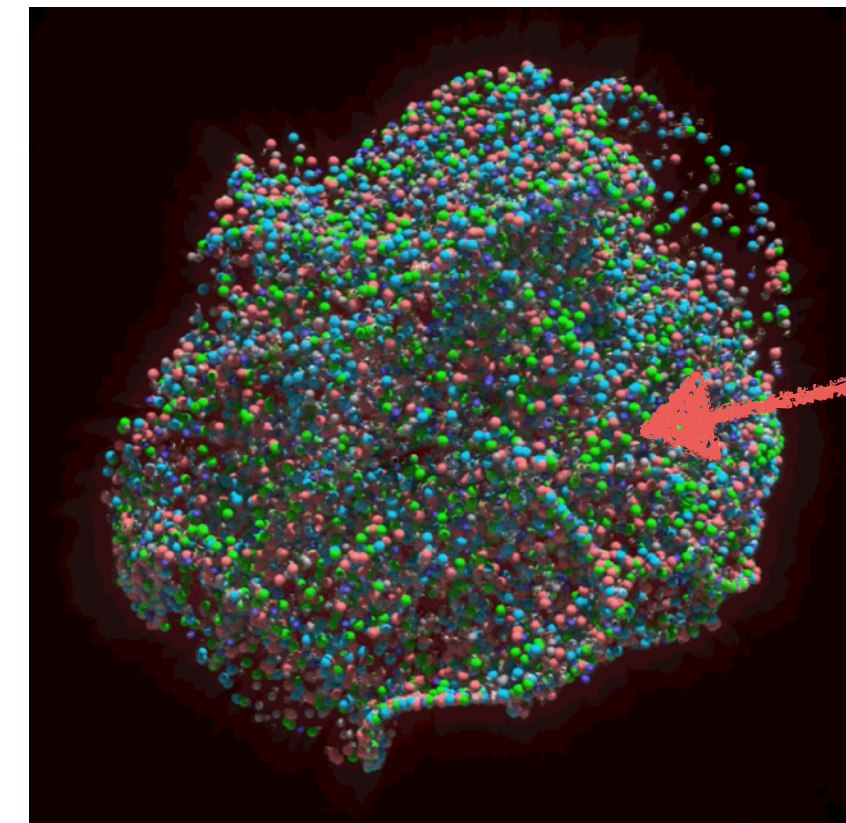
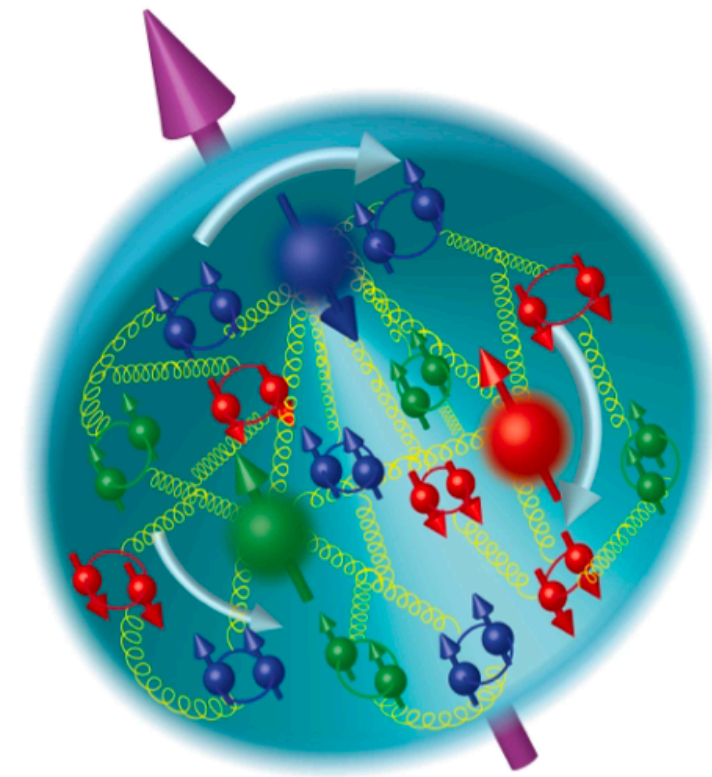


# Spin and QCD Phase Structure



*Temperature/density*

Yi Yin  i

*Institute of Modern Physics, CAS*

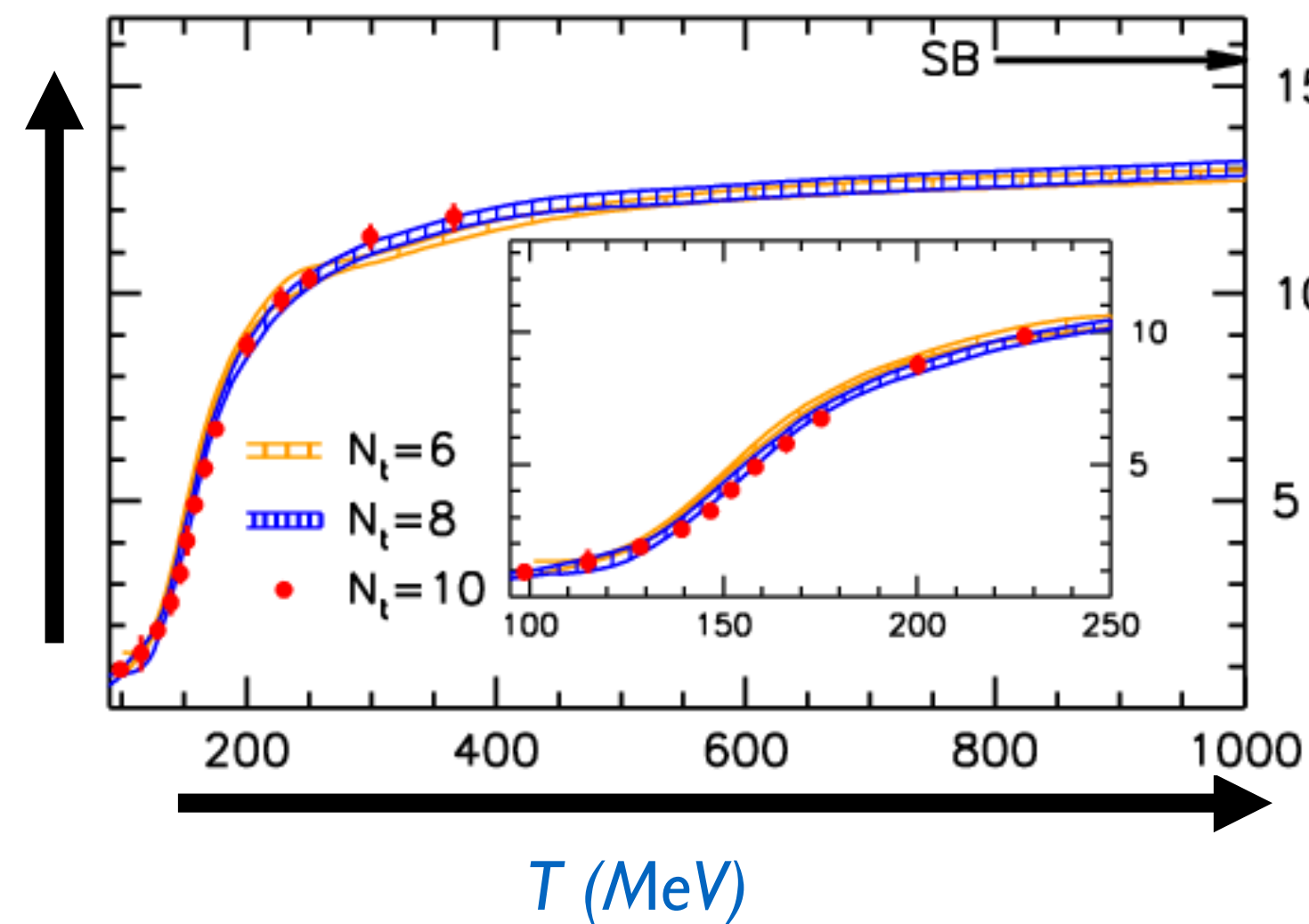
*CPOD2024, May. 23rd, 2024*

# Outline

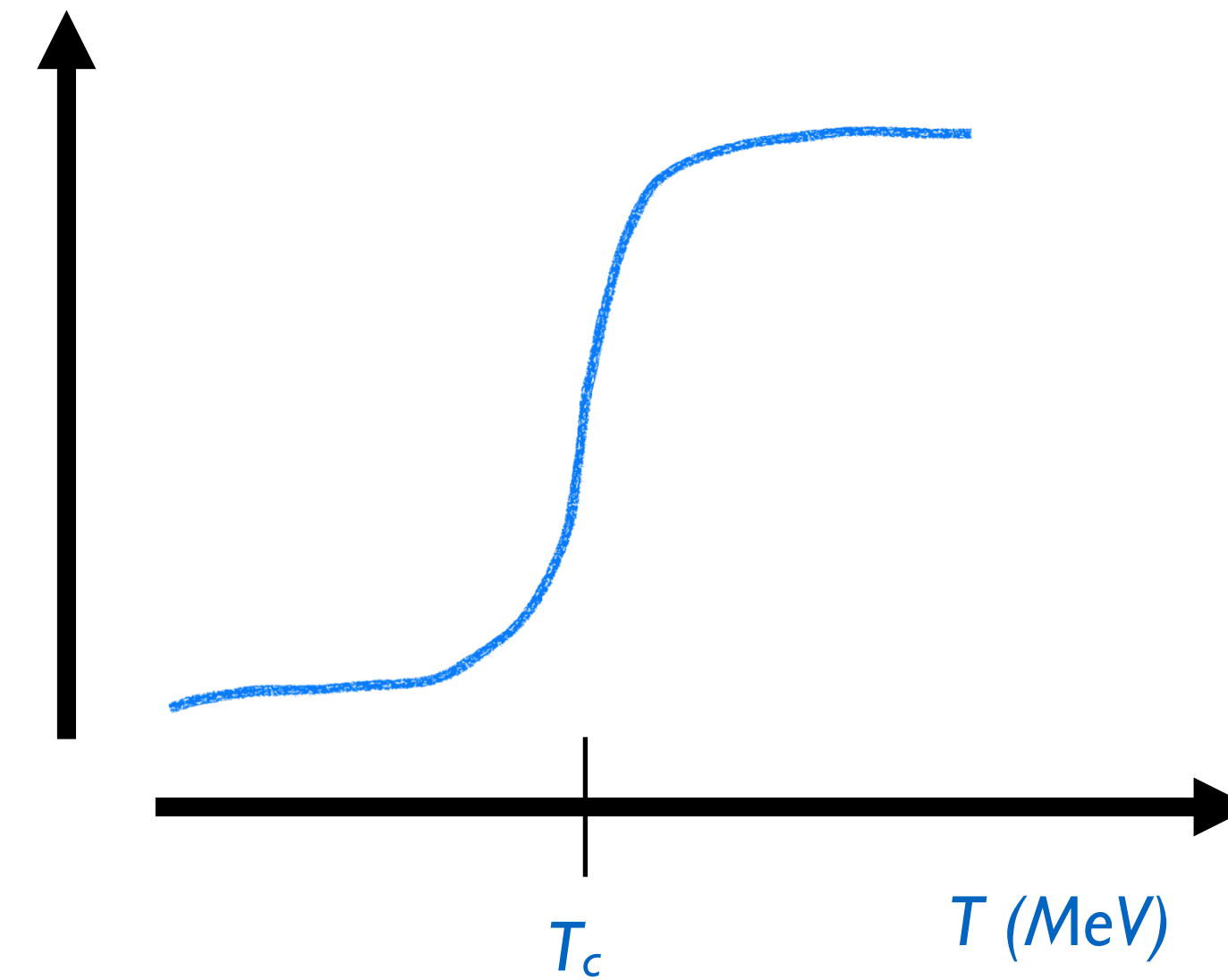
- Spin polarization generation: recent theoretical progress
- Phenomenological application
- Summary and outlook

# Spin and Phase Structure

$\varepsilon/T^4 \sim \# \text{ of Degree of freedom}$



# of spin carrier



(Budapest-Marseille-Wuppertal Collaboration, JHEP'10)

- Spin carriers change dramatically near transition temperature
- $\Lambda$  spin polarization/vector meson spin alignment measurement in heavy-ion collisions open a new frontier to study the properties of QCD matter

STAR Nature 2017, 2023

# Polarization Generation in HIC

- Vorticity/rotation effect describes the trends of momentum-averaged (global)  $\Lambda$  polarization; was considered as the main mechanism for generating polarization

$$\hat{s} \parallel \vec{\Omega}$$

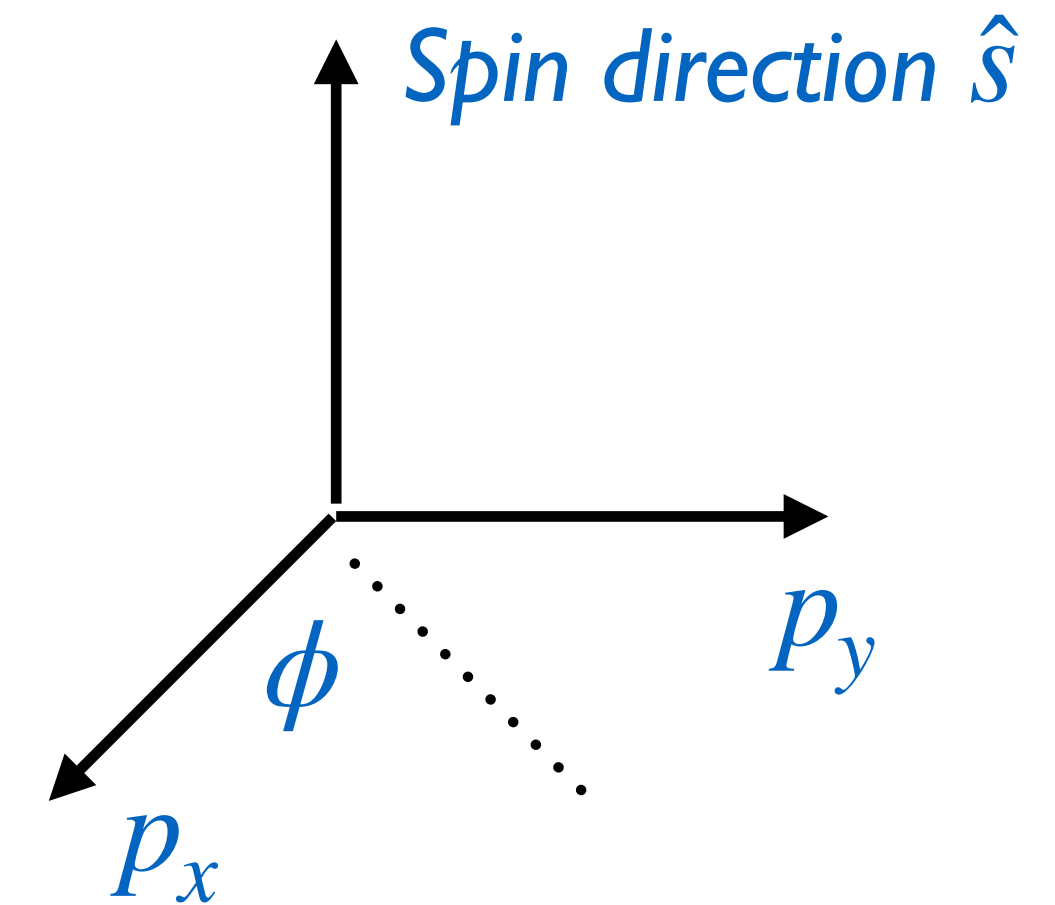
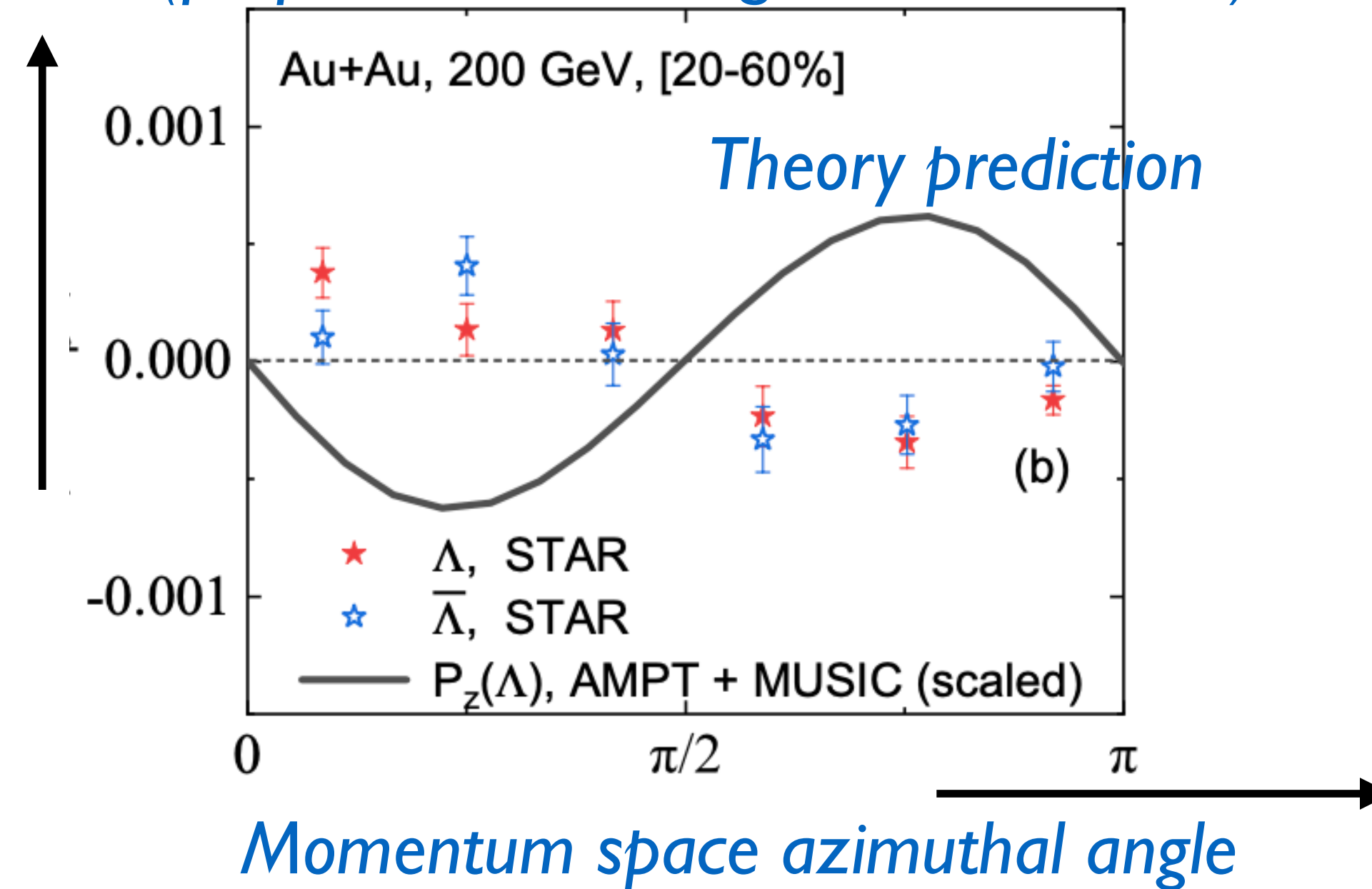
*Xin-Nian Wang, Zuo-Tang Liang, PRL 05';  
Becattini et al, Annals Phys 13'*

- Since 2021', significant progress revealing rich spin effects
- Is instructive to revisit spin “sign puzzle” for differential polarization

# Differential Spin Polarization

STAR Collaboration PRL 19

Spin along beam direction (perpendicular to angular momentum)

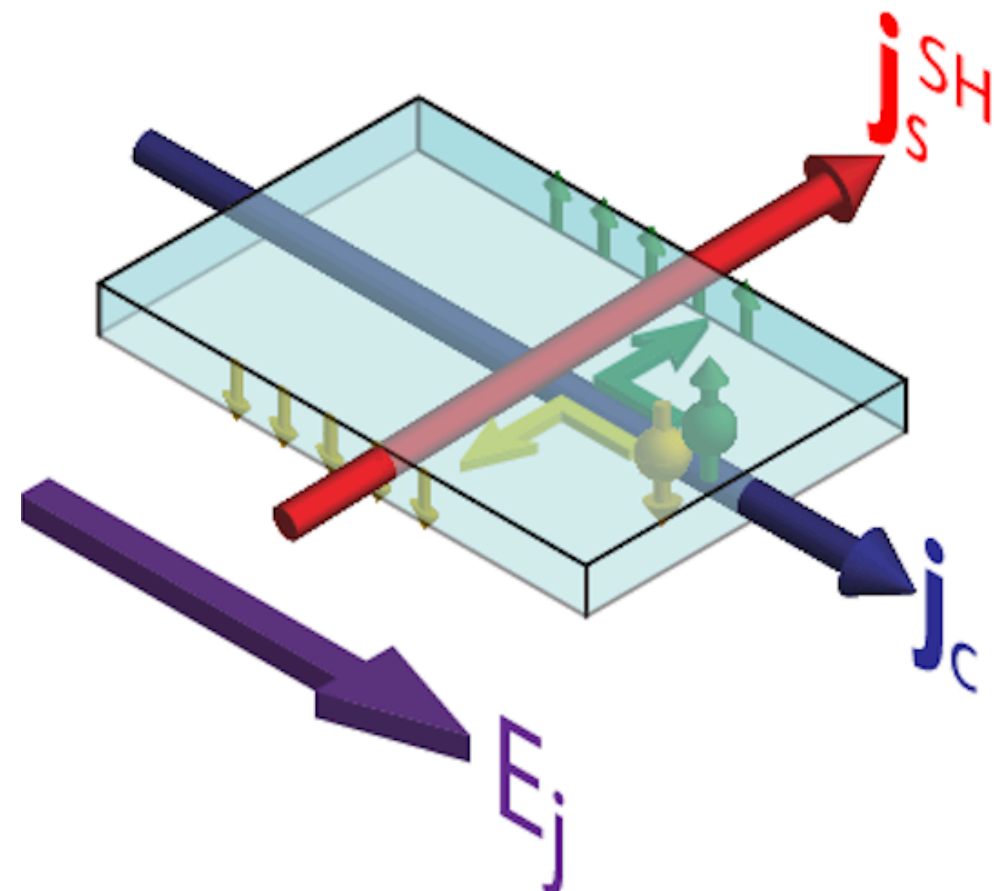


- Data indicates non-trivial **spin-motion correlation**, yet its origin is puzzling

A class of models based on vorticity effect predict **qualitatively different** behavior (“sign puzzle”)

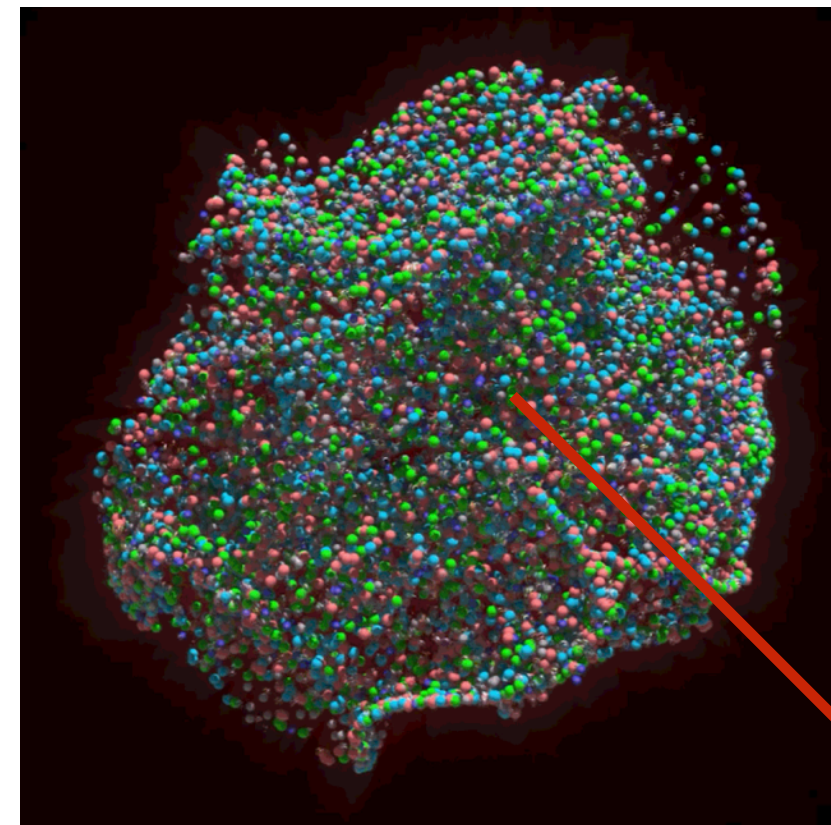


# Spin Hall Effect



*Meyer et al, Nature material 17*

$$\hat{s} \propto \vec{v} \times \vec{E}$$



$$\hat{s} \propto \vec{v} \times \vec{\partial}$$

*Direction of gradient*

- Electric force generates spin-motion correlation
- The **gradient of density** (e.g. momentum, energy/charge density) in QGP acts as generalized force that polarizes spin; can be analyzed systematically by extending usual gradient expansion to spin observables

# Uncovering New Effects

Shuai Liu-YY JHEP 21  
Also Becattini et al, PLB 21

Spin in phase space

$$s^i(t, \vec{x}, \vec{v}) = c_\omega \omega^i + c_T \epsilon^{ijk} v_j \partial_k T + c_\sigma \epsilon^{ikj} \hat{v}_j \hat{v}_l \sigma_k^l$$

Vorticity effect
T-gradient
Shear-induced polarization

$$\vec{\omega} = \nabla \times \vec{u}$$

$$\sigma_{ij} = (\partial_i u_j + \partial_j u_i)$$

- **Shear-induced polarization (SIP)**: allowed by symmetry, was never considered before
- One-loop calculation and quantum kinetic theory confirm the existence of SIP:  $c_\omega \sim c_\sigma \propto$  density of spin carriers
- **Baryon density gradient also polarizes spin**

Shuai Liu and YY, PRD 20; Fu et al, 2022

$$\vec{s} \propto \vec{v} \times \vec{\partial} \mu_B$$

# An Emerging New Field

- Rapid progress in relativistic quantum kinetic theory, spin hydrodynamics

*Works by many*

- **Dissipative or not:** shear effect is typically dissipative but spin is inherently quantum.

Shear-induced polarization exemplifies a new class of emergent phenomena that the system is off-equilibrium, yet the transport is non-dissipative

*Becattini and YY, in preparation.*

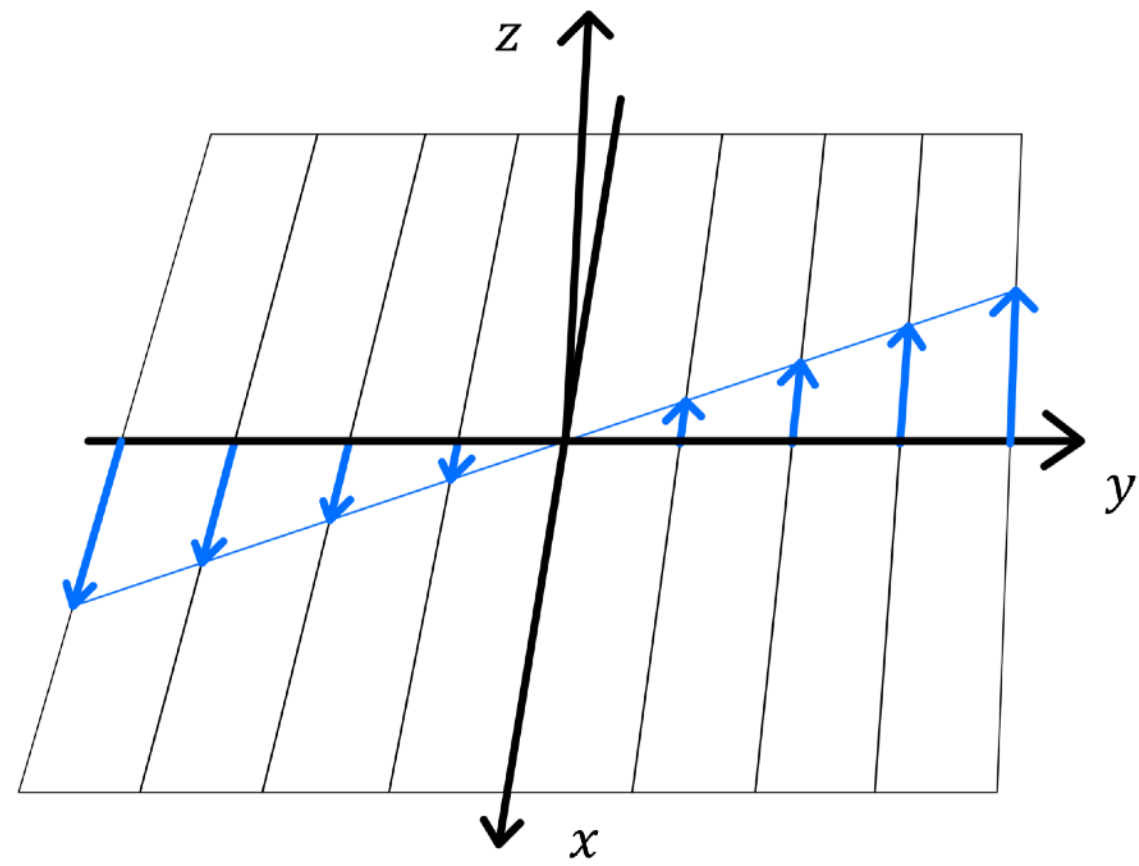


# Phenomenological Implications

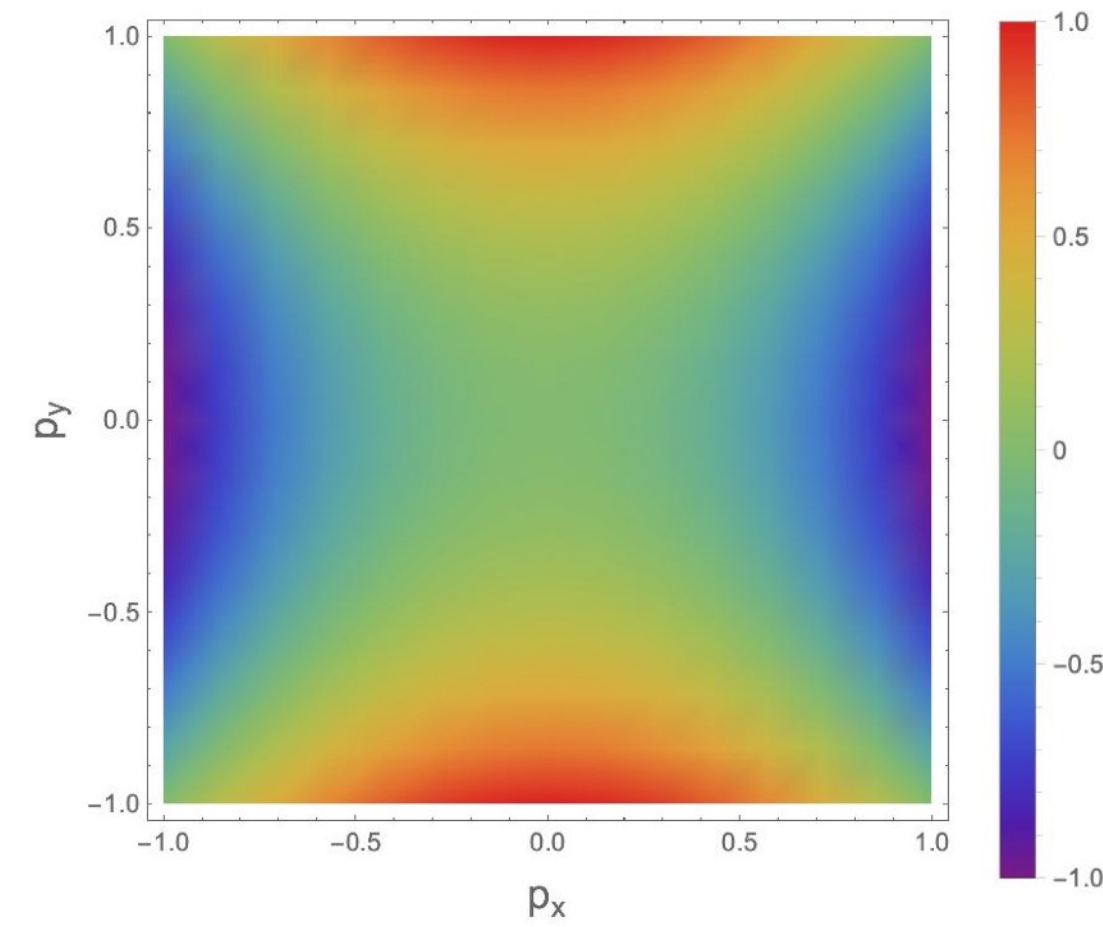
Particle distribution:  $\epsilon, u^\mu$  + gradient corrections

Polarization distribution  $\propto$  gradient; sensitive to initial condition, transport coefficients, etc

# How Shear Induces Polarization



$$s^i \propto \epsilon^{ikj} \hat{v}_j \hat{v}_l \sigma^l_k$$

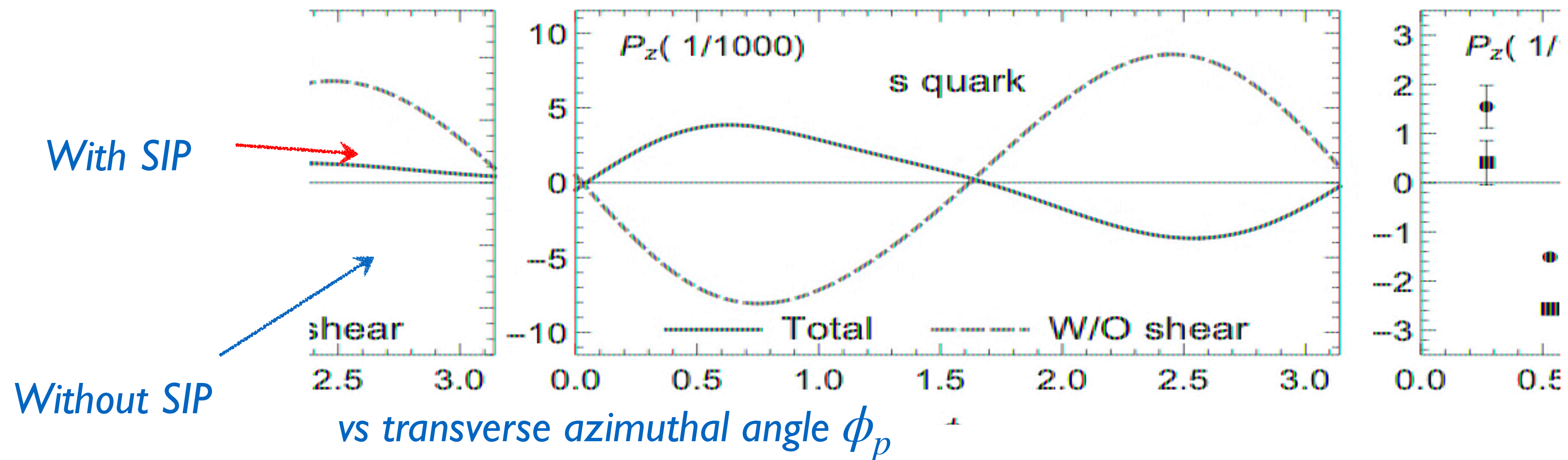


A standard shear flow profile:  
 $\omega^z \neq 0, \sigma^{xy} \neq 0$

Distribution of  $s^z$  in  $v_x - v_y$  plane  
 due to SLP; vorticity does not induce  
 any momentum distribution

# Differential Polarization and SIP

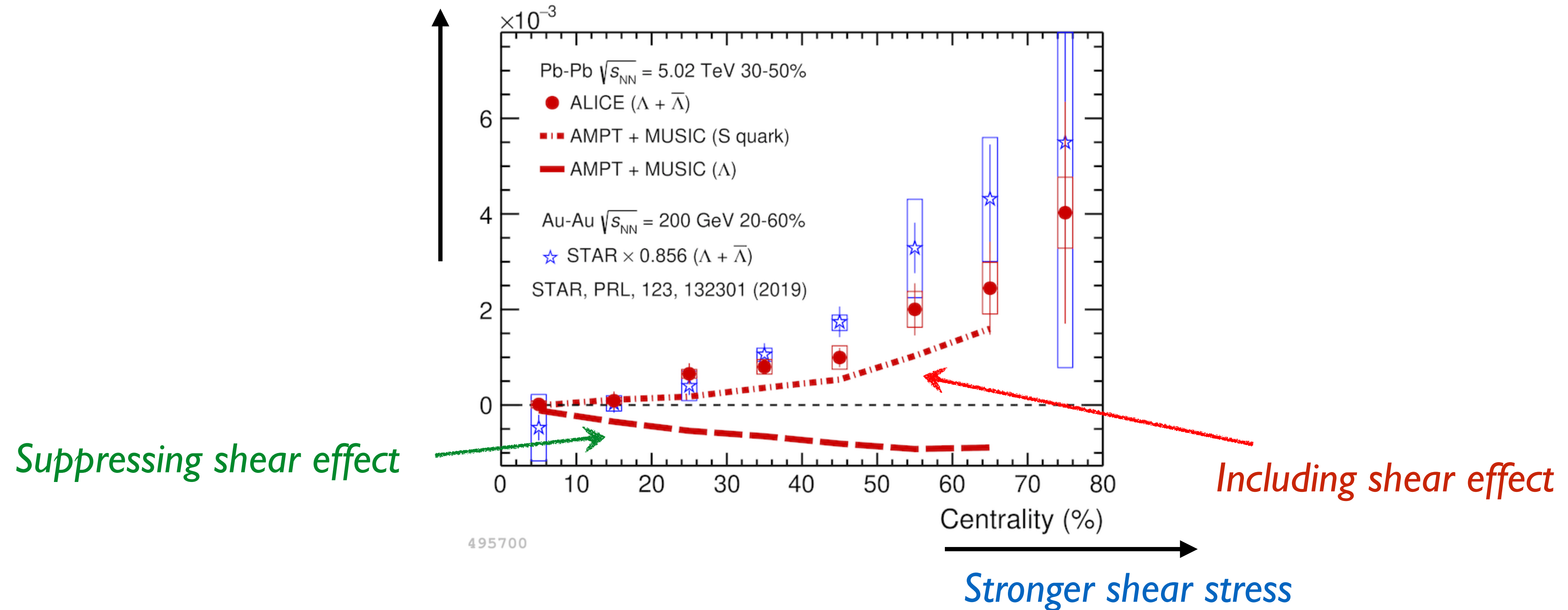
Baochi Fu, Shuai Liu, Longgang Pang, Huichao Song, YY, PRL 21  
 also confirmed in Becattini et al PRL 21



- Shear-induced polarization (SIP) contribution qualitatively agrees with the data

## Coefficient of $\sin(2\phi)$ modulation

LHC results from ALICE collaboration PRL 22



- **Tantalizing evidence for SIP:** data can no be understood without including shear effects. More efforts are needed to claim discovery

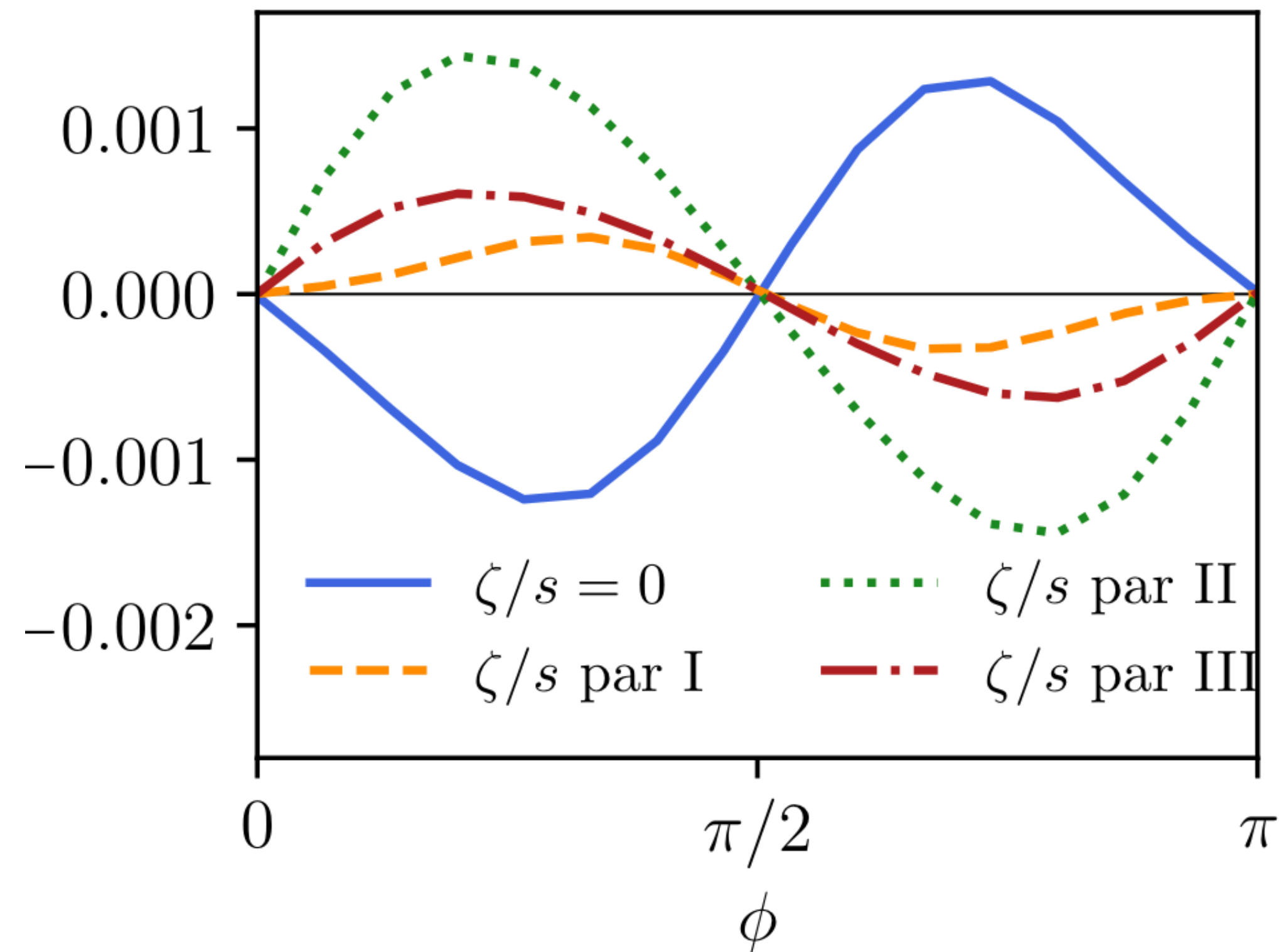
Shear effects on other spin observables: STAR PRL 23

# Sensitivity to Transport Coefficient

Longitudinal polarization

LHC PbPb 5020 GeV

Palermo et al., arXiv: 2404.14295

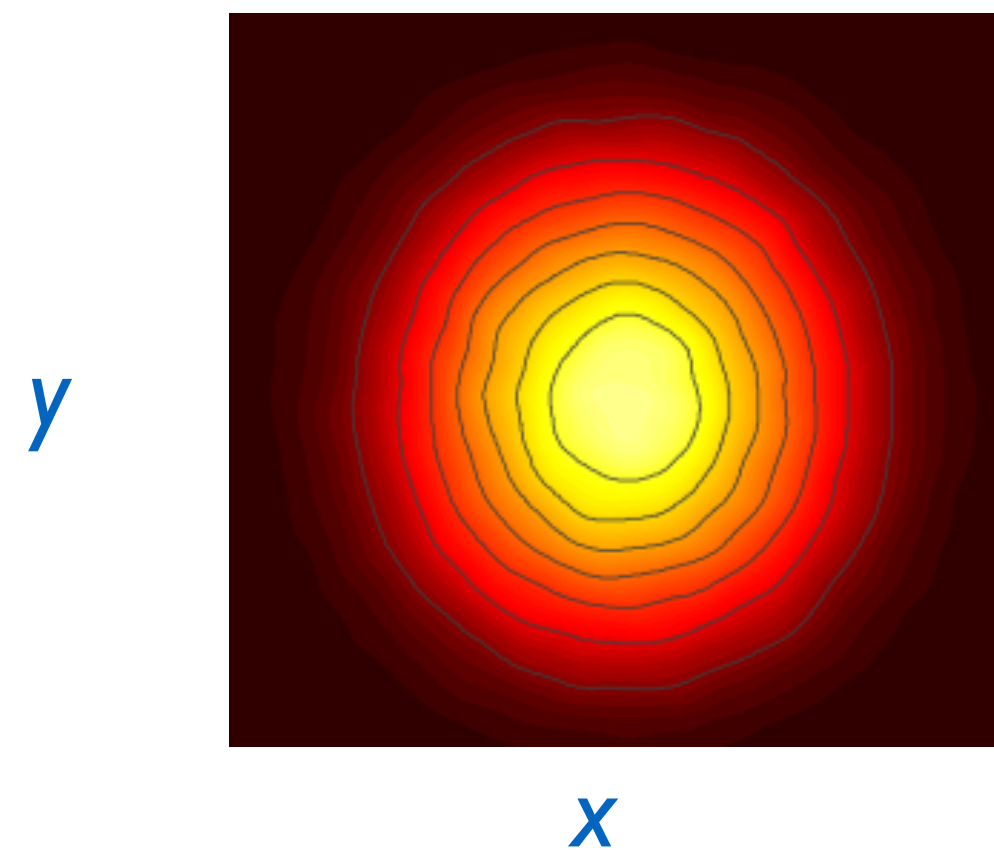


- Extension to BESII data can help constraining transport properties of Baryon-rich QGP



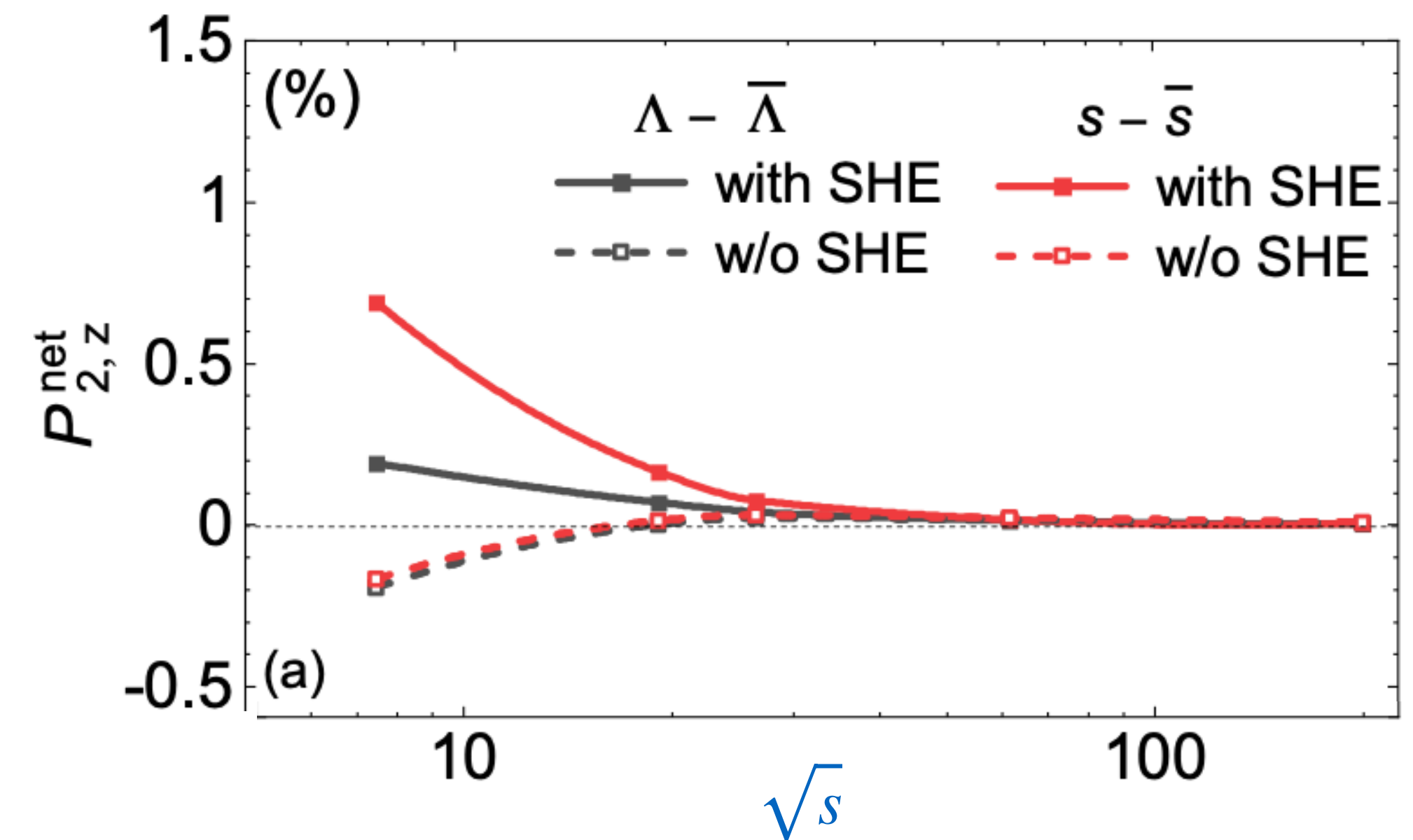
# Baryonic Spin Hall Effect

Baochi Fu, Longgang Pang,  
Huichao Song, YY, 2201.12970



$$\vec{s} \propto \vec{v} \times \vec{\partial} \mu_B$$

Coefficient of  $\sin(2\phi)$  modulation:  $\Lambda - \bar{\Lambda}$



Initial  $n_B$  profile at  $\sqrt{s} = 7.7$  GeV  
from AMPT

- Sensitive to EoS, diffusive constant and initial baryon stopping

A similarly effect induces neutrino current in supernovae

Di-Lun Yang, Naoki Yamamoto PRD 24

# Vector Meson Spin Alignment

- measures the difference between the occupation of transverse and longitudinal spin states

$$\delta\rho_{00} = \rho_{00}(\hat{n}) - \frac{1}{3} \propto \text{long. mode density} - \text{trans. mode density}$$

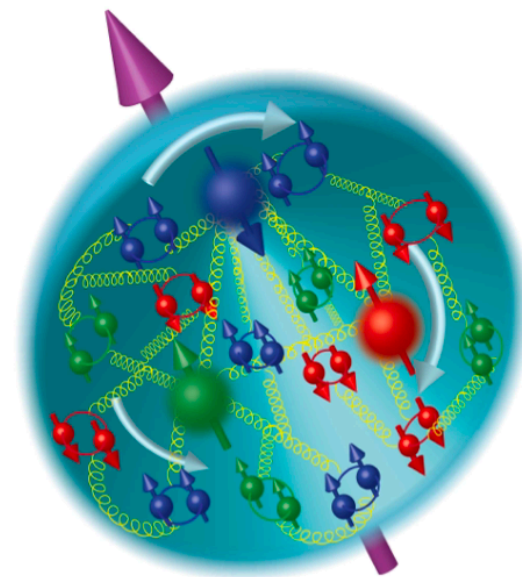
- shows non-trivial dependence on the species of mesons, centrality and  $\sqrt{s}$  in both sign and magnitude; the underlying mechanism is under debate

*e.g. Xin-Li Shen et al, PRL 23*

- can be used to constrain in-medium properties of vector mesons

$$\delta\rho_{00}^{(0)} \propto E_L(p) - E_T(p)$$

# Outlook: QCD Spin Structure



$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma + \Delta G + L$$

*Xiangdong Ji et al, Nature Review, 20*

*orbital ang. momen.*

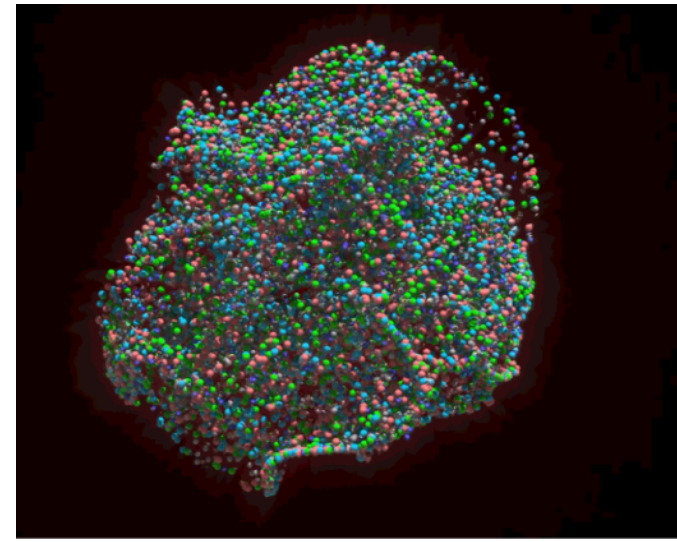
*quark spin (only  $\approx 20\%$ )*

*gluon spin (up to  $50\%$ )*

- Is the complex spin structure specific to confinement? Or a generic feature of non-perturbative quark-gluon interaction?
- Need to examine deconfined but strongly-coupled quark matter

# Spin Structure of Quark Matter

Total angular momentum  
 $\hat{J} \neq 0$



$$J = \frac{1}{2} \Delta \Sigma + \Delta G + L$$

*gluon spin? orbital ang. mom.?*

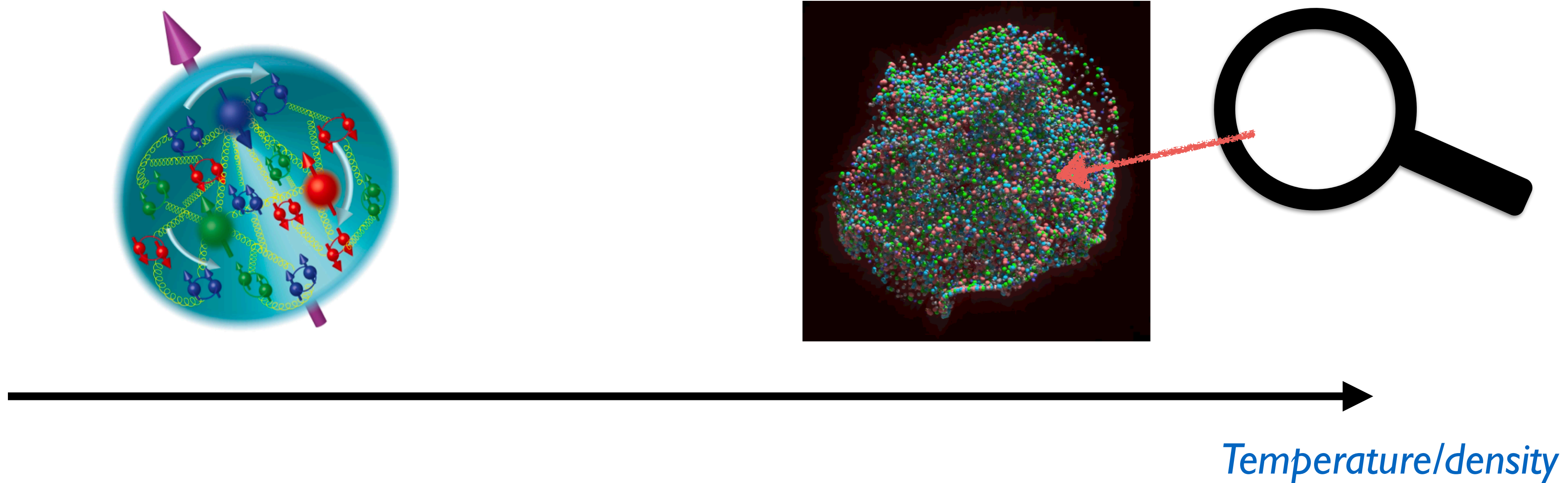
- Consider rotating hot/dense quark matter

Quark spin:  $\frac{1}{2} \frac{\Delta \Sigma}{\Omega} = \frac{1}{12} T^2 + c_0 g^2$  *Two-loop, De-fu Hou et al 2013*  $\frac{\Delta G, L}{\Omega} = ?$   
*Related to Chiral Vortical Effect coefficients*

Analyzing and comparing spin structure will deepen the understanding of confinement/deconfinement transition



# Summary



- Recent theoretical progress allows for utilizing spin observables to constraint the properties of QGP at different energies
- Outlook: spin structure monitors QCD phase transition



# Back-up

# Spin, Quantum Matter and QCD

- Broad context: spin effects reveal quantum behavior of many-body systems
- QCD employs a sophisticated way to build up proton spin
- $\Lambda$  spin polarization/vector meson spin alignment measurement in heavy-ion collisions open a **new frontier to study the properties of QCD matter**

*STAR Nature 2017, 2023*

(Modern view: quantum effects are important in characterizing and understanding phases)

# Spin Dynamics

- Baryon density gradient also polarizes spin; the experimental investigation is under way *Shuai Liu and YY, PRD 20; Fu et al, 2022*

A similarly effect induces neutrino current in supernovea *Di-Lun Yang, Naoki Yamamoto PRD 24*

- Rapid progress in relativistic quantum kinetic theory, spin hydrodynamics

*Works by many, e.g. Jianhua Gao, Xu-Guang Huang, Koichi Hattori, Defu Hou, Shu Lin, Shi Pu, Qun Wang, Pengfei Zhuang, Shuzhe Shi*

- **Dissipative or not:** shear effect is typically dissipative but spin is inherently quantum. Calling for a deeper understanding *Becattini and YY, in progress.*

# Gradient Expansion

- Observables are expressible in terms of conserved densities, e.g., energy and momentum density (or flow velocity  $u^\mu$ ) for slow varying gradient  $\partial \sim k$ ,  $kl_{\text{mfp}} \ll 1$  In a collision,  $kl_{\text{mfp}} \sim 0.1$

$$O = (\partial^0) + (\partial^1) + \dots$$

- All possible terms allowed by symmetry should be included with expansion coefficients computed from microscopic calculations

Reminiscent of effective field theory

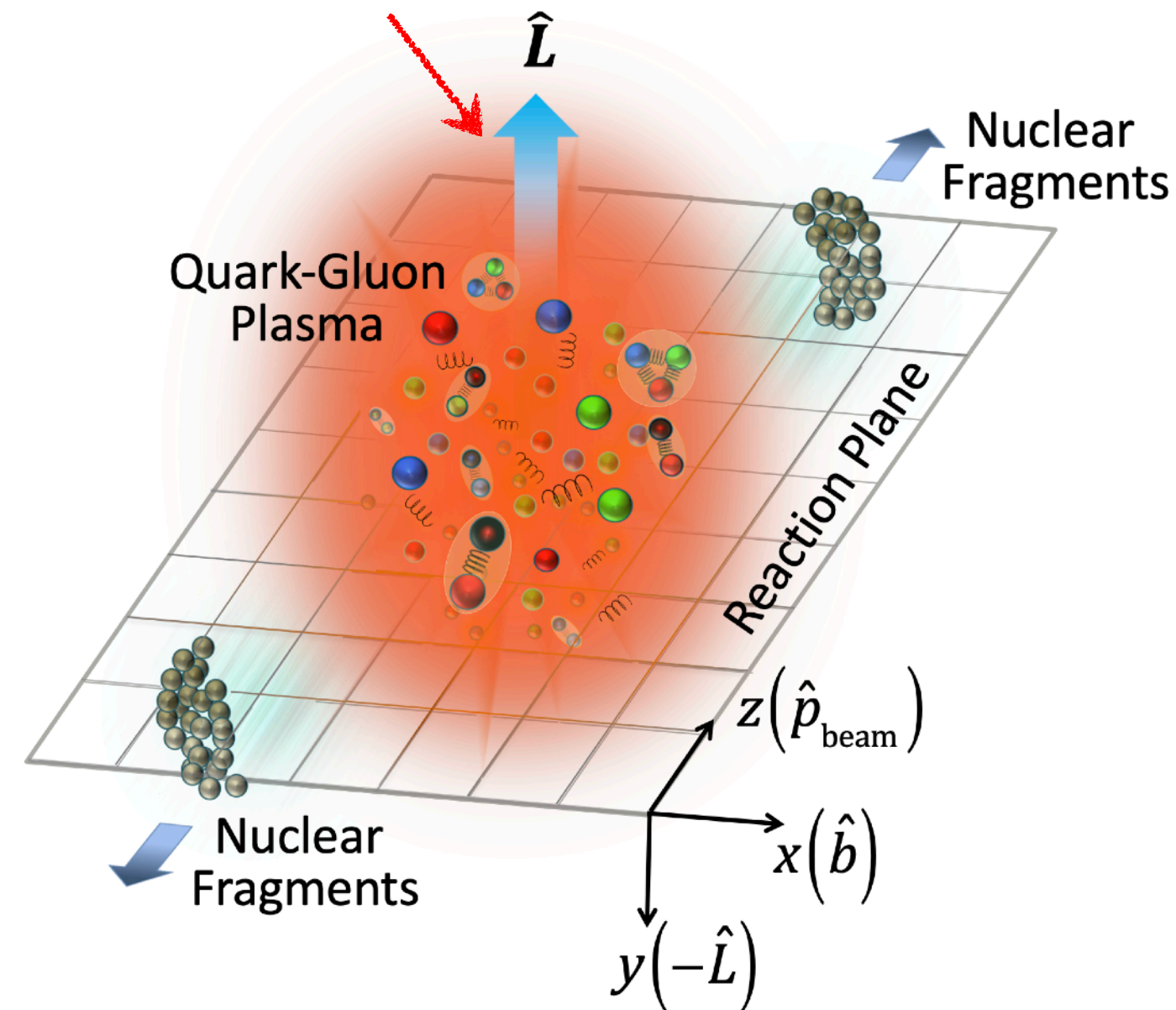
Constitutive relation in hydro:  $T^{ij} = p \delta^{ij} + \eta \sigma^{ij} + \dots$   
← shear stress

- Applying the same method to **spin observables**

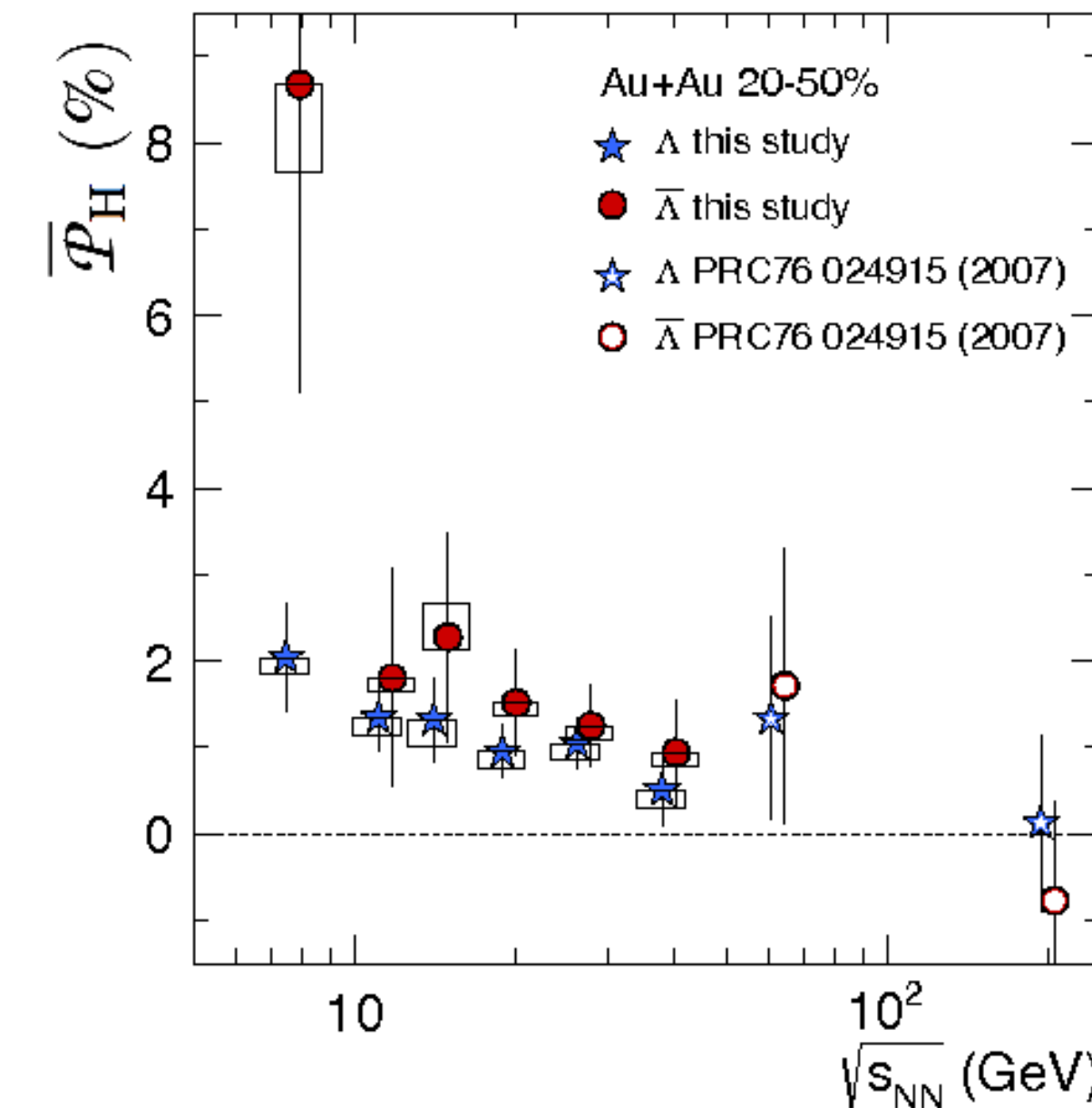
# $\Lambda$ Hyperon Polarization at RHIC

STAR Collaboration Nature 17

Direction of angular momentum



Rotating quark matter



$\Lambda$  polarization (momentum-averaged) along the direction of angular momentum vs collision energy

Vorticity effect describes the trends of momentum-averaged  $\Lambda$  polarization (spin parallels to angular velocity)