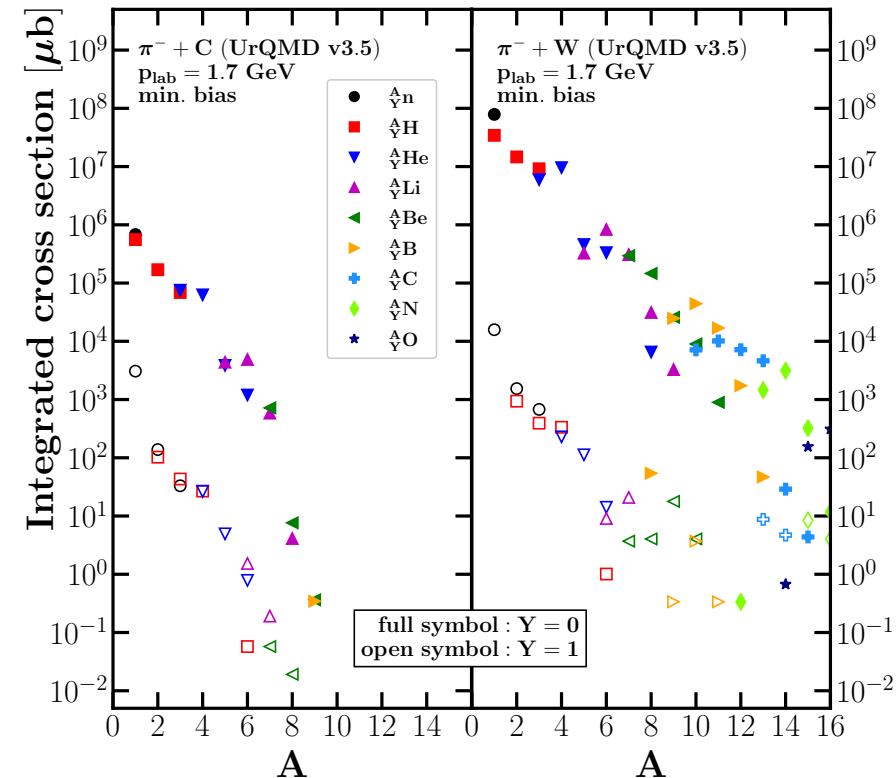
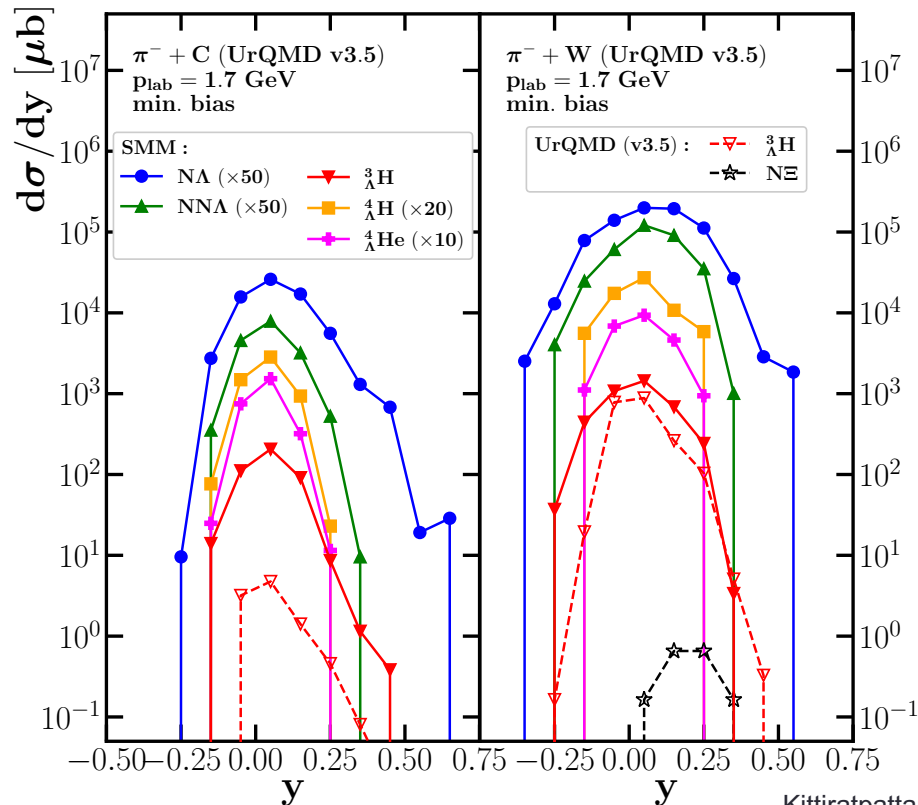
# Centrality dependence of $S_3$

- Dependence on source size also observed at 3 GeV
- Here  $\Delta r$  also affects  $S_3$  in central collisions
- Preliminary STAR data at 3 GeV:  
 $S_3 = 0.2 - 0.5$  at  $dN_{ch}/d\eta = 20 - 50$
- Not conclusive either



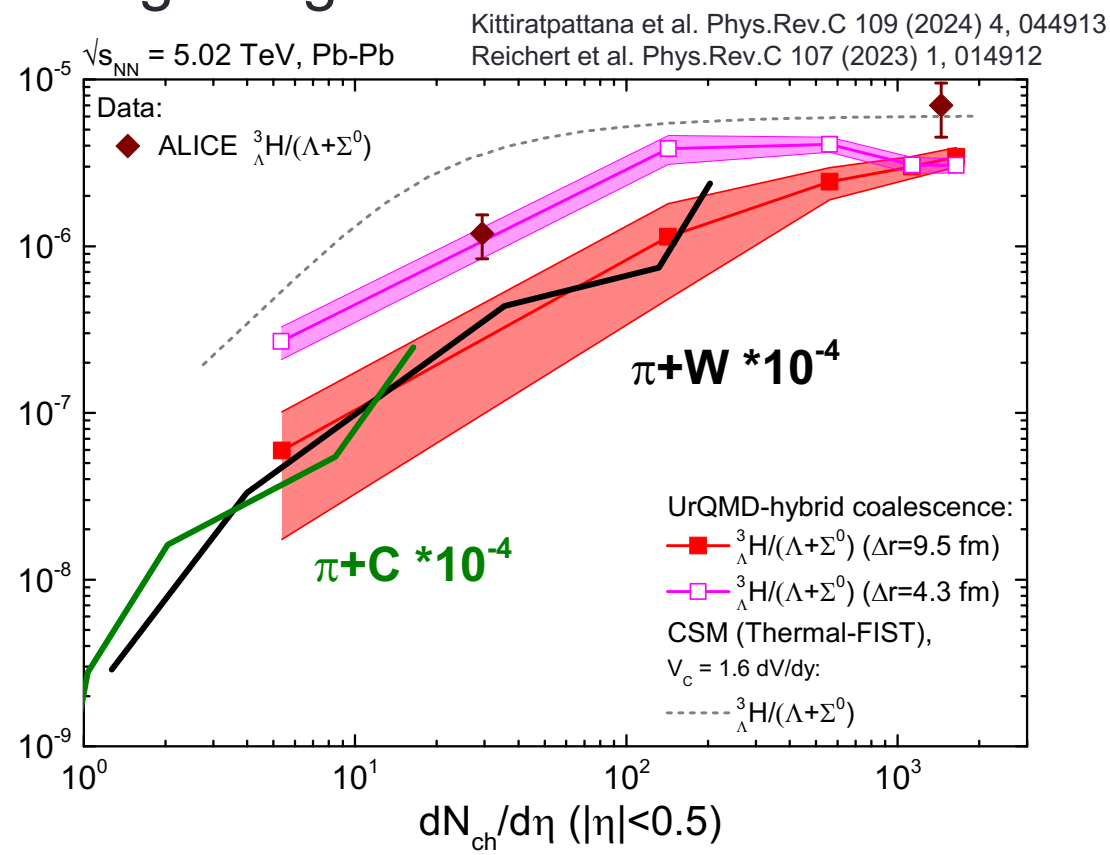
# Cluster production in pion induced reactions

- Using a pion beam allows to create hyperon within the target
- (Hyper-)nuclei formation through fragmentation



# System size dependence in pion induced reactions

- Using a pion beam allows to create hyperon within the target
- (Hyper-)nuclei formation through fragmentation
- Abundant (hyper-)nuclei yields even more large mass numbers
- One might event observe  $\Xi$ -hypernuclei
- Same system size dependence as ALICE data (scaled  $S_3$ )





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# Take-home messages

- Coalescence successfully describes the production of light- and hypernuclei in various systems and energies
- Isospin effects at high baryon densities are relevant
- Strong annihilation signal seen in  $^4\text{He}/p$  ratio at the LHC
- Strong fluctuations in coordinate space seen, signal in momentum space is rather weak
- System size dependence of hypertriton production can tell us about its source size, can be studied in various systems
- Pion beams pose a unique tool to study multi-hypernuclear objects



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