

Recent experimental results on 2nd order conserved charge fluctuations

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Yale University

CPOD 2024 - 15th Workshop on Critical Point and Onset of Deconfinement
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Yale



Wright
Laboratory

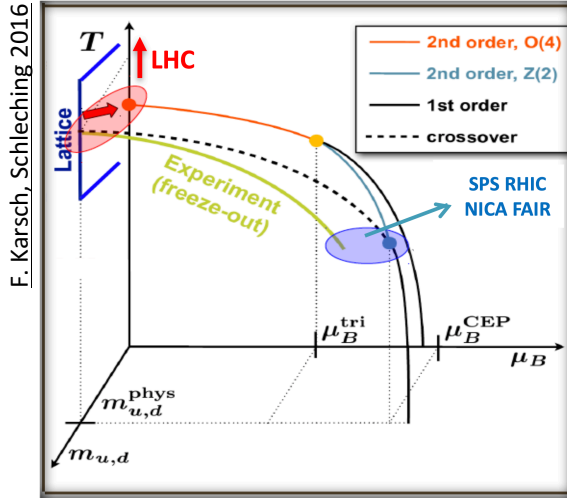


In part supported by

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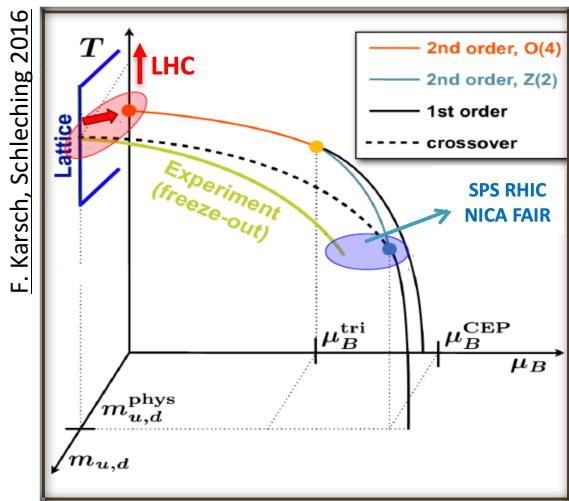
Office of
Science

Nature of QCD phase diagram



- **Pseudocritical features** at the crossover due to massless modes
- Long range correlations & **increased fluctuations**
- **Non-monotonic energy dependence**
- ...

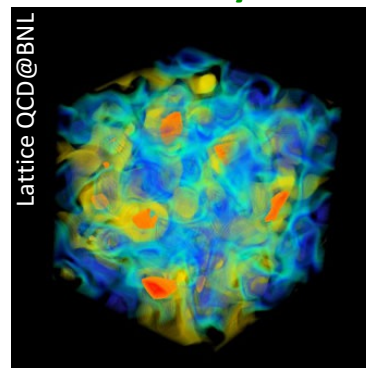
Nature of QCD phase diagram



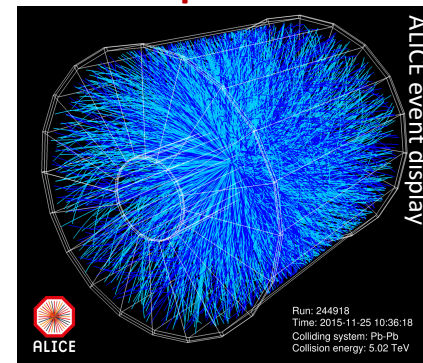
- **Pseudocritical features** at the crossover due to massless modes
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- **Non-monotonic energy dependence**
- ...

Bridge experimental data to LQCD calculations

Theory



Experiment



Static

Coordinate space

Net-baryon

Fixed V

...

Dynamic

Momentum space

Net-proton

Fluctuating V

...

LQCD ↔ Experiment

Google Translate

Detect language English German Spanish **LQCD**

$$\chi_{klmn}^{BQSC} = \frac{\partial^{(k+l+m+n)} [P(\hat{\mu}_B, \hat{\mu}_Q, \hat{\mu}_S, \hat{\mu}_C) / T^4]}{\partial \hat{\mu}_B^k \partial \hat{\mu}_Q^l \partial \hat{\mu}_S^m \partial \hat{\mu}_C^n} \Big|_{\vec{\mu}=0}$$

Baryon number (**B**), Strangeness (**S**), Electric charge (**Q**), Charm (**C**) 0 / 5,000

↔ **EXPERIMENT** Spanish ▾

Translation

$$\chi_2^B = \frac{\kappa_2(\Delta N_B)}{VT^3} \rightarrow \frac{\kappa_4(\Delta N_B)}{\kappa_2(\Delta N_B)} = \frac{\chi_4^B}{\chi_2^B}$$

$\kappa_n \rightarrow$ cumulants of $\Delta N_B = N_B - N_{\bar{B}}$

LQCD ↔ Experiment

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LQCD



EXPERIMENT

Spanish



Translation

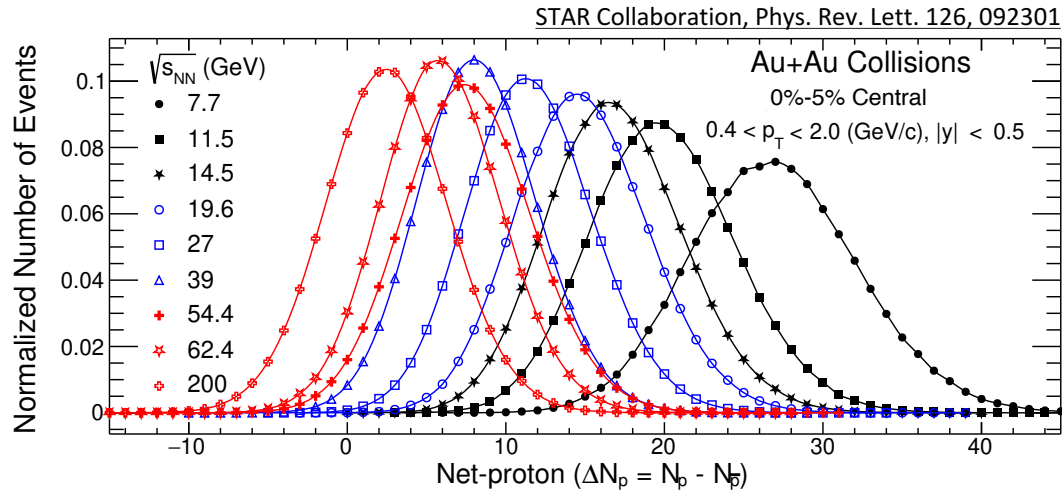
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Translation

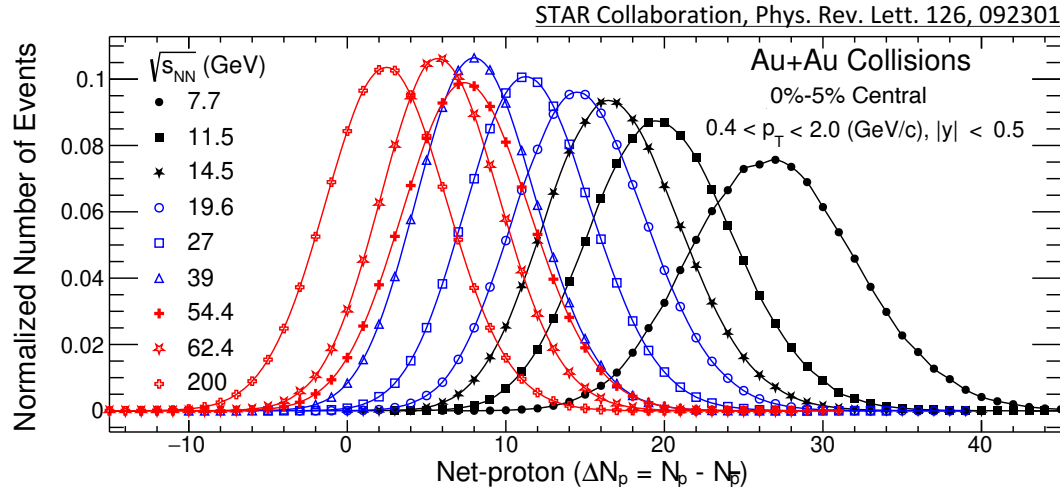
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Baryon number (B), Strangeness (S), Electric charge (Q), Charm (C) 0 / 5,000



➤ The devil is in the tails!

➤ What can we learn from κ_2 ?

Outline

- **Experimental challenges:** Particle identification, efficiency correction, effect of event pileup, volume fluctuations ...
- **Theoretical/phenomenological challenges:** Effect of resonances, charge conservation, effect of magnetic field, cluster formation, baryon annihilation, excluded volume ...

Outline

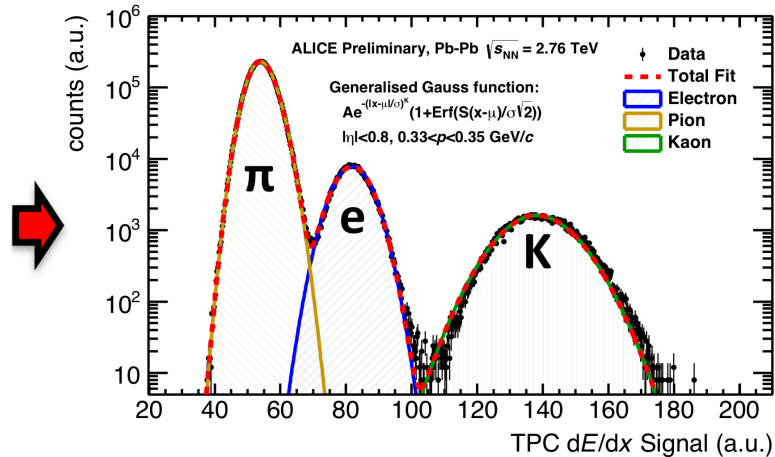
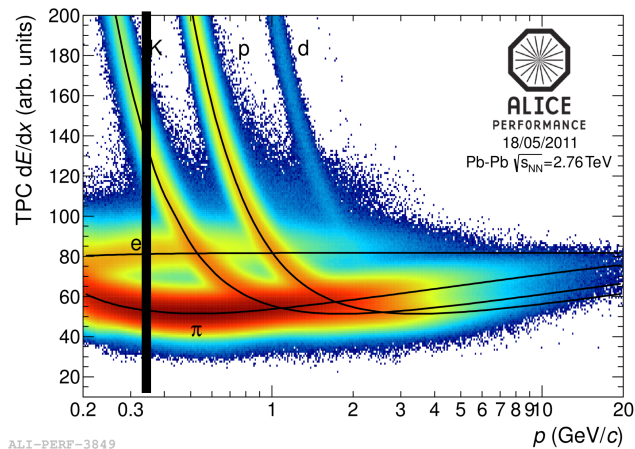
- **Experimental challenges:** Particle identification, efficiency correction, effect of event pileup, volume fluctuations ...
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- How do we measure cumulants of conserved charges?
- How do we interpret the results?
- What have we learned so far from 2nd order cumulants?
 - Net- $[\pi, K, p, \Lambda, \Xi]$ and cross-cumulants and correlations
- What to expect from future?

How do we measure cumulants?

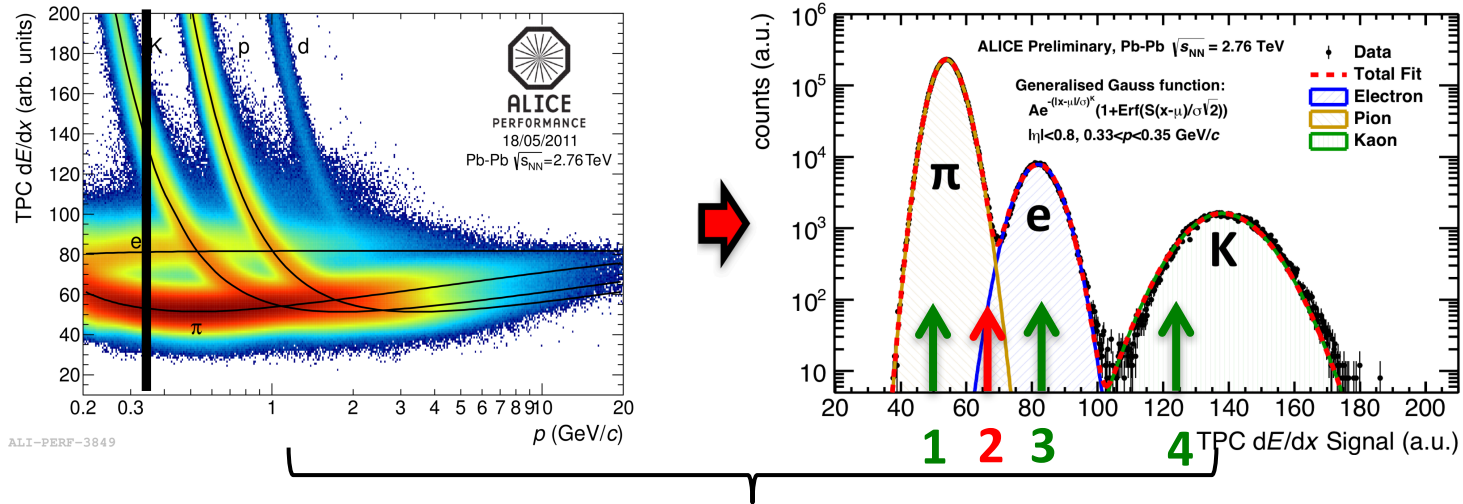
Main challenge: Particle identification (PID)

Cut-based approach (track counting) and **Identity method** (probability counting)



Main challenge: Particle identification (PID)

Cut-based approach (track counting) and **Identity method** (probability counting)

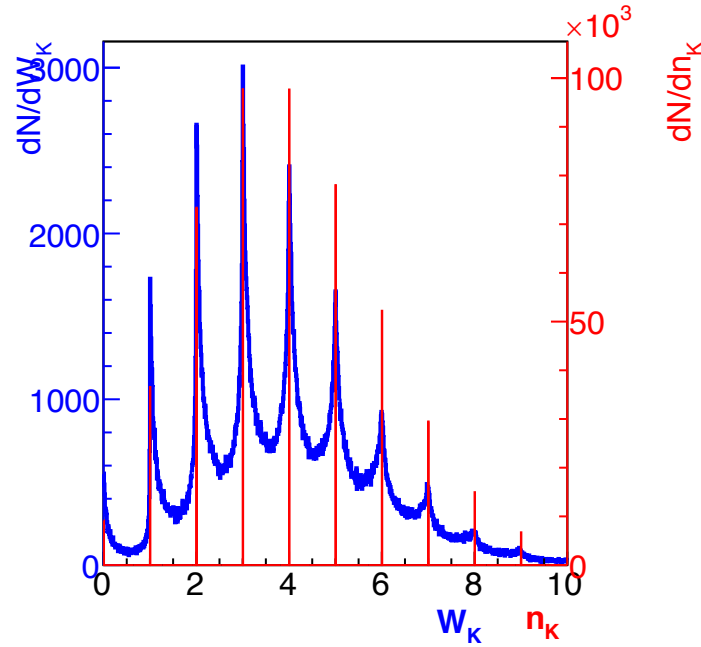


$$\omega_{\pi}^{(1)} = 1, \quad \omega_{\pi}^{(2)} \cong 0.6, \quad \omega_{\pi}^{(3)} = 0, \quad \omega_{\pi}^{(4)} = 0 \quad \Rightarrow \quad W_{\pi} = 1.6 \neq N_{\pi}$$

A. Rustamov, M. Gazdzicki, M. I. Gorenstein, PRC 86, 044906 (2012), PRC 84, 024902 (2011)

A. Rustamov, M. Arslanodk, Nucl. Instrum. A946 (2019) 162622}

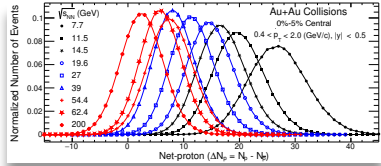
Identity method vs cut-based approach



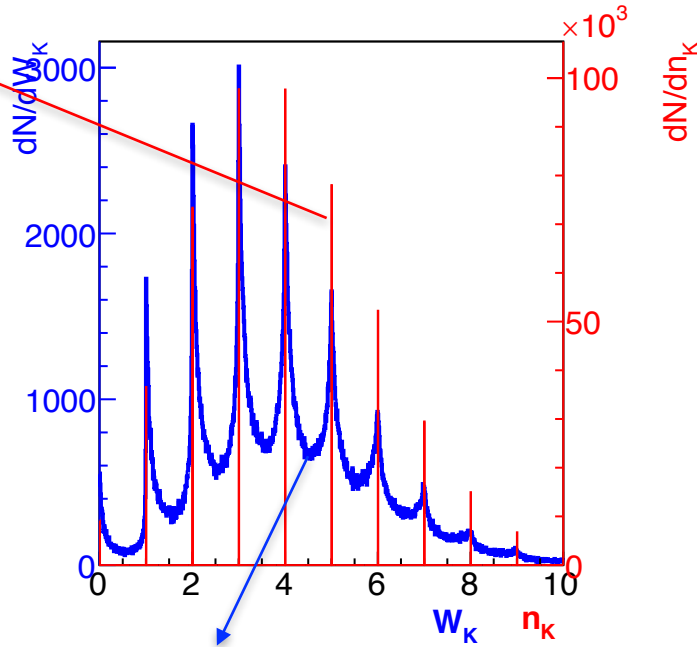
$$\langle N_j^n \rangle = A^{-1} \langle W_j^n \rangle$$

Identity method vs cut-based approach

Cut-based

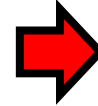


Cost off efficiency!



Identity method

$$\langle N_j^n \rangle$$

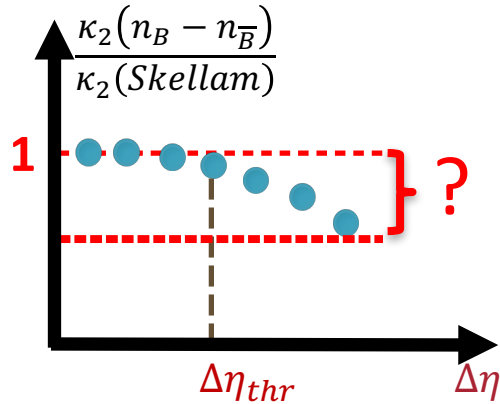


$$\langle N_j^n \rangle = A^{-1} \langle W_j^n \rangle$$

How do we interpret?

To keep in mind!

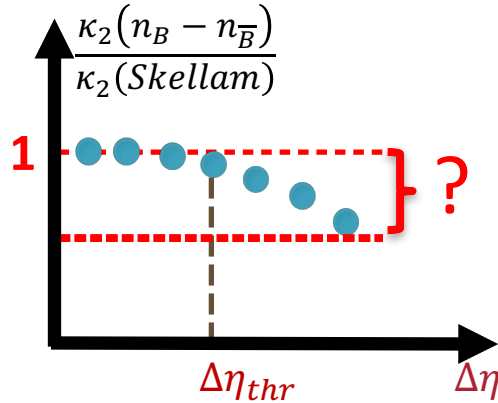
Source of the deviation?



- Baryon number conservation
- Volume fluctuations
- Resonance decays
- Initial-state fluctuations
- ...

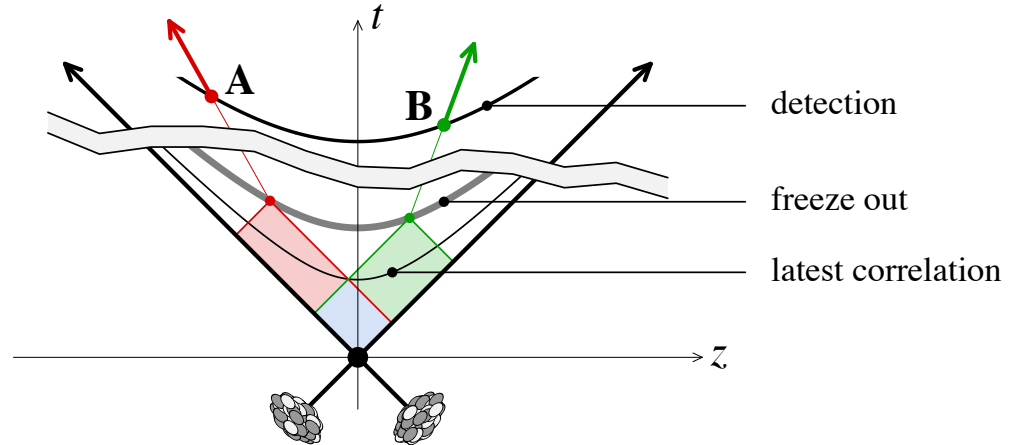
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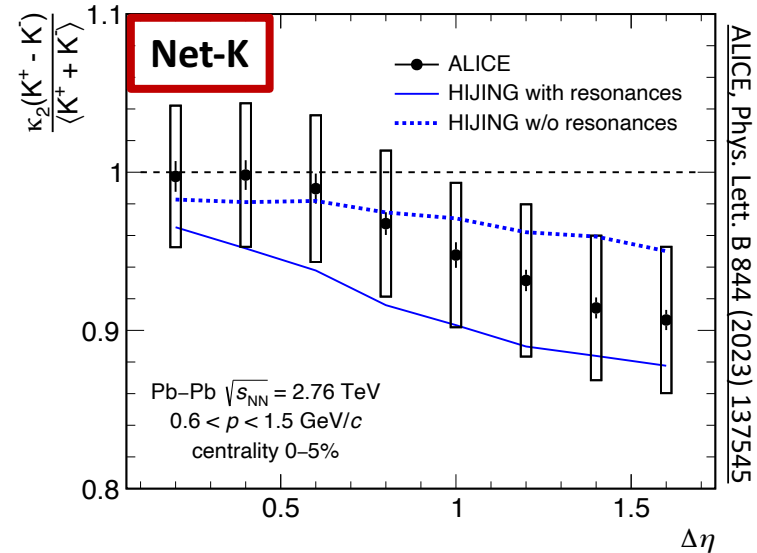
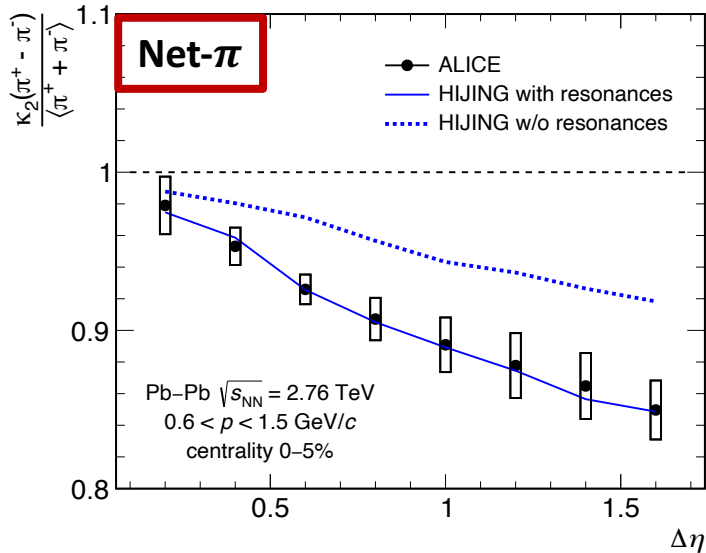
Only early correlations can be long range in rapidity



$$\tau \leq \tau_{\text{freeze out}} e^{-\frac{1}{2}|y_A - y_B|}$$

A. Dumitru, F. Gelis, L. McLerran, and R. Venugopalan, *Nucl. Phys. A* 810 (2008) 91

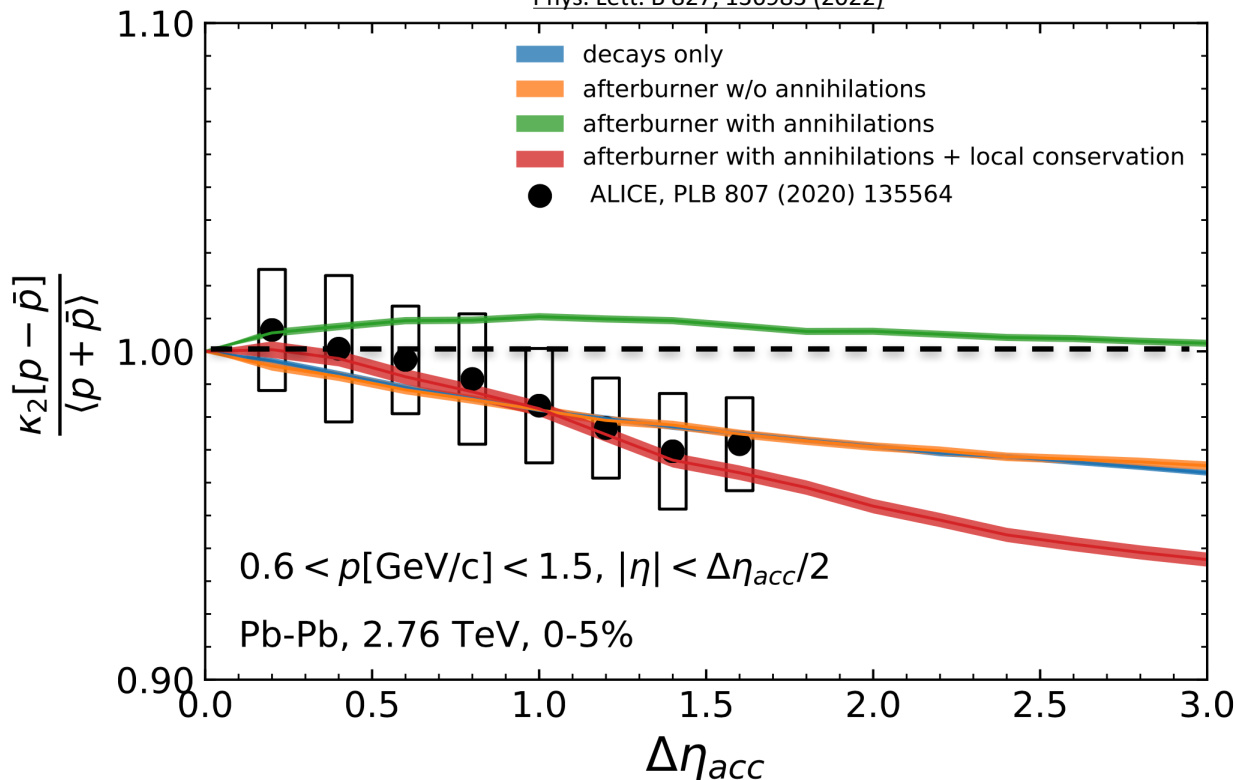
Resonance decays



- **Net- π and net-K are** strongly dominated by resonance contributions
- **Net-[p, Λ , Ξ]** are free from resonance contributions

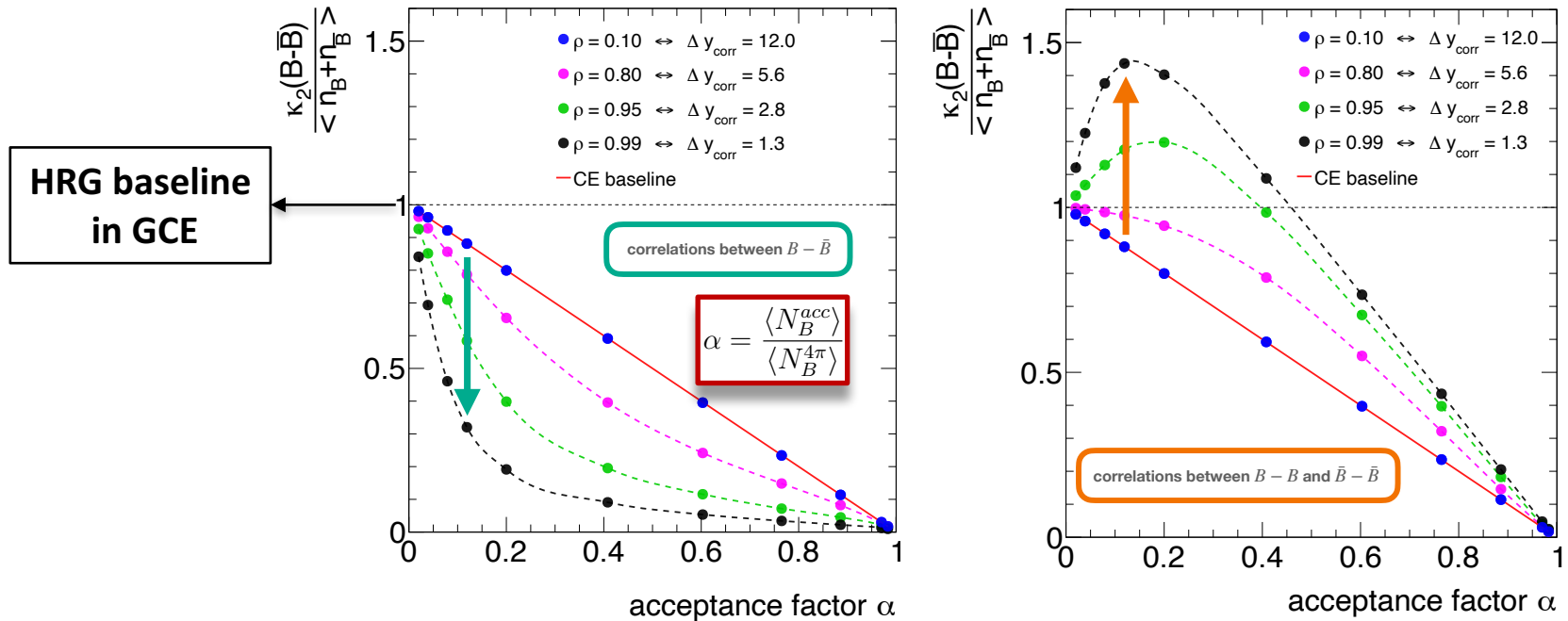
Baryon annihilation

O. Savchuk, V. Vovchenko, V. Koch, J. Steinheimer, H. Stoecker
Phys. Lett. B 827, 136983 (2022)



Baryon number conservation vs “cluster” formation

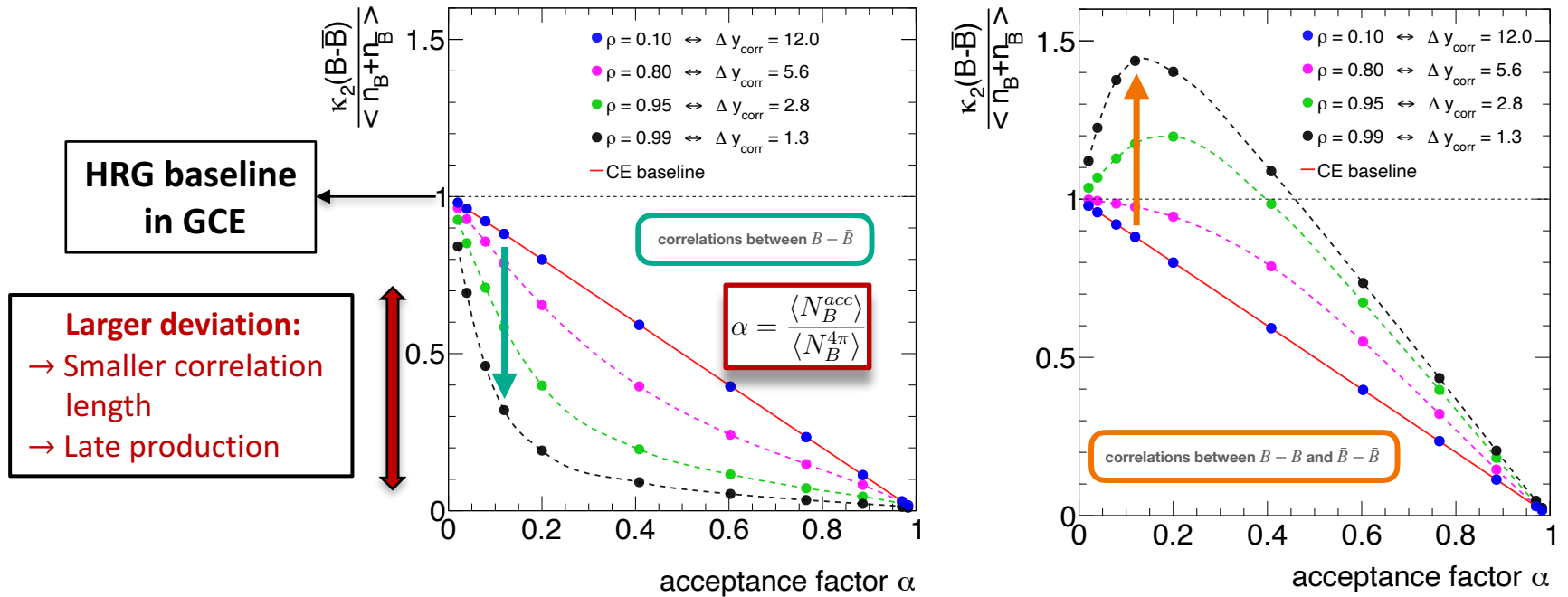
P. Braun-Munzinger, K. Redlich, A. Rustamov, J. Stachel, arXiv:2312.15534v1



- Measured values depend on the fraction of (anti-)protons in the acceptance
- (Global) local baryon number conservation: **unlike-sign correlations**
- (Anti-)proton clusters: **like-sign correlations**

Baryon number conservation vs “cluster” formation

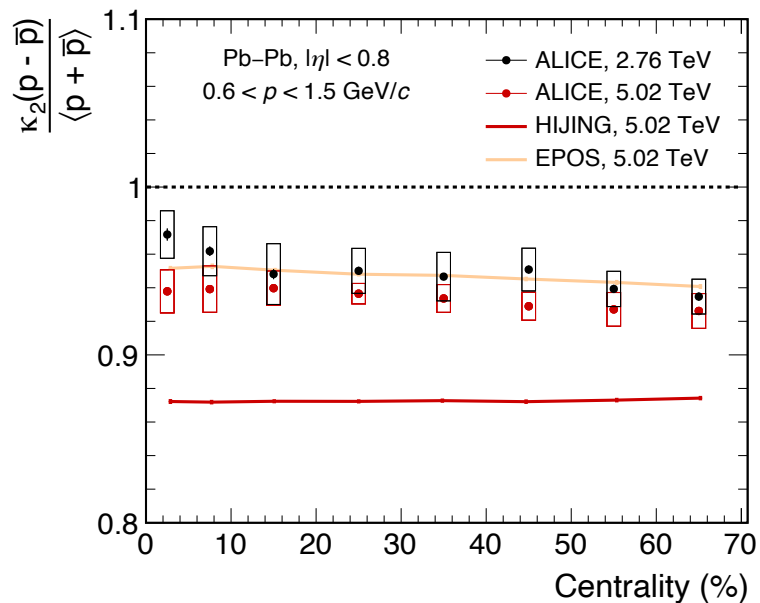
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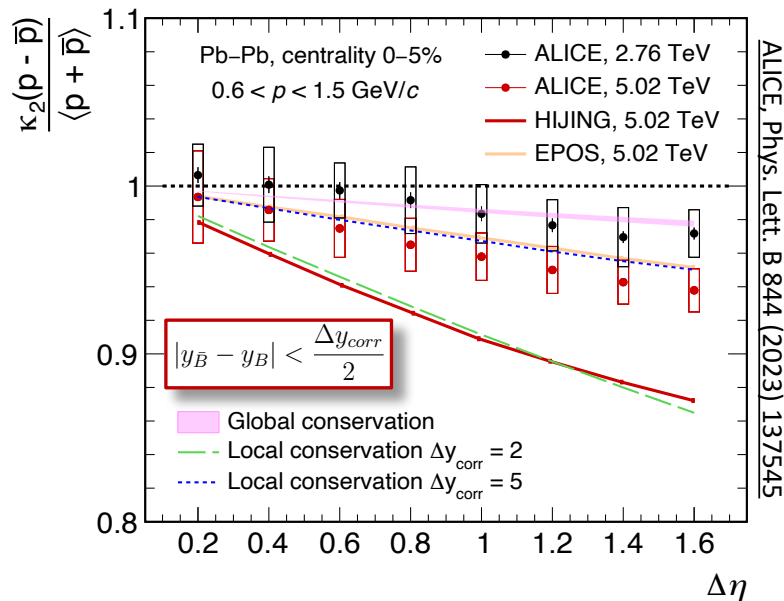
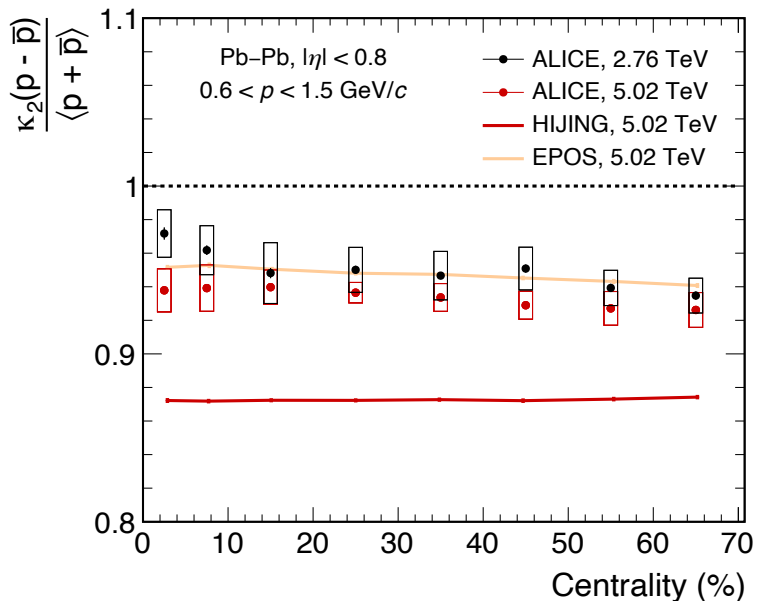
What did we learn?

2nd order cumulants of net-p



- Deviation from Skellam baseline is due to **baryon number conservation**

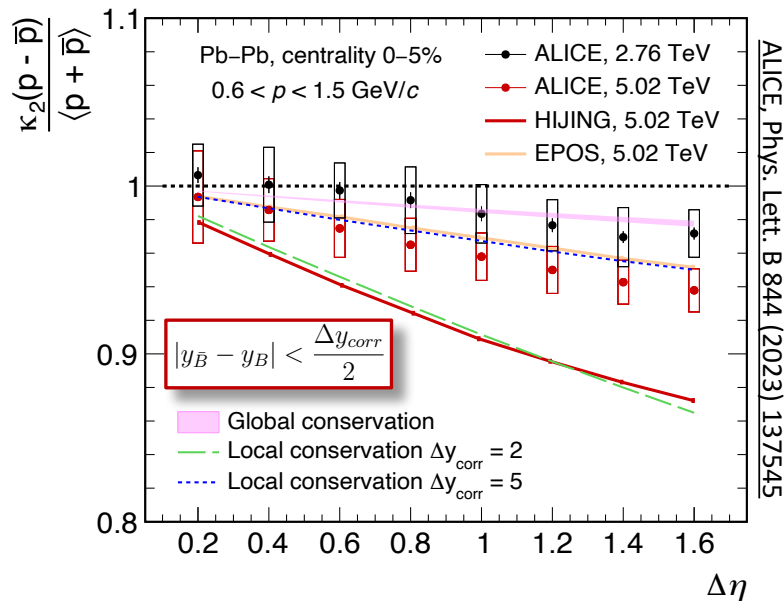
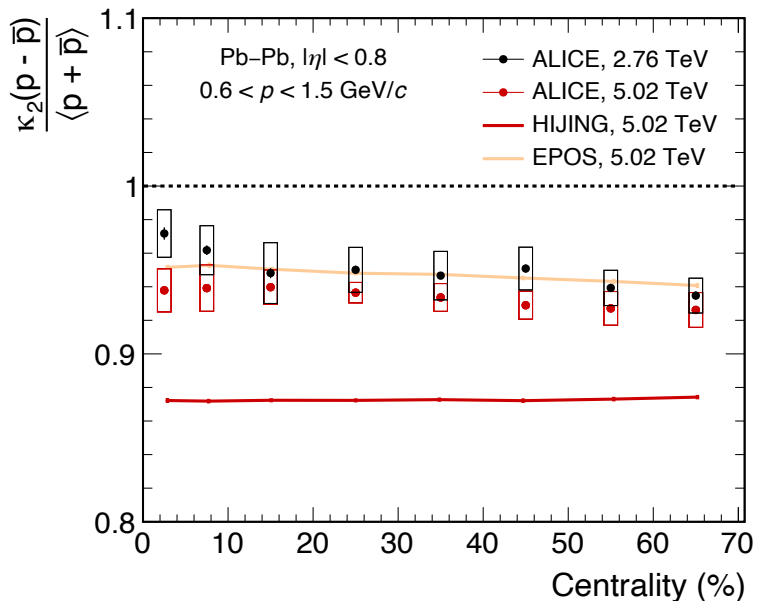
2nd order cumulants of net-p



ALICE Phys. Lett. B 844 (2023) 137545

- Deviation from Skellam baseline is due to **baryon number conservation**
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- Event generators based on **string fragmentation (HIJING)** conserve baryon number over $\Delta y = \pm 1$ unit

2nd order cumulants of net-p



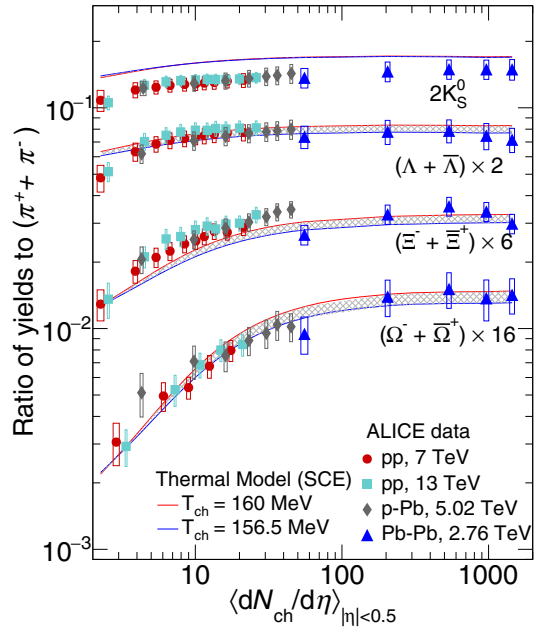
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How about strangeness?

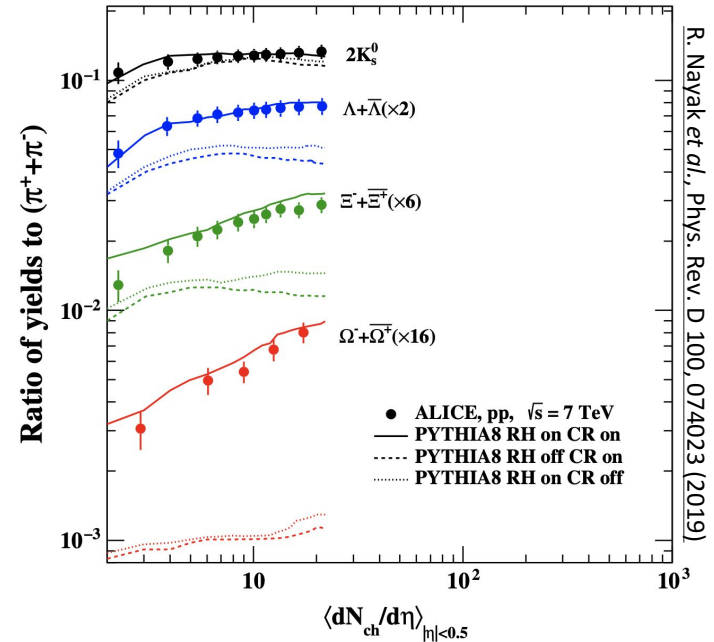
Reminder: Strangeness enhancement/suppression

Canonical statistical model



J. Cleymans, P. M. Lo, K. Redlich, N. Sharma
Phys. Rev. C 103, 014904 (2021)

Lund string fragmentation (PYTHIA)

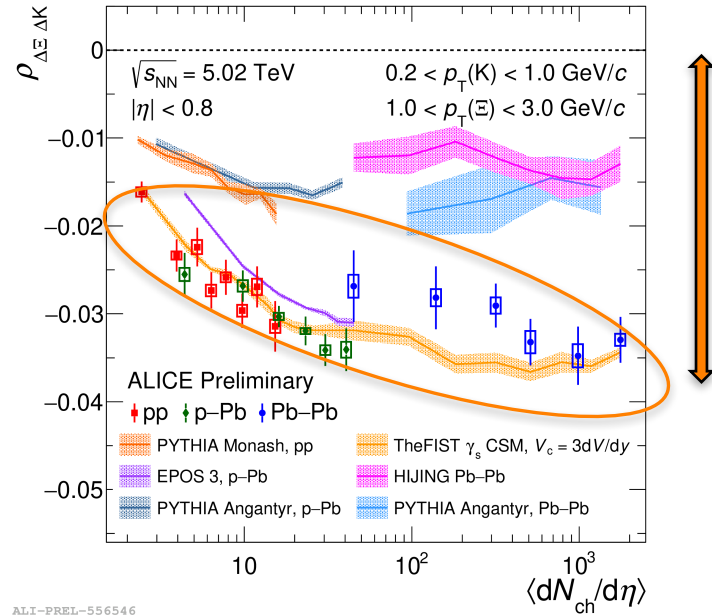
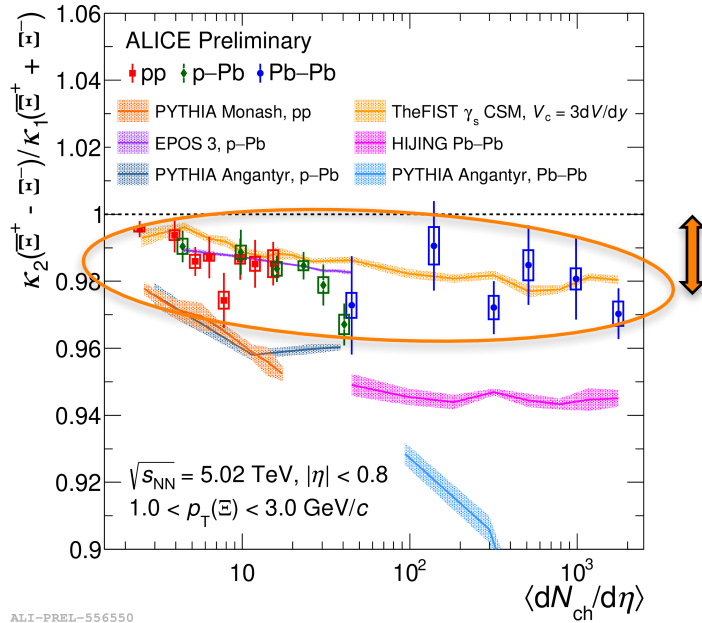


R. Nayak et al., Phys. Rev. D 100, 074023 (2019)

First order moments:

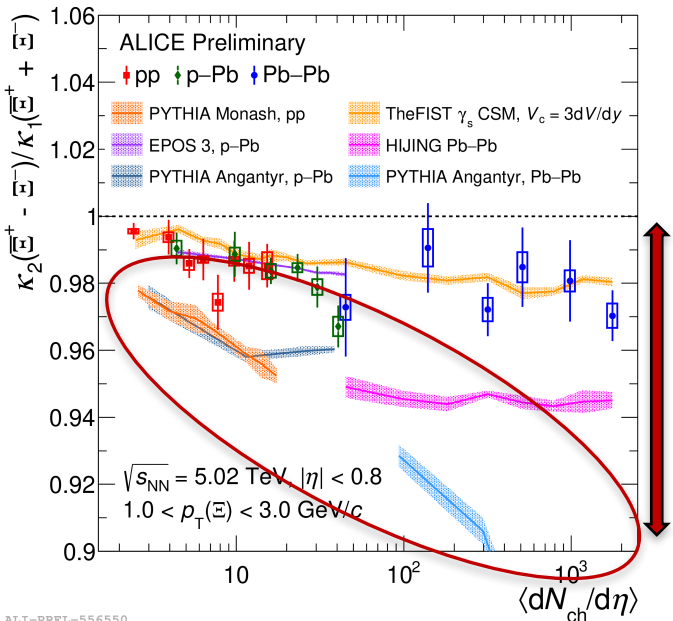
Thermal model with $\mu_B \approx 0$ and $T \approx 150 - 160$ MeV and
PYHTIA with “RH on and CR” on does well at lower multiplicities

2nd order cumulants of Net-Ξ & Net-Ξ̄ — net-K correlations

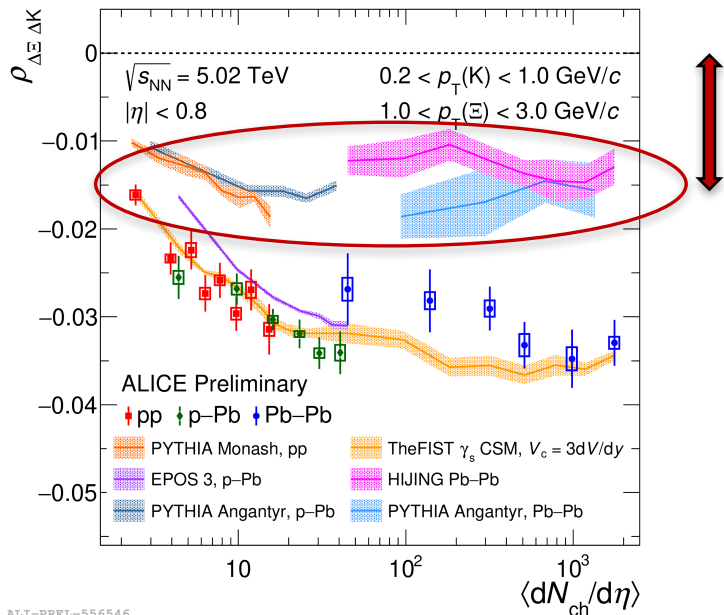


- Canonical picture describes the data with **correlation volume of about 3dV/dy**
 → Indication of large volume (early production) for strangeness (as in case of baryon number)

2nd order cumulants of Net-Ξ & Net-Ξ̄ – net-K correlations



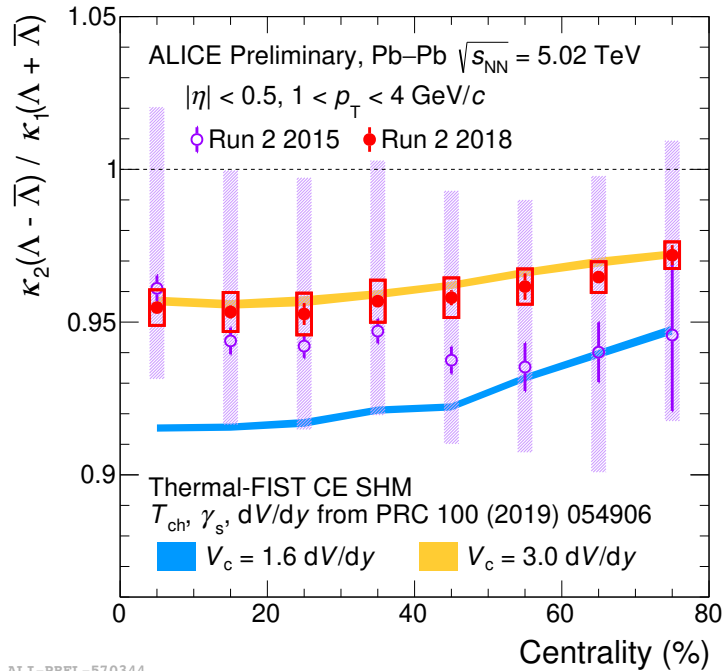
ALI-PREL-556550



ALI-PREL-556546

- Canonical picture describes the data with **correlation volume of about 3dV/dy**
 → Indication of large volume (early production) for strangeness (as in case of baryon number)
- Event generators based on **string fragmentation fails for the second order**

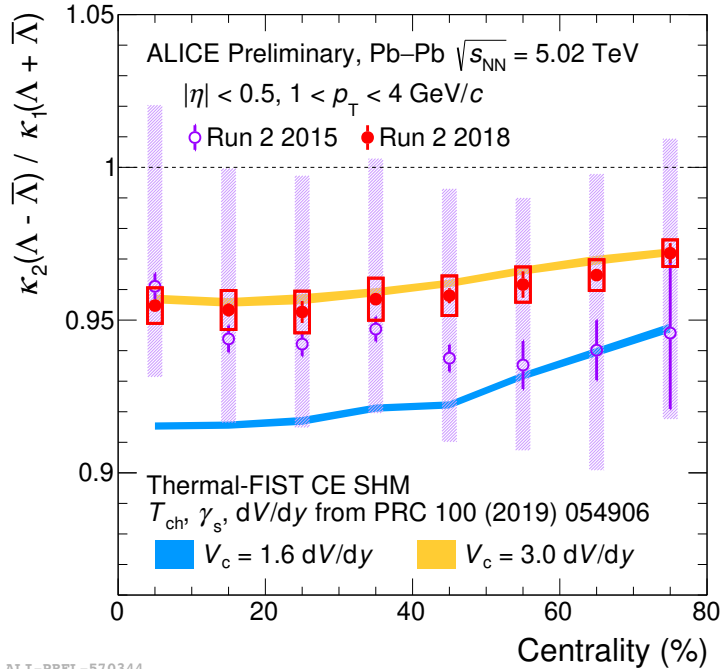
2nd order cumulants of **Net- Λ**



ALI-PREL-570344

- Canonical picture describes the data with **correlation volume of about 3dV/dy**

2nd order cumulants of Net- Λ



ALI-PREL-570344

- Canonical picture describes the data with **correlation volume of about 3dV/dy**

How about off-diagonal cumulants?

$$\chi_{B,S,Q}^{lmn} = \frac{1}{VT^3} \sigma_{B,S,Q}^{lmn}$$

$$\begin{aligned} \sigma_{BS}^{11} &= \langle BS \rangle - \langle B \rangle \langle S \rangle \\ \sigma_{QS}^{11} &= \langle QS \rangle - \langle Q \rangle \langle S \rangle \\ \sigma_{QB}^{11} &= \langle QB \rangle - \langle Q \rangle \langle B \rangle \end{aligned}$$

$$\begin{aligned} \sigma_S^2 &= \langle S^2 \rangle - \langle S \rangle^2 \\ \sigma_B^2 &= \langle B^2 \rangle - \langle B \rangle^2 \\ \sigma_Q^2 &= \langle Q^2 \rangle - \langle Q \rangle^2 \end{aligned}$$



$$C_{BS} = \sigma_{BS}^{11} / \sigma_S^2$$

$$C_{QS} = \sigma_{QS}^{11} / \sigma_S^2$$

$$C_{QB} = \sigma_{QB}^{11} / \sigma_B^2$$

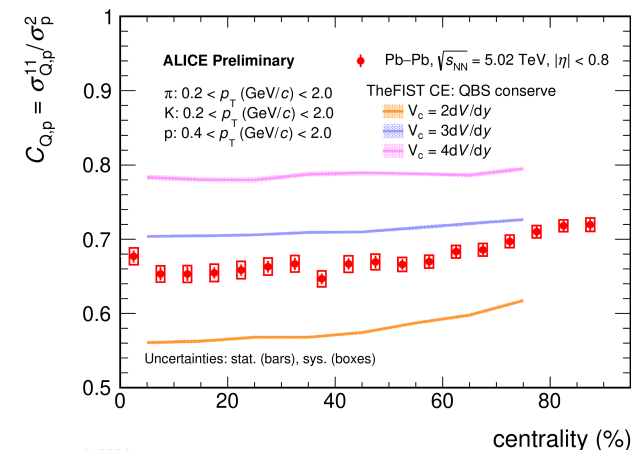
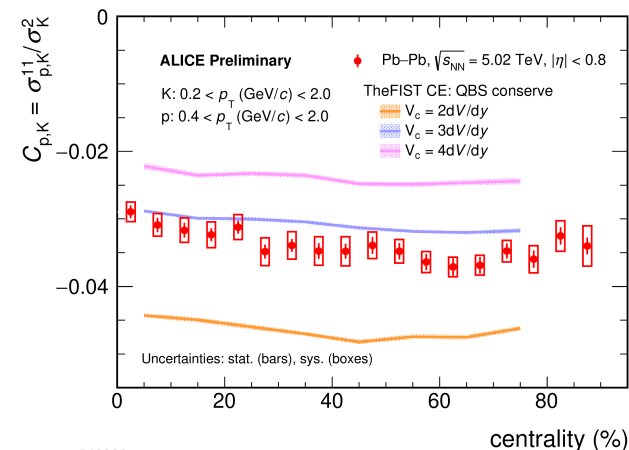
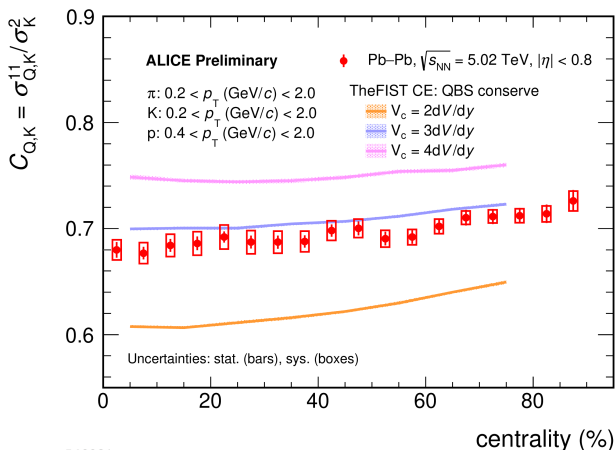
Proxies: Charge: K, π , p | Baryon: p | Strangeness: K

Cross cumulants in view of correlation volume

Q - K

p - K

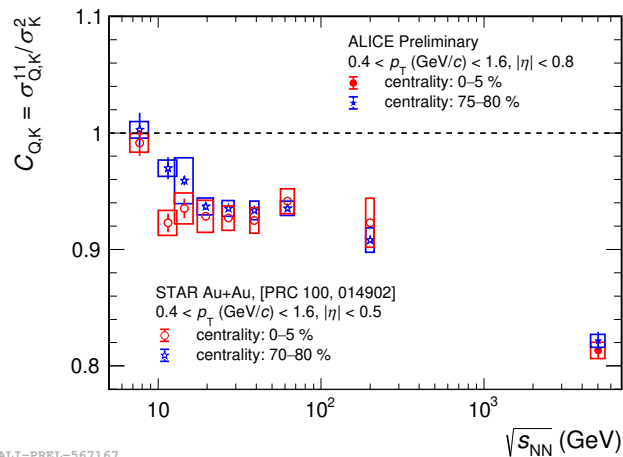
Q - p



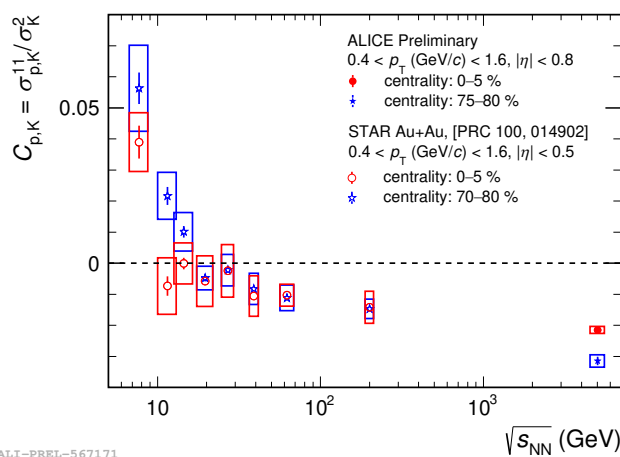
- **Q, B and S conserved** within a correlation volume
V. Vovchenko et al., Phys. Rev. C 100, 054906 (2019)
- Simultaneous description leads to $V_c = \sim 2.64dV/dy$!!!

Cross cumulants: energy dependence

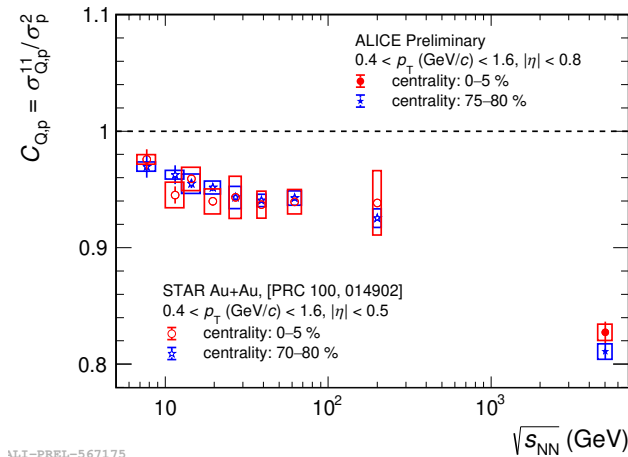
Q - K



p - K



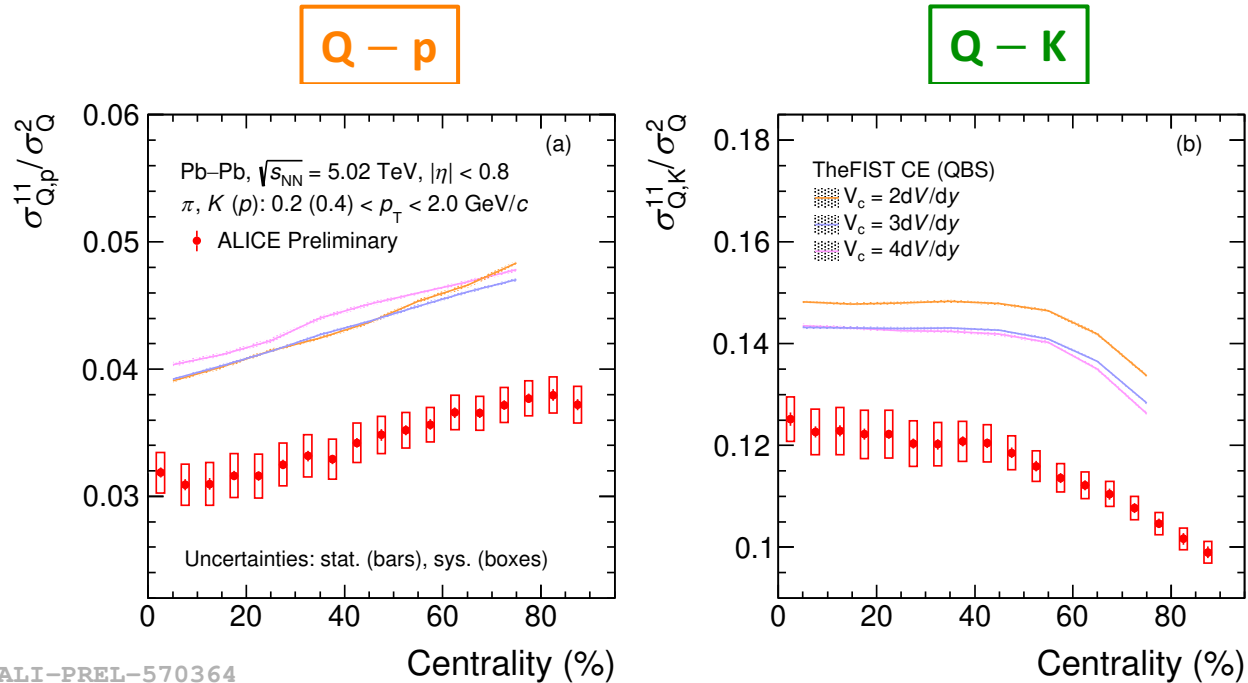
Q - p



➤ **Monotonic decrease of the correlations with increasing energy**

- How much of this because of conservation?
- What are the other possible contributions?

Cross cumulants: Volume independent normalization



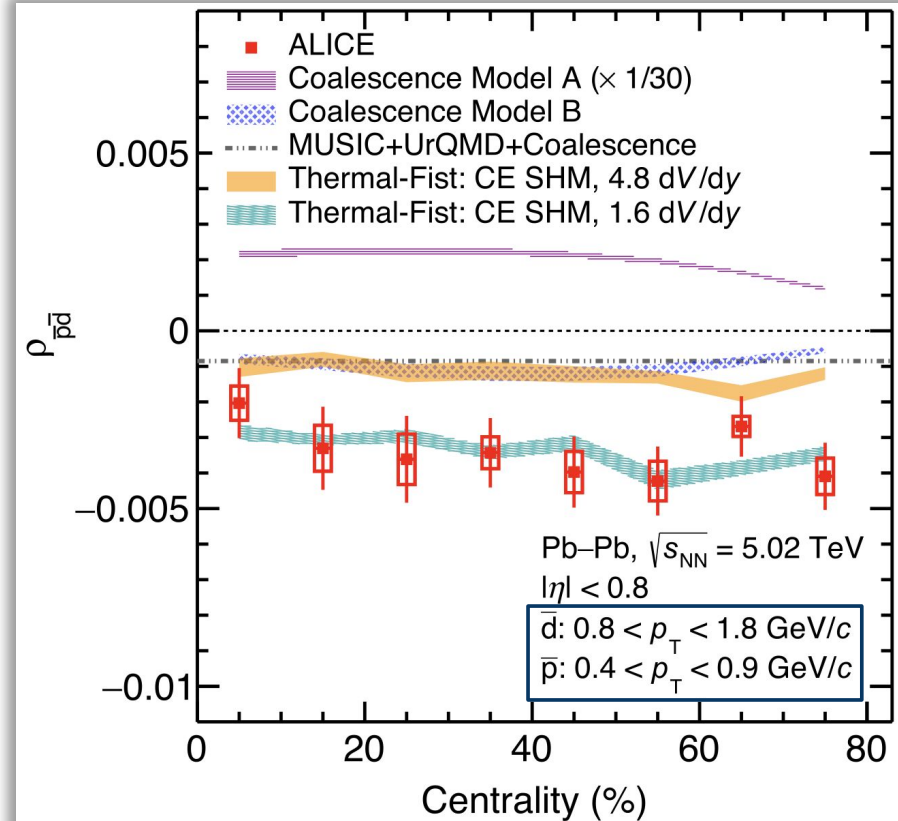
- **Sensitivity to V_c is gone but there is a deviation**
→ What is the underlying physics?

Light nuclei production in view of correlation volume

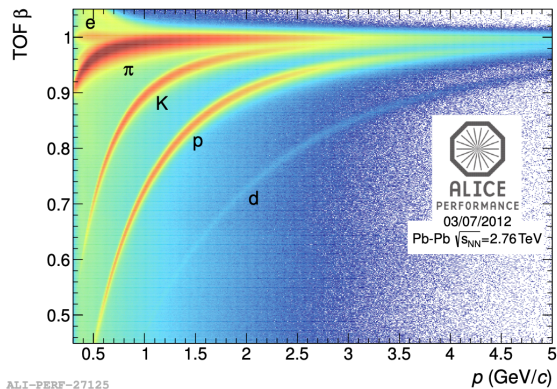
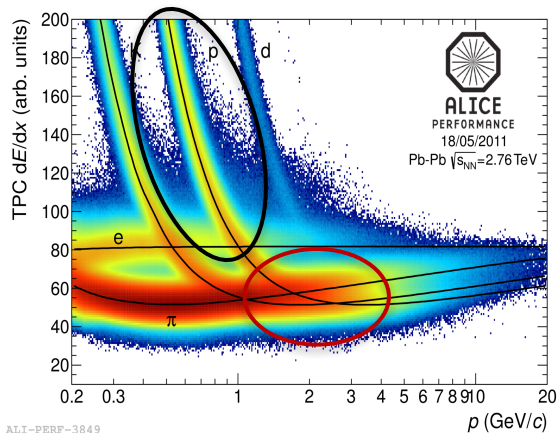
- **Simple coalescence** Z. Fecková *et al.*, PRC 93, 054906 (2016)
 - **Model A**: correlated nucleons
 - **Model B**: independent nucleons
- **Improved coalescence** K.-J. Sun *et al.*, PLB, 840, 137864 (2023)
 - MUSIC + UrQMD + Coalescence: No initial correlation between protons and neutrons
- **Canonical Statistical Model** V. Vovchenko *et al.*, PLB 785, (2018) 171
 - Correlation volume, V_c

- **Different correlation volume than for B and S**
- **Stay tuned for SQM** $\rightarrow \bar{d}\Delta\Lambda$ correlations

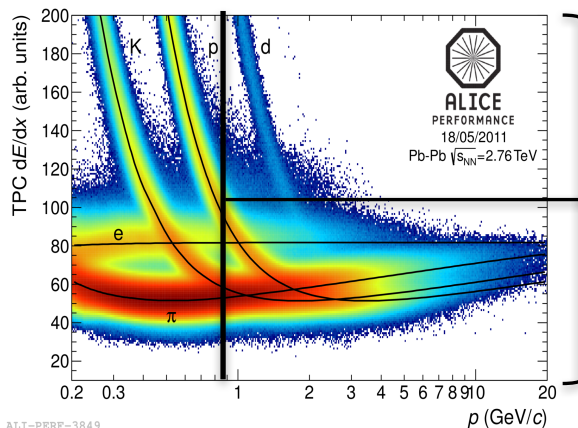
ALICE, PRL 131 (2023) 041901



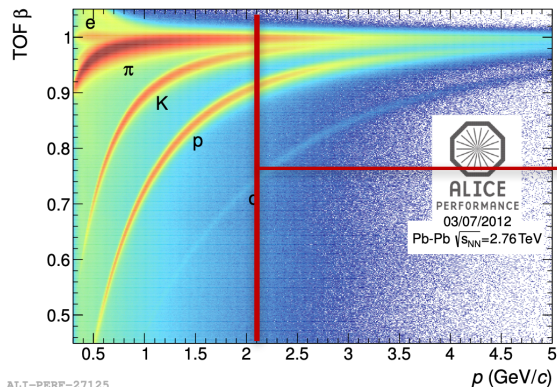
Pushing 2nd net-p to the limits with Identity Method



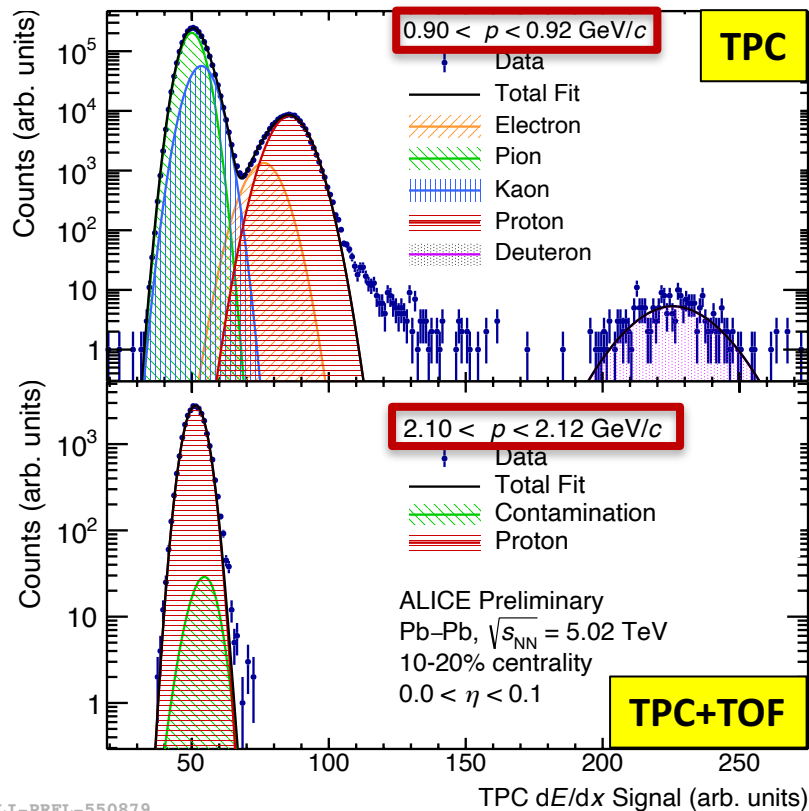
Pushing 2nd net-p to the limits with Identity Method



ALI-PERF-3849



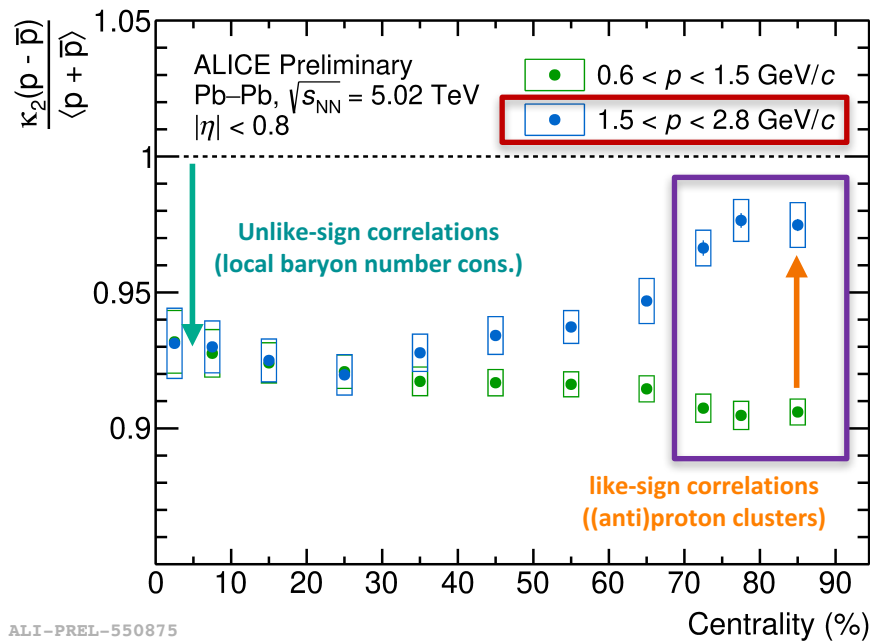
ALI-PERF-27125



ALI-PREL-550879

Pushing 2nd net-p to the limits

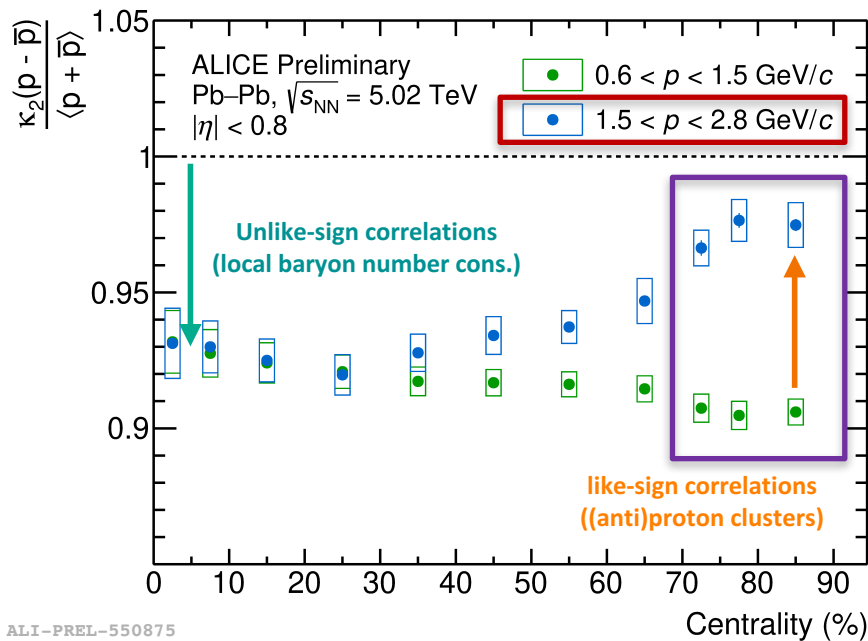
More peripheral and larger momentum



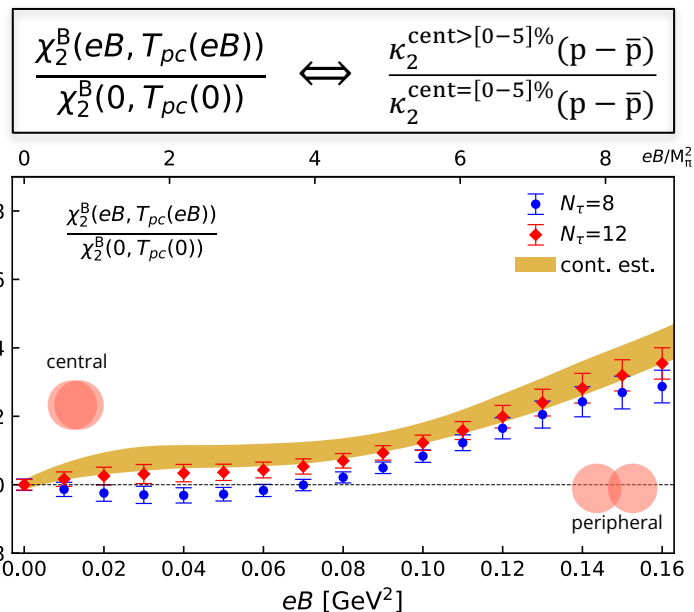
ALI-PREL-550875

Pushing 2nd net-p to the limits

More peripheral and larger momentum

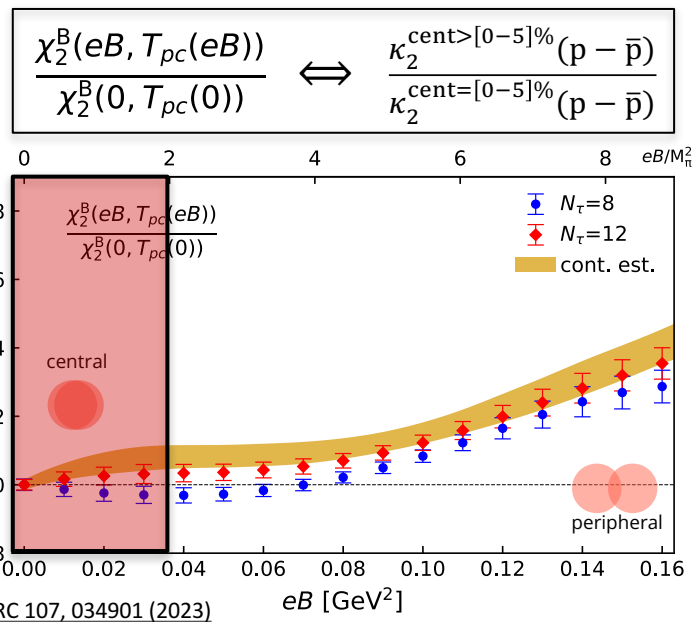
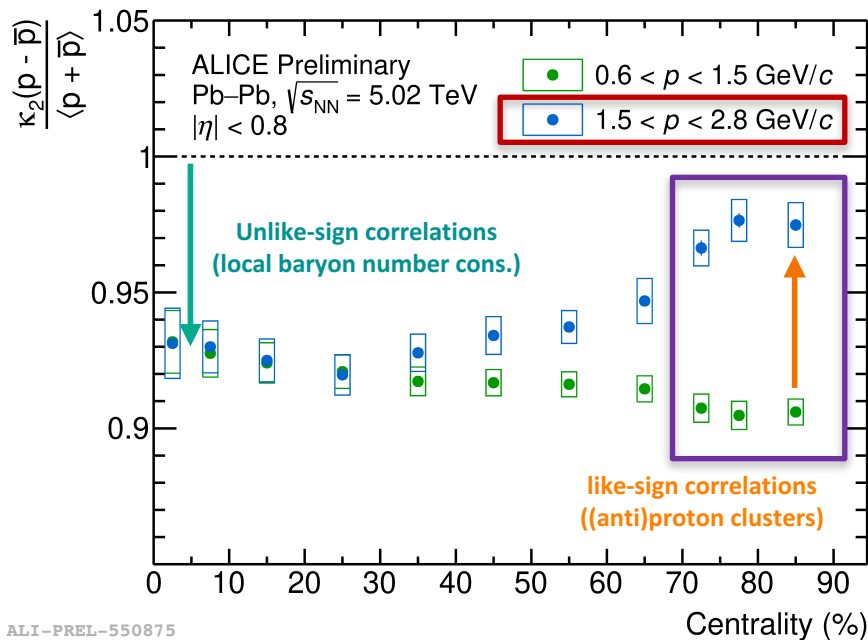


ALI-PREL-550875



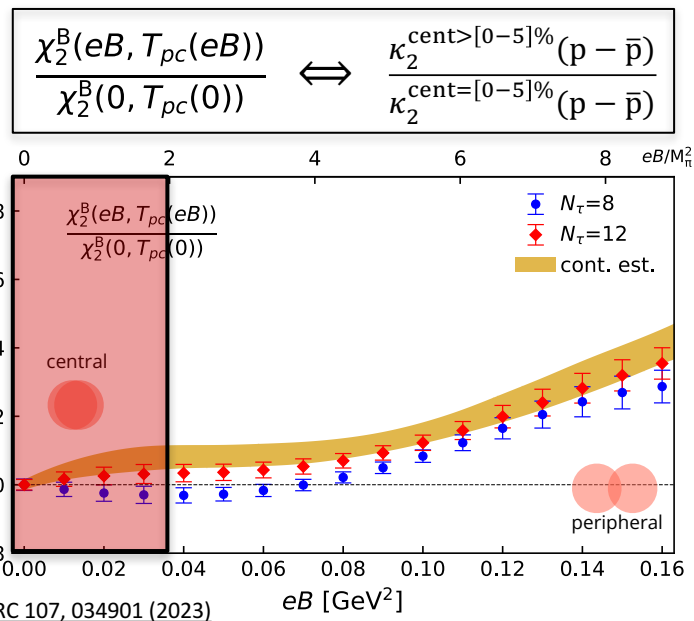
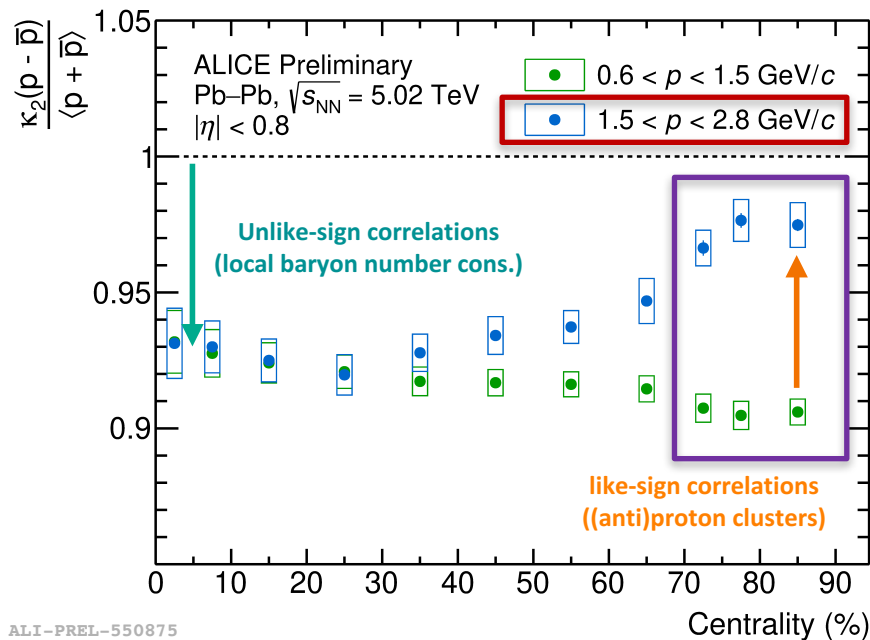
Pushing 2nd net-p to the limits

More peripheral and larger momentum



Pushing 2nd net-p to the limits

More peripheral and larger momentum



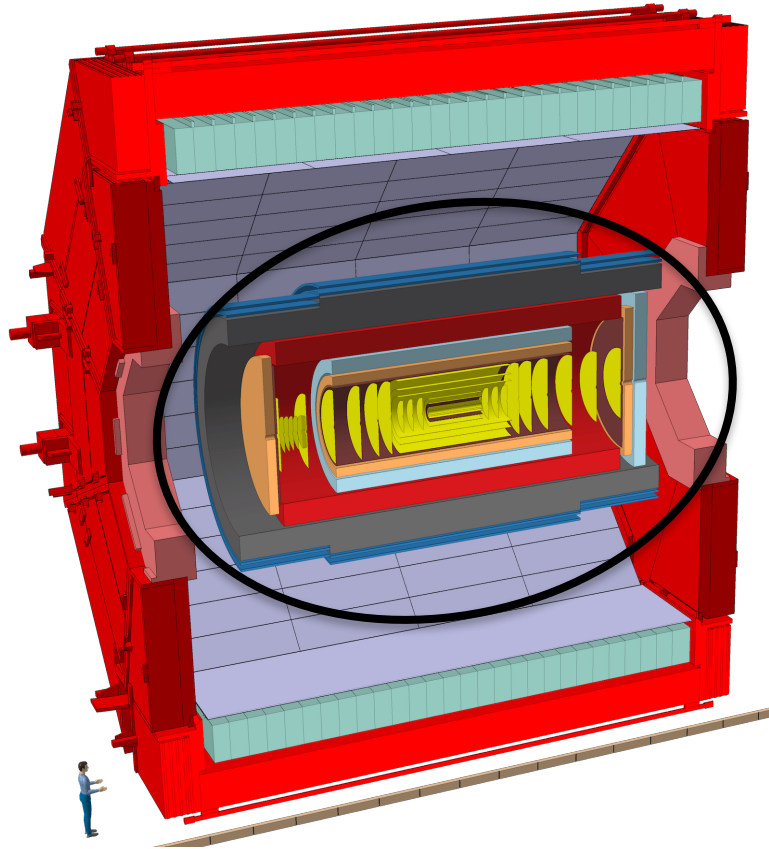
Cluster formation, magnetic field effect or ...?

What can we learn?

(ALICE 3)

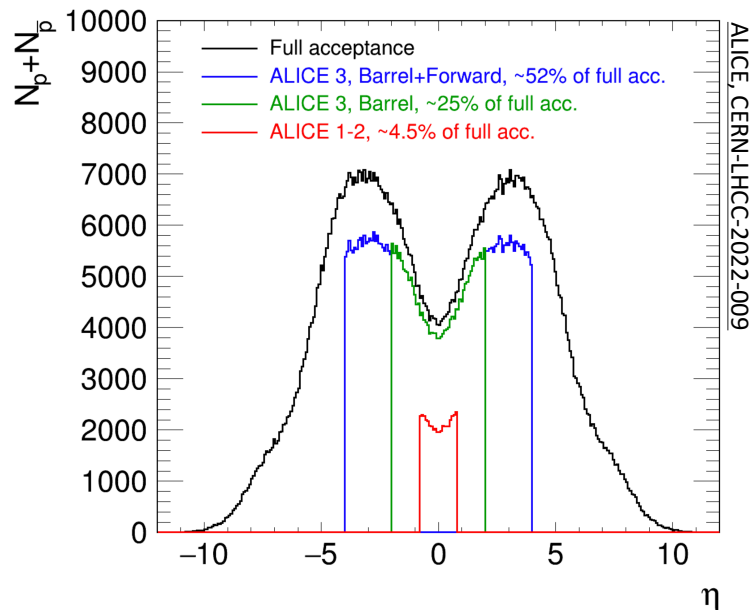
Future beyond early 2030s: ALICE 3

ALICE, CERN-LHCC-2022-009

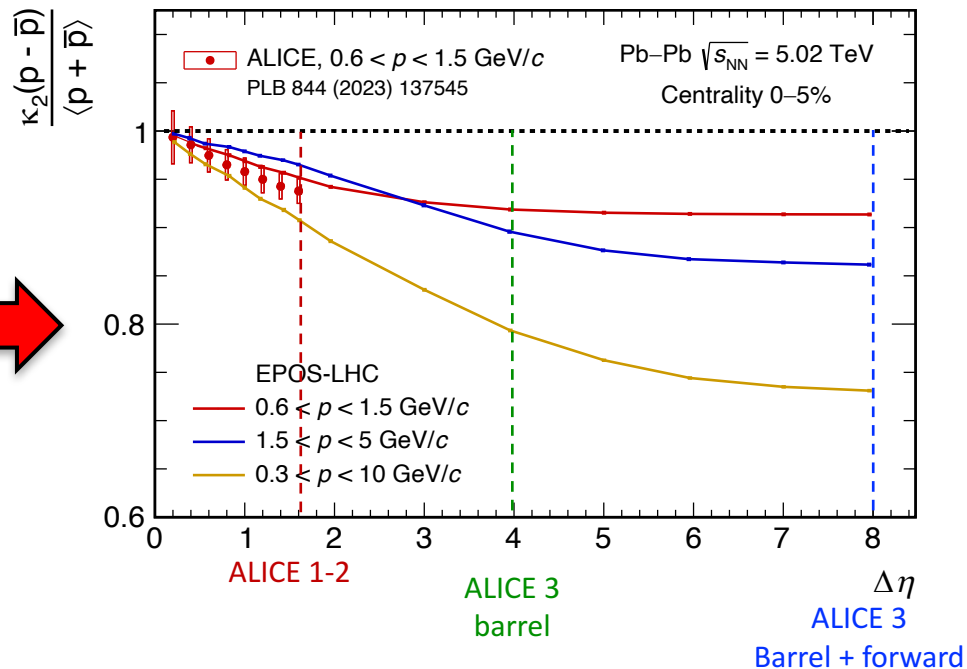


- ✓ **High statistics** → $O(10^9)$ billion events
- ✓ **Large acceptance** → $|\eta| < 4$
- ✓ **High PID purity** → $0.3 < p < 10$ GeV/c
- ✓ **High efficiency** → $\sim 95\%$
- ✓ **Excellent vertexing** → $O(3\mu\text{m})$ resolution

2nd order cumulants of net-p in ALICE 3



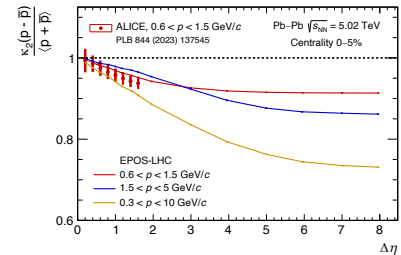
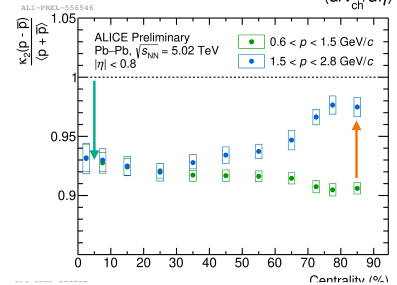
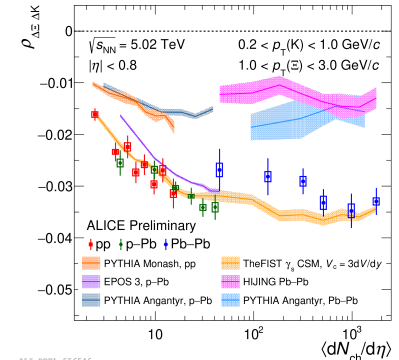
- **High PID purity and efficiency within a larger acceptance**
($0.3 < p < 10$ GeV/c, $|\eta| < 4$)



- **More differential and high precision to disentangle:**
Thermal blurring, Initial-state fluctuations, baryon annihilation, excluded volume effects, baryon number conservation ...

Summary

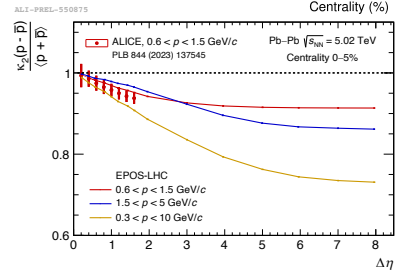
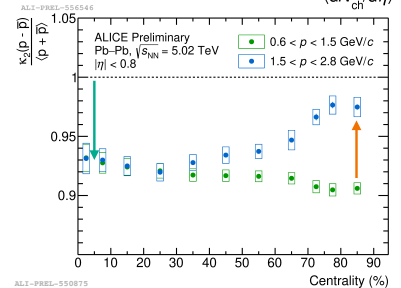
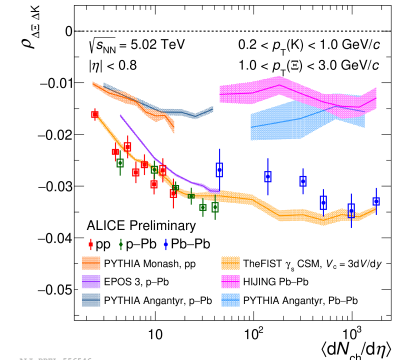
- **String fragmentation fails** at the second order net- $[p, \Lambda, \Xi]$
- **Large V_c (≈ 3 dV/dy)** but still not fully global
 - What is the source of “locality”?
 - How large is the contribution from annihilation etc.?
- **Slightly smaller V_c for net-Q than net- $[p, \Lambda, \Xi]$**
 - Assumption in the implementation of the V_c and/or unprecise description of resonances in FIST?
 - Contribution from other hadronisation mechanisms? Hard vs soft? Coalescence? ...
- **Larger momentum range** \rightarrow interesting centrality dependence
 - Magnetic field? What do pp collisions say?
 - Cluster formation?
- **What impact do these effects have on the higher-order cumulants?**



Summary

- **String fragmentation fails** at the second order net- $[p, \Lambda, \Xi]$
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 - Magnetic field? What do pp collisions say?
 - Cluster formation?
- **What impact do these effects have on the higher-order cumulants?**

A lot to do but future is very bright!

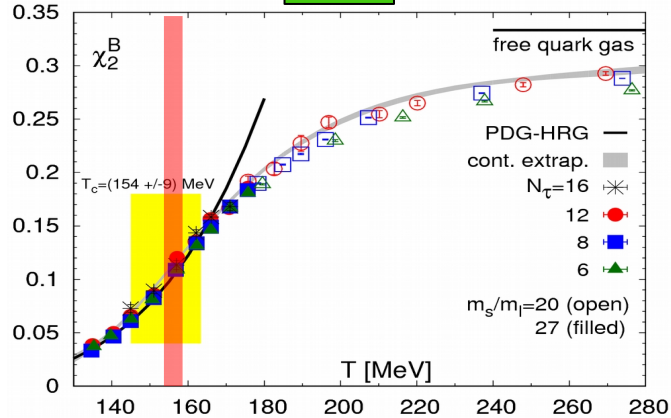


BACKUP

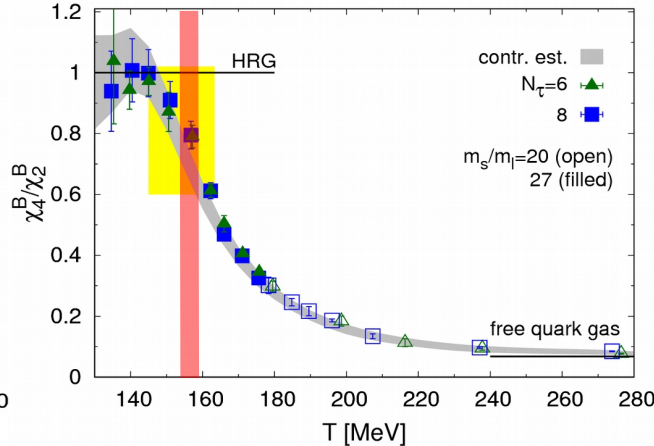
Example case: $\mu_B \approx 0$

- **Baseline:** Difference between two independent Poissonian distributions (Skellam distr.)
 $\Rightarrow \kappa_n/\kappa_2$ is **0 (n odd) or 1 (n even)**
- **Holy grail:** Critical behavior as from 6th order
 \Rightarrow **4th order ~30%, 6th order ~150%**

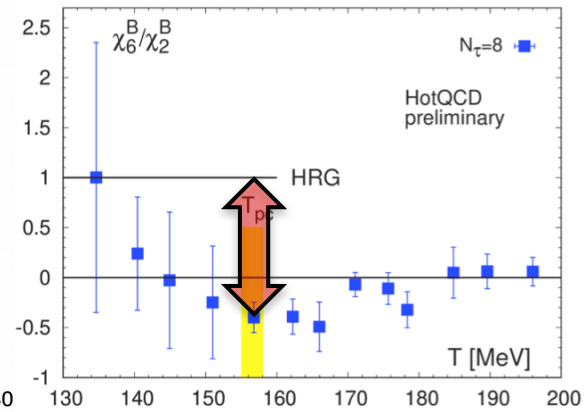
2nd



4th

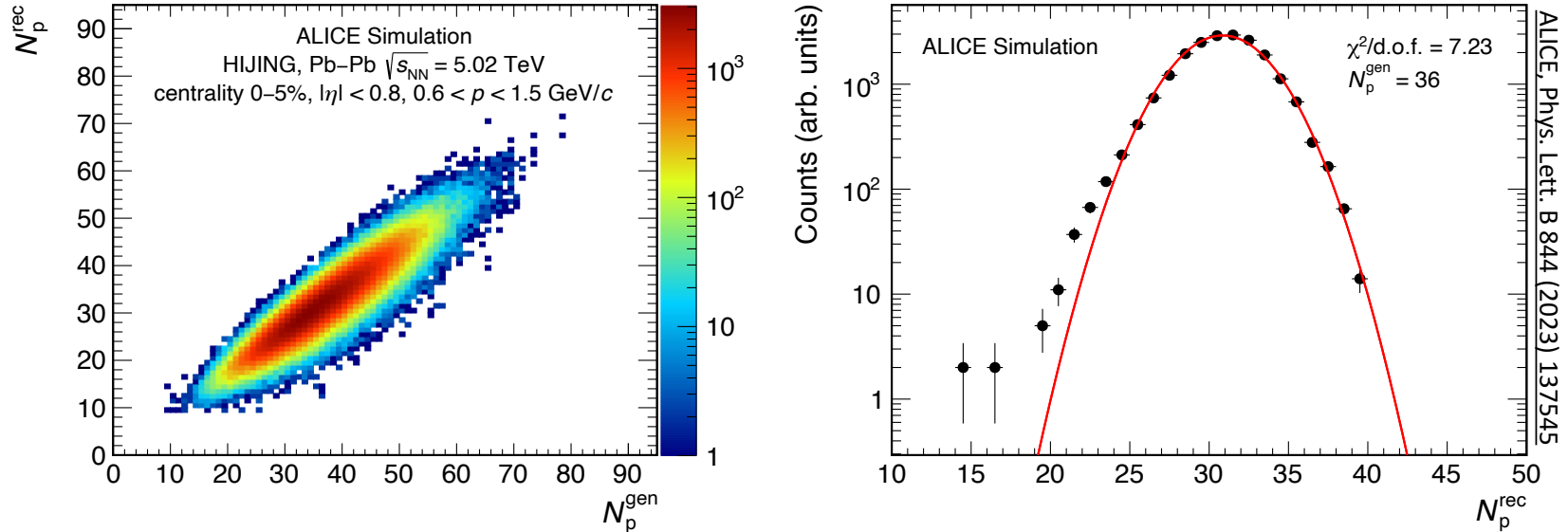


6th



Efficiency correction

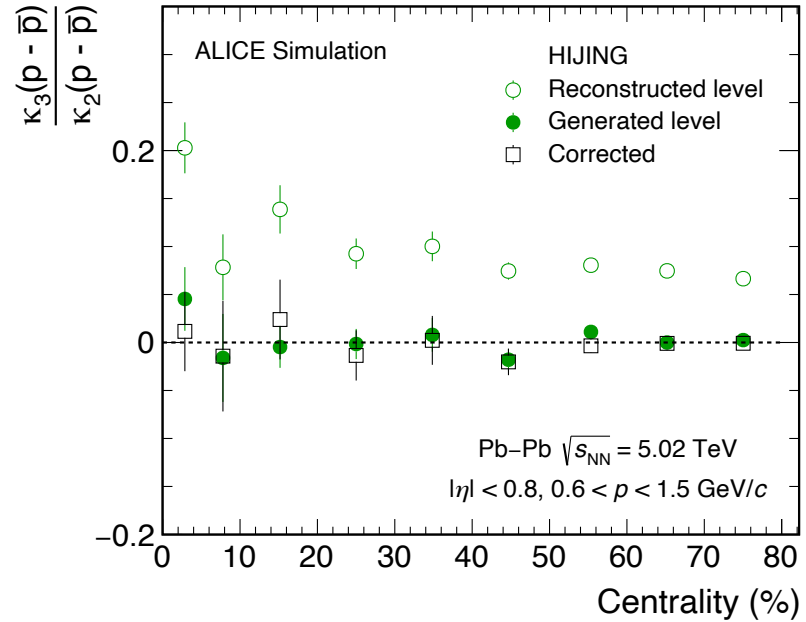
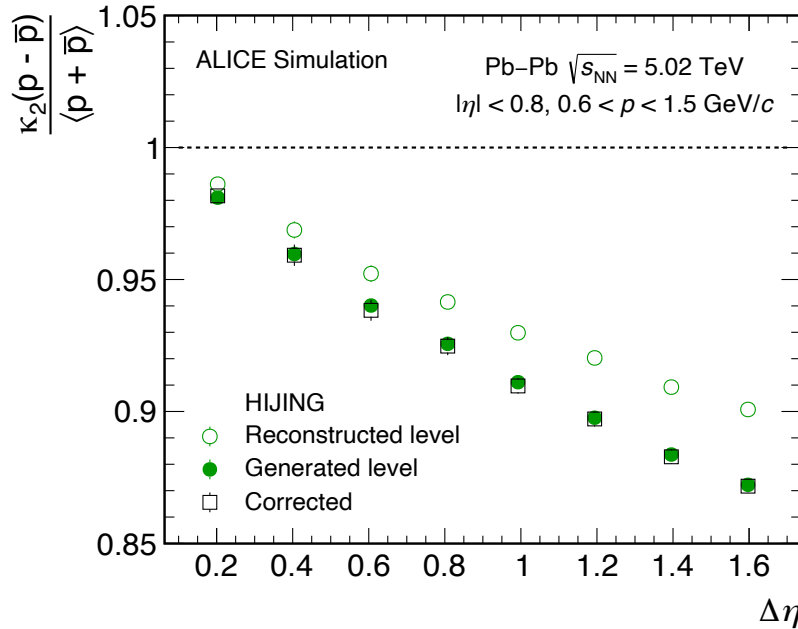
Binomiality of the detector response is important for the efficiency correction



Slight deviation from the binomial efficiency loss

- Event and track selection
- TPC dE/dx calibration in particular for the events with **pileup**
M. Arslanodk, E. Hellbär, M. Ivanov, R.H. Münzer and J. Wiechula, *Particles* 2022, 5(1), 84-95
- Realistic detector simulation

Efficiency correction



ALICE, Phys. Lett. B 844 (2023) 137545

Very good closure despite the slight deviation from binomial loss

Efficiency correction with binomial assumption:

T. Nonaka, M. Kitazawa, S. Esumi, Phys. Rev. C 95, 064912 (2017)

Adam Bzdak, Volker Koch, Phys. Rev. C 86, 044904 (2012)

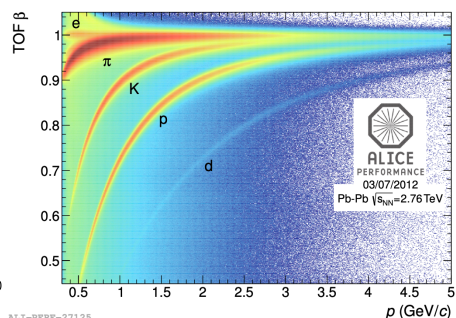
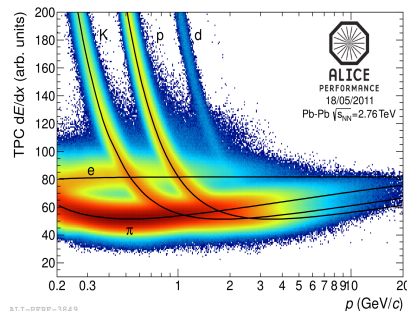
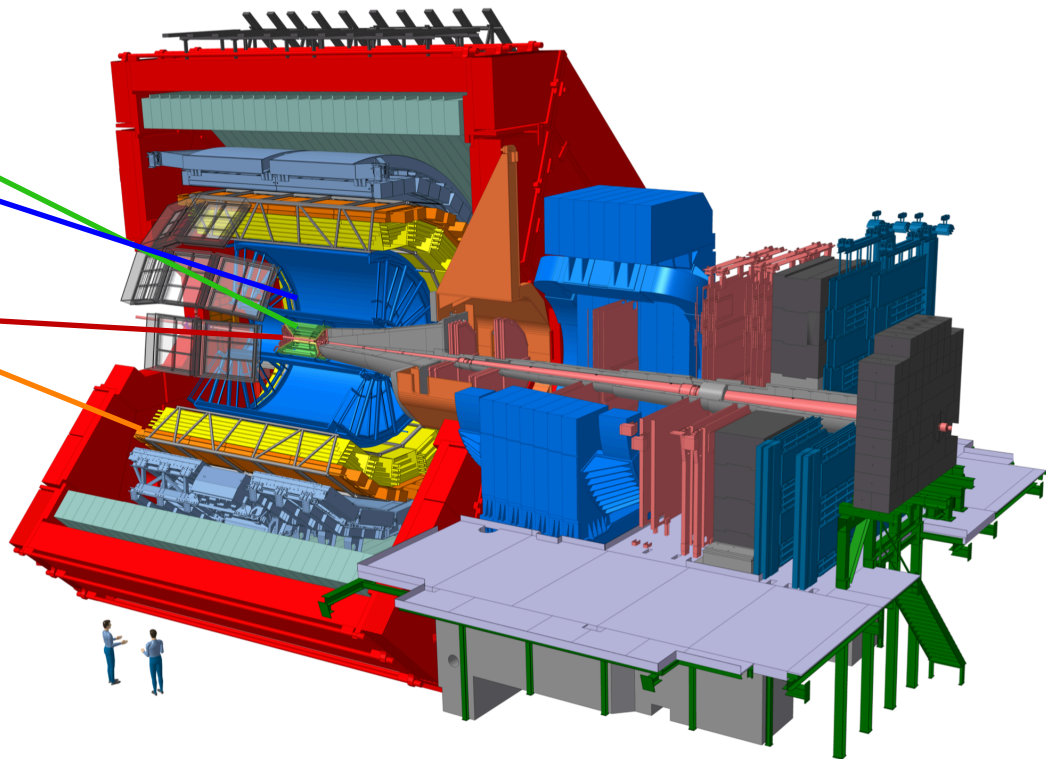
A Large Ion Collider Experiment

Main detectors used:

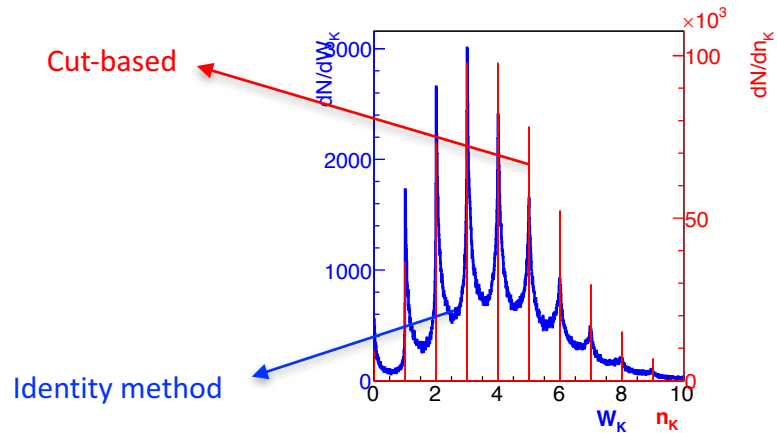
- Inner Tracking System (ITS) → Tracking and vertexing
- Time Projection Chamber (TPC) → Tracking and Particle Identification (PID)
- Time Of Flight (TOF) → Tracking and PID
- V0 → Centrality determination

Data Set:

- $\sqrt{s_{NN}} = 5.02$ TeV, ~ 78 M events
- $\sqrt{s_{NN}} = 2.76$ TeV, ~ 13 M events

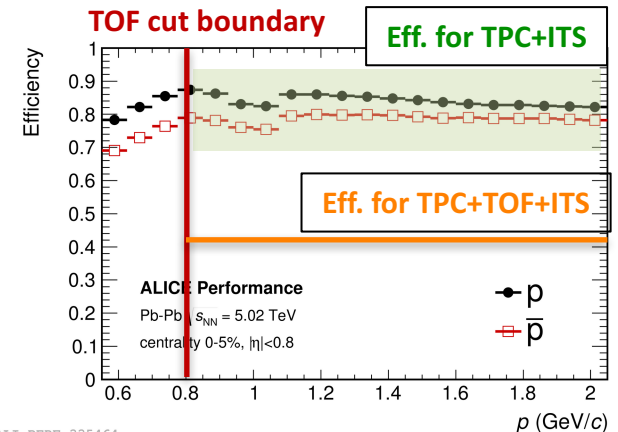


Identity method vs cut-based approach



$$\langle N_j^n \rangle = A^{-1} \langle W_j^n \rangle$$

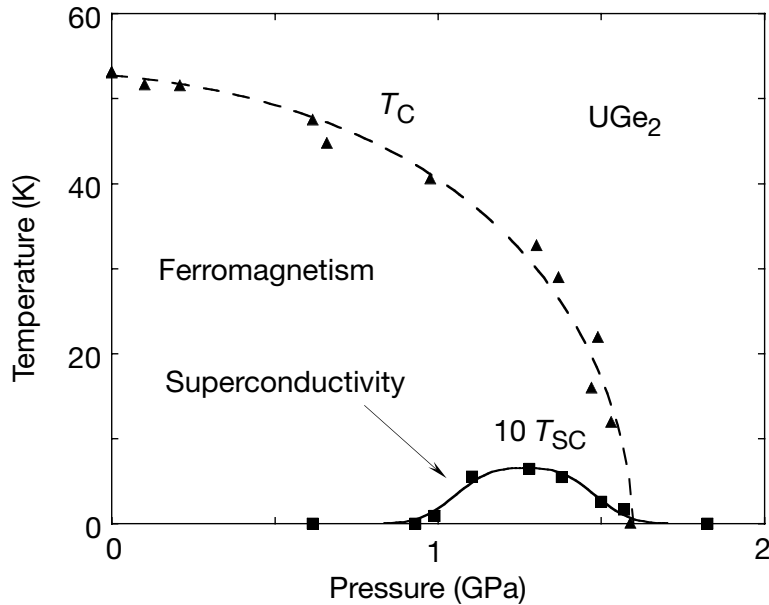
- **Identity Method**
 - Gives folded multiplicity distribution
 - **Maximal efficiency & no PID contamination**
- **Cut based approach**
 - Additional detector || reject a given phase space
 - **Low efficiency & PID contamination**



ALI-PERF-335464

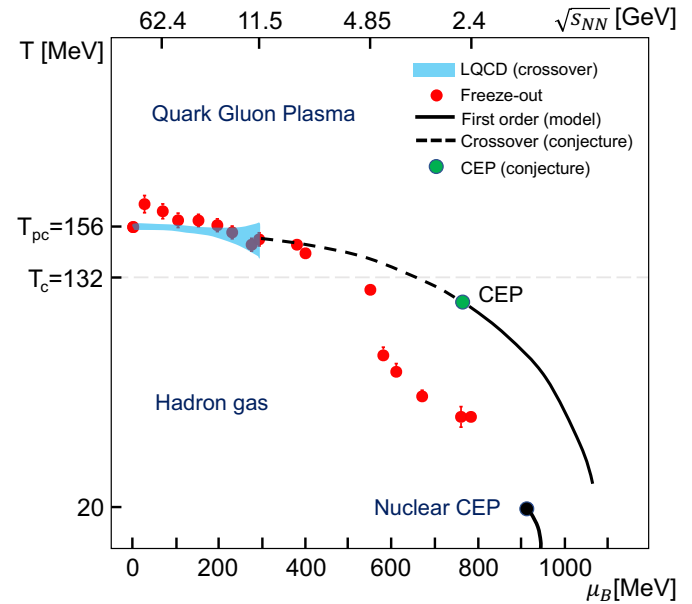
Phase transition

Ferromagnetic phase transition (Electro-magnetic interaction)



Nature volume 406, pages 587–592 (2000)

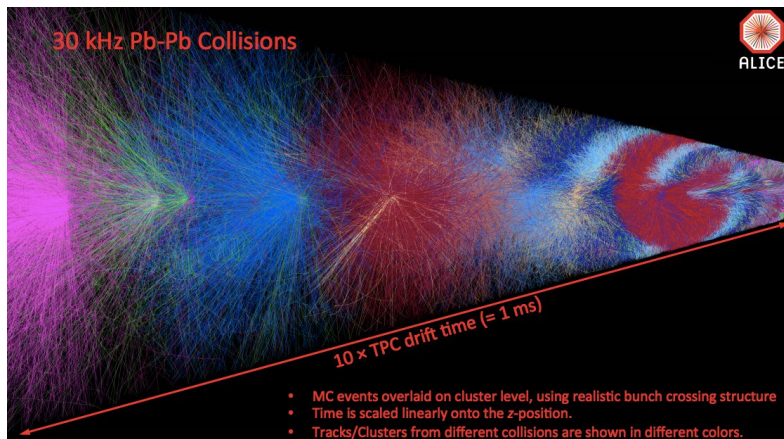
QCD phase diagram (Strong interaction)



P. Braun-Munzinger, A. Rustamov, J. Stachel, e-Print: 2211.08819

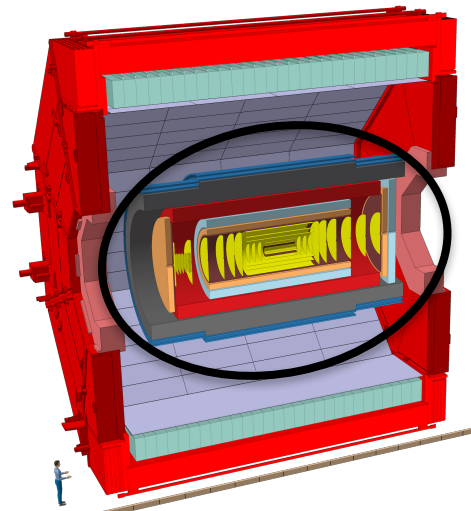
Future of ALICE

ALICE 2 (2022-2030)



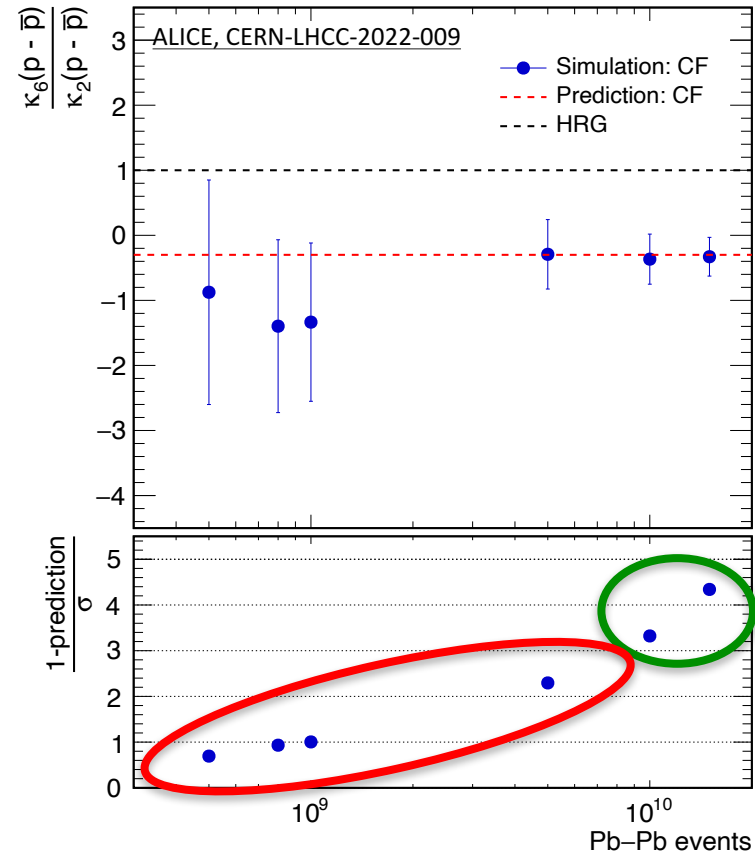
- ✓ **Continuous readout:**
→ ~ 50kHz Pb-Pb min. bias
→ ~ 5 pileup events within the TPC
- ✓ **Improved vertexing**
- ✓ **High tracking efficiency at low p_T**

ALICE 3 (beyond early 2030s)



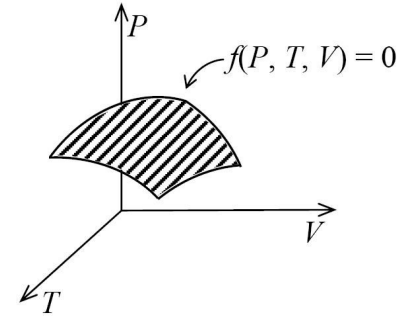
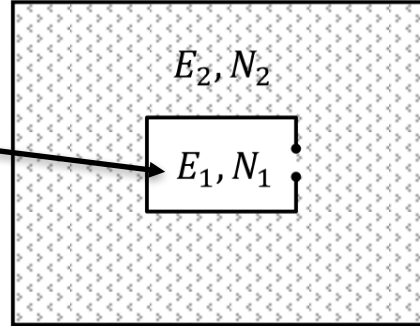
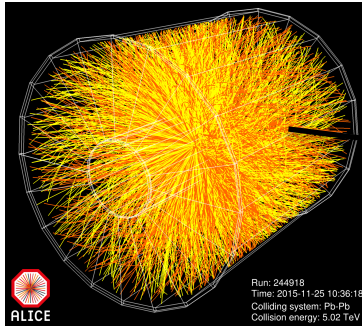
- ✓ **High statistics** → O (10^9) billion events
- ✓ **Large acceptance** → $|\eta| < 4$
- ✓ **High PID purity** → $0.3 < p_T < 10$ GeV/c
- ✓ **High efficiency** → ~95%
- ✓ **Excellent vertexing** → O ($3\mu\text{m}$) resolution

Criticality search in ALICE 2 and 3



- Simulation of the Critical Fluctuations (CF) is based on PQM model [G. A. Almasi, B. Friman, and K. Redlich, Phys. Rev.D96 \(2017\), 014027](#)
- **ALICE 2:**
→ More than 5 billion central Pb-Pb collisions is required
- **ALICE 3:**
→ **x3 larger statistics:** $>4\sigma$ significance with ALICE 2 acceptance

What kind of a system we are talking about?



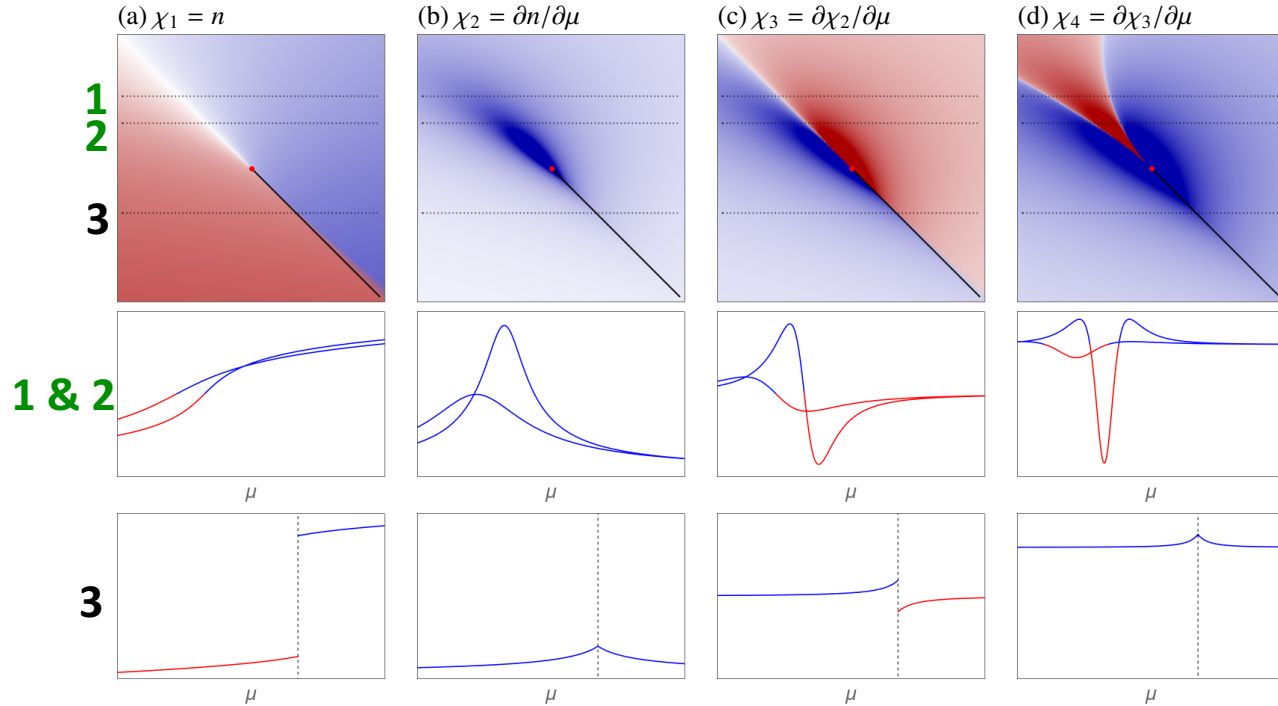
Grand canonical ensemble where particles are in a thermal equilibrium

- Energy (E) and number of particles (N) are **not conserved** in each microstate
- EOS can be represented **by a surface** in the state space spanned by P , V and T
- Conservation laws are applied **on average**
- Chemical potential (μ_B), Volume (V) and Temperature (T) are constant
- For a given state E_j and N_j **grand canonical partition function**

$$Z_{GCE}(T, V, \mu) = \sum_j \exp\left[-\frac{E_j - \mu N_j}{T}\right] \quad \rightarrow \quad \langle N \rangle = \sum_j N_j p_j = T \left. \frac{\partial \ln Z_{GCE}}{\partial \mu} \right|_V$$

Thermodynamic susceptibilities

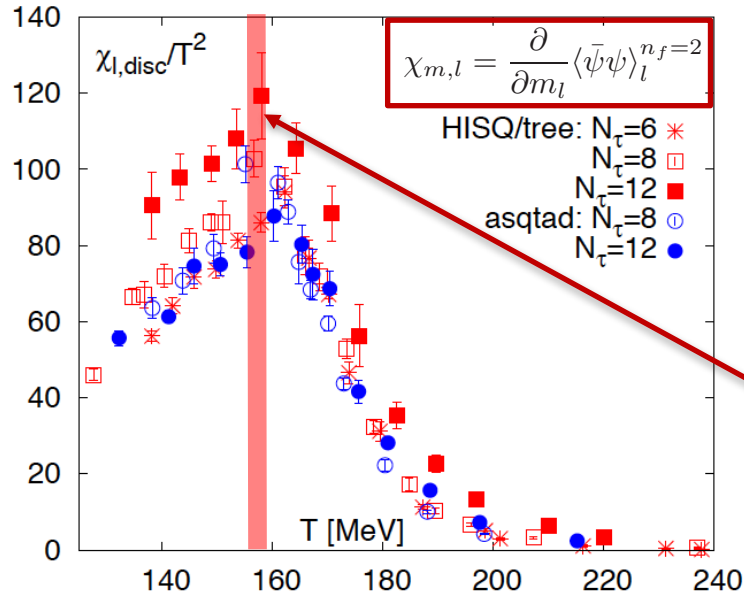
$$\langle N \rangle = \sum_j N_j p_j = T \frac{\partial \ln Z_{GCE}}{\partial \mu} \Big|_V \quad \Rightarrow \quad n \equiv \frac{\langle N \rangle}{V} = \left(\frac{\partial P}{\partial \mu} \right)_T \quad \Rightarrow \quad \chi_k = \left(\frac{\partial^k P}{\partial \mu^k} \right)_T = \left(\frac{\partial^{k-1} n}{\partial \mu^{k-1}} \right)_T$$



Chiral susceptibility: sum of connected and disconnected Feynman diagrams

Free energy density 2-flavor light quark chiral condensate

$$f = -\frac{T}{V} \ln Z \quad \langle \bar{\psi}\psi \rangle_l^{n_f=2} = \frac{T}{V} \frac{\partial \ln Z}{\partial m_l}$$

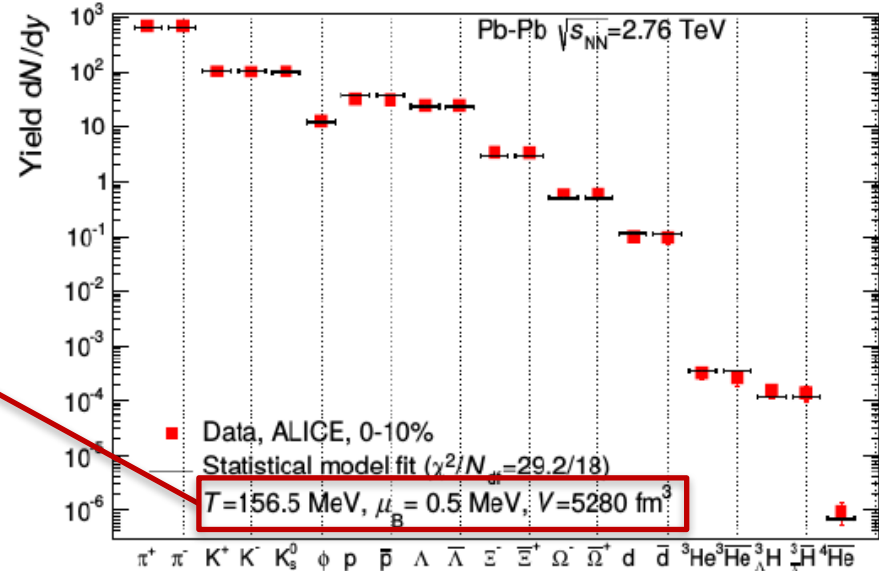


“The disconnected part of the light quark susceptibility describes the fluctuations in the light quark condensate”

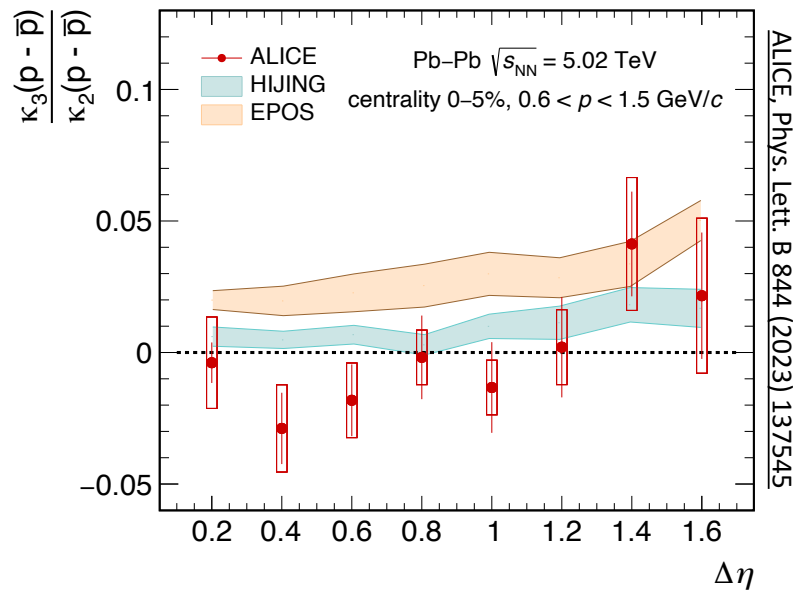
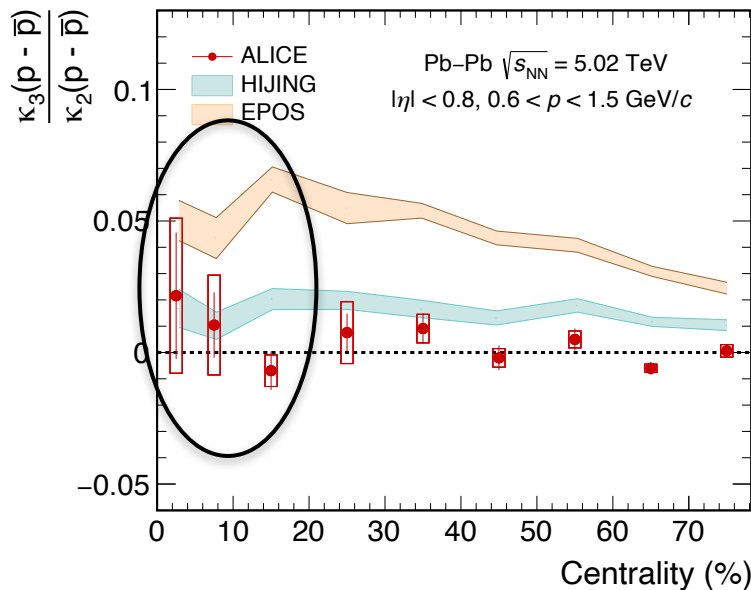
$$\langle N_i \rangle = V \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp[(E_i - \mu_i)/T] \pm 1}$$

$$\mu_i = \mu_B B_i + \mu_S S_i + \mu_I I_i$$

$$\chi^2 = \sum_{k=1}^n \frac{(\langle N_k^{\text{exp}} \rangle - \langle N_k^{\text{HRG}} \rangle)^2}{\sigma_k^2}$$



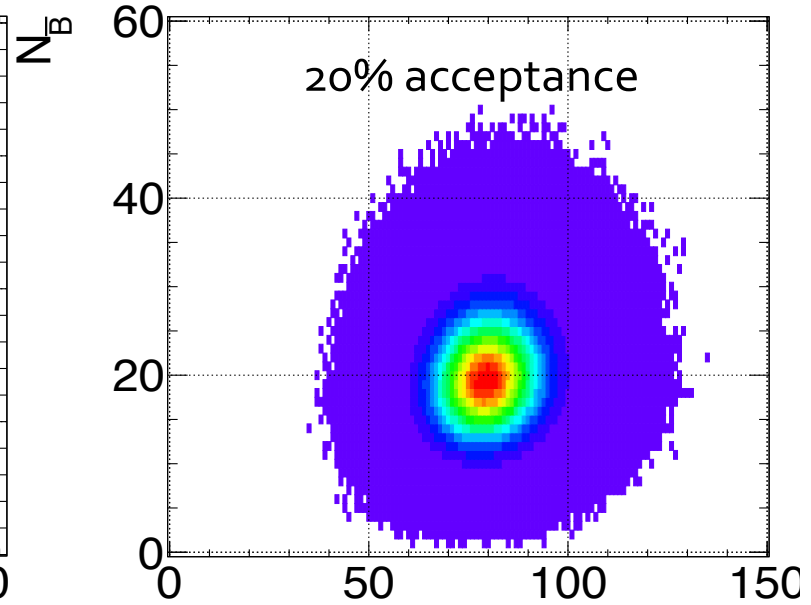
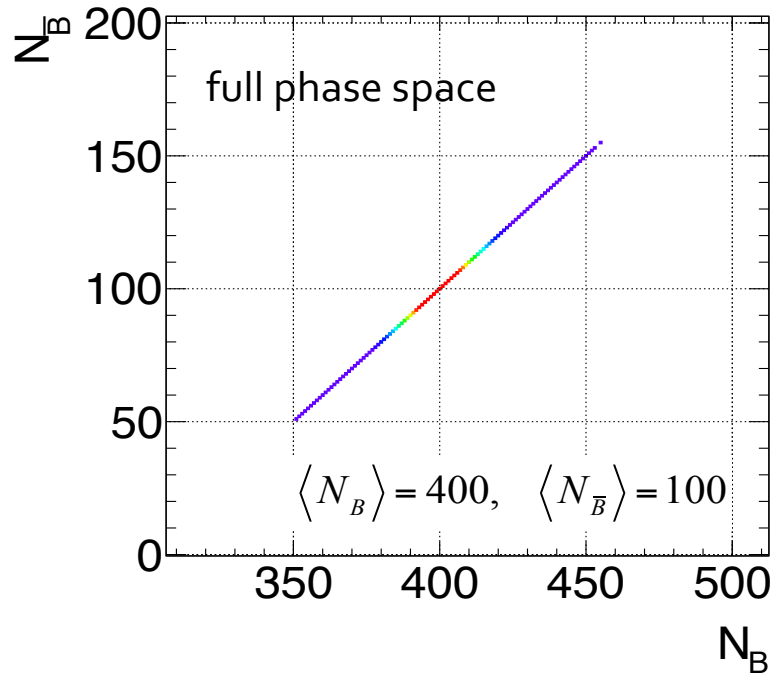
3rd order cumulants of net-p



- **Data agree with Skellam baseline "0"** → μ_B is very close to 0 (ALICE Collaboration, arXiv:2311.13332v2)
- **EPOS and HIJING deviate from "0"**
 - They conserve global charge but $\mathbf{p/\bar{p}}$ deviates from unity: 1.025 ± 0.004 (EPOS), 1.008 ± 0.002 (HIJING)
 - **Volume fluctuations** for 2nd and 3rd order cumulants are not negligible

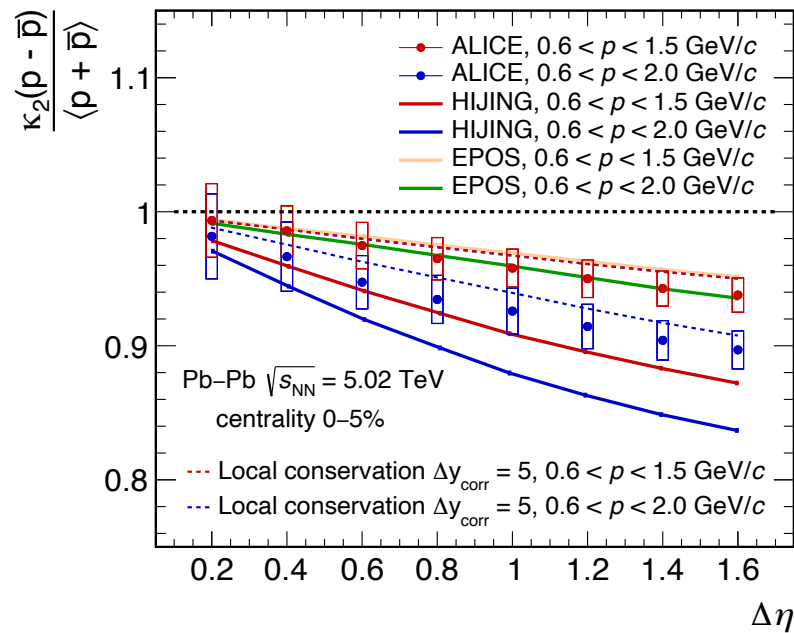
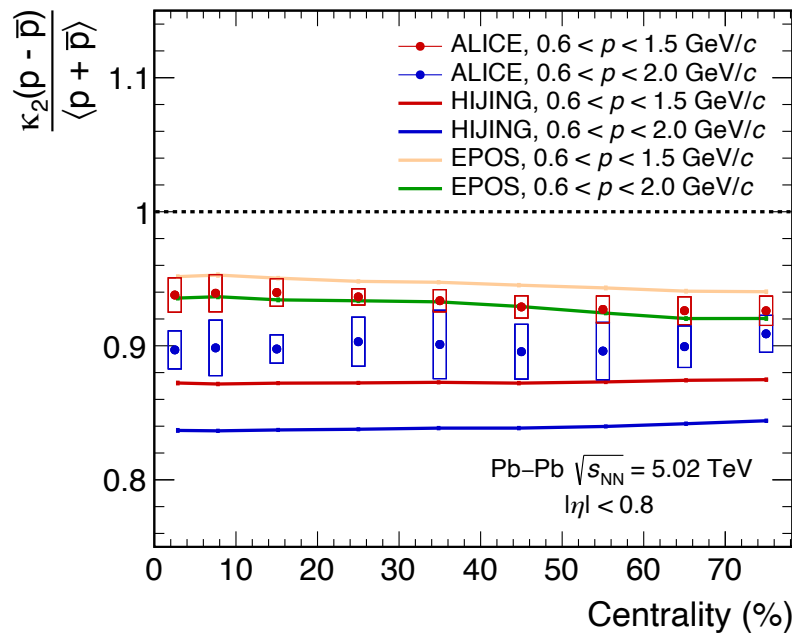
Acceptance effect

Importance of acceptance



P. Braun-Munzinger, A. Rustamov, J. Stachel, QM18, NPA 982 (2019) 307-310

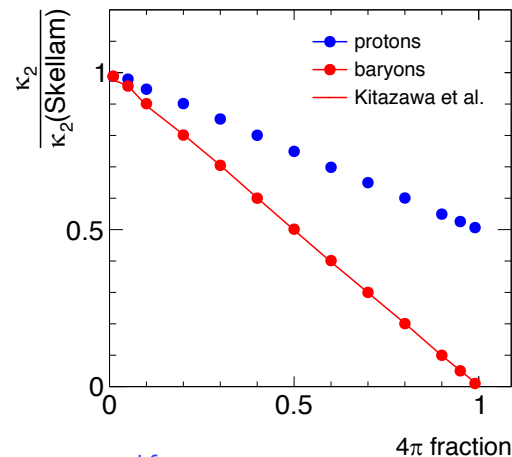
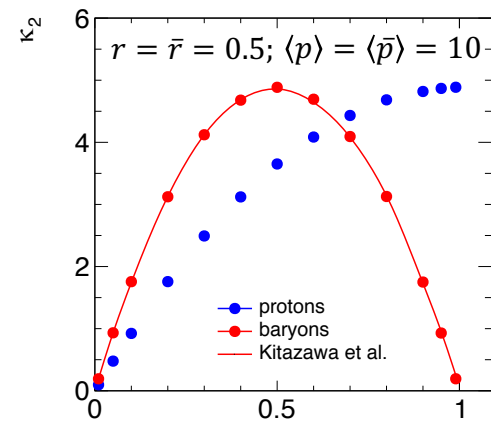
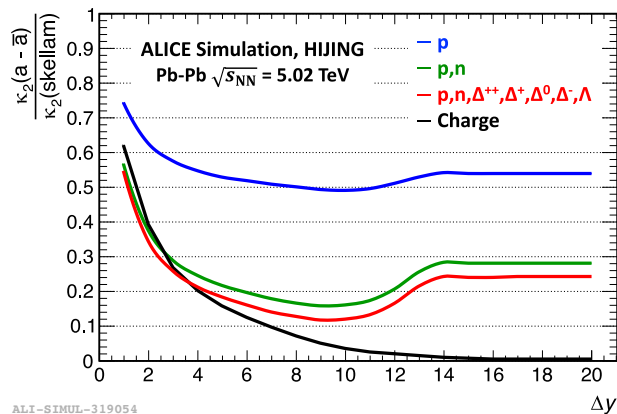
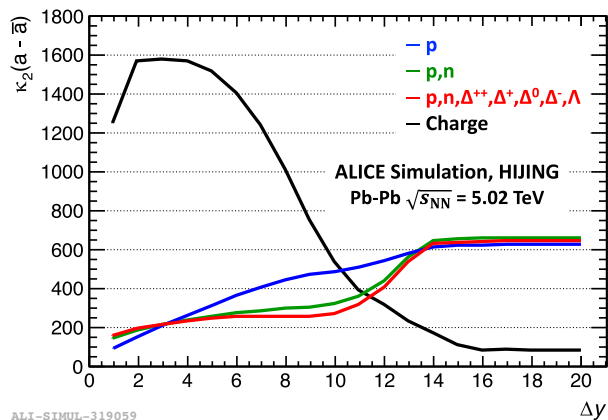
2nd order cumulants of net-p: Acceptance dependence



- Consistent with the baryon number conservation picture
 - Increase in fraction of accepted $p, \bar{p} \rightarrow$ stronger constraint of fluctuations due to baryon number conservation
- EPOS & HIJING show this drop qualitatively

2nd order cumulants in full phase space

- **Net-baryon vs Net-p**
- Due to **isospin randomization** at $\sqrt{s_{NN}} > 10$ GeV net-baryon fluctuations can be easily obtained from corresponding **net-proton measurements**
M. Kitazawa, and M. Asakawa, Phys. Rev. C86 (2012)

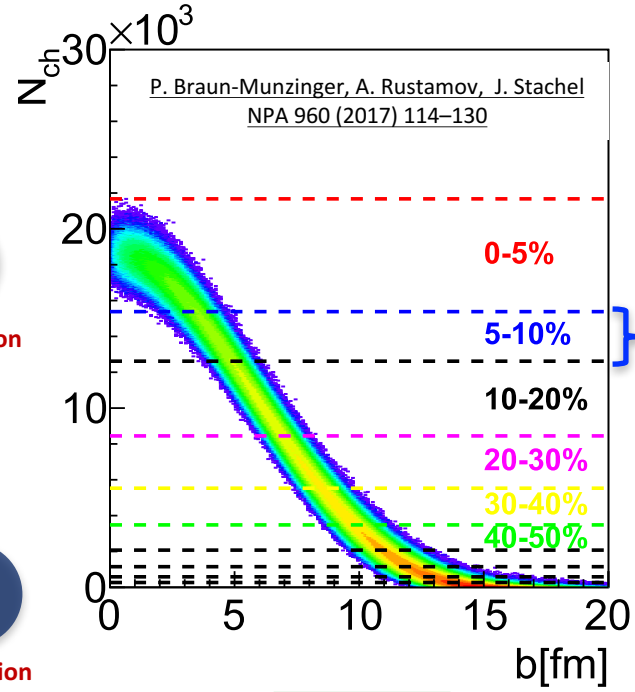


P. Braun-Munzinger, A. Rustamov, J. Stachel, NPA 982 (2019) 307-310

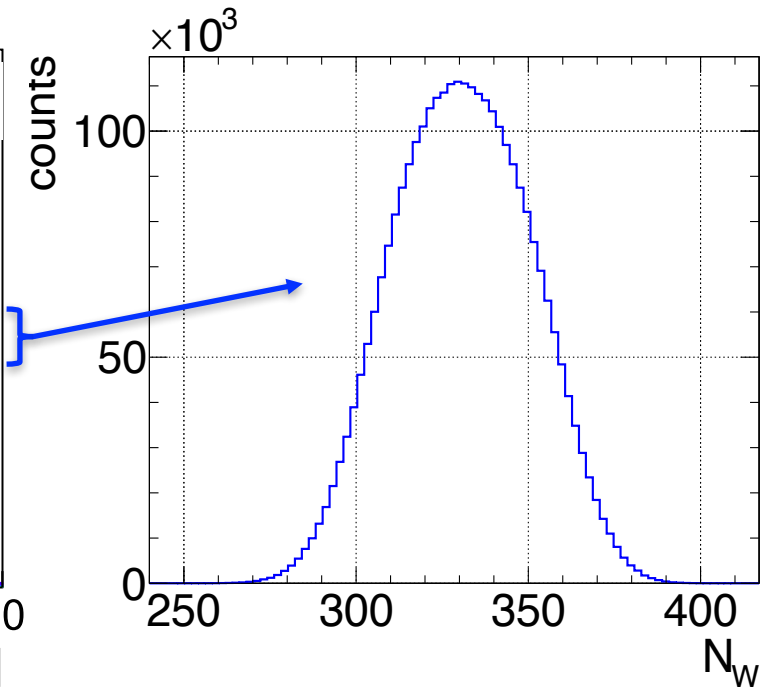
Experimental Effects

Volume fluctuations

Experiment



Theory

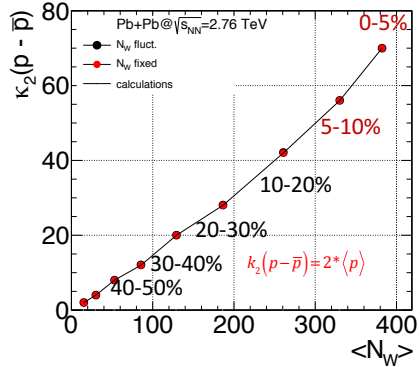


Volume fluctuations: TOY model at LHC

2nd order cumulants

Net-p

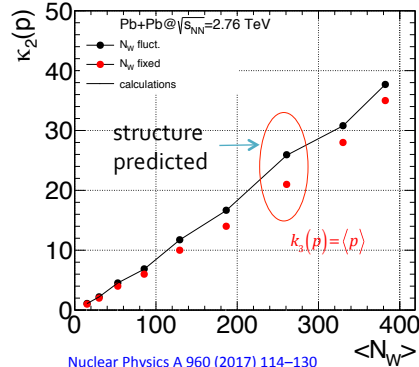
150*10⁶ Events



$$k_2(p-\bar{p}) = \langle N_w \rangle k_2(n-\bar{n}) + \langle n-\bar{n} \rangle^2 k_2(N_w)$$

↓
vanishes for ALICE

p



$$k_2(p) = \langle N_w \rangle k_2(n) + \langle n \rangle^2 k_2(N_w)$$

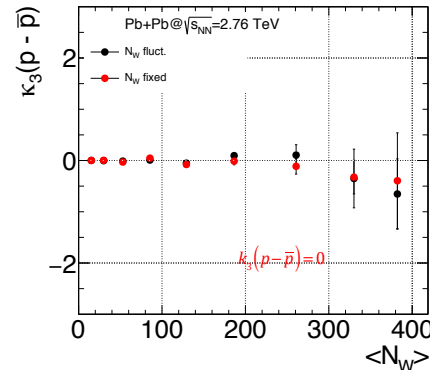
↓
does not vanish

$n, \bar{n} \rightarrow$ from single wounded nucleon

3rd order cumulants

Net-p

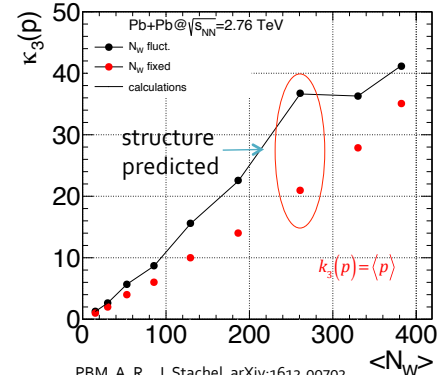
150*10⁶ Events



$$k_3(p-\bar{p}) = \langle N_w \rangle k_3(n-\bar{n}) + \langle n-\bar{n} \rangle (\dots)$$

↓
vanishes for ALICE

p



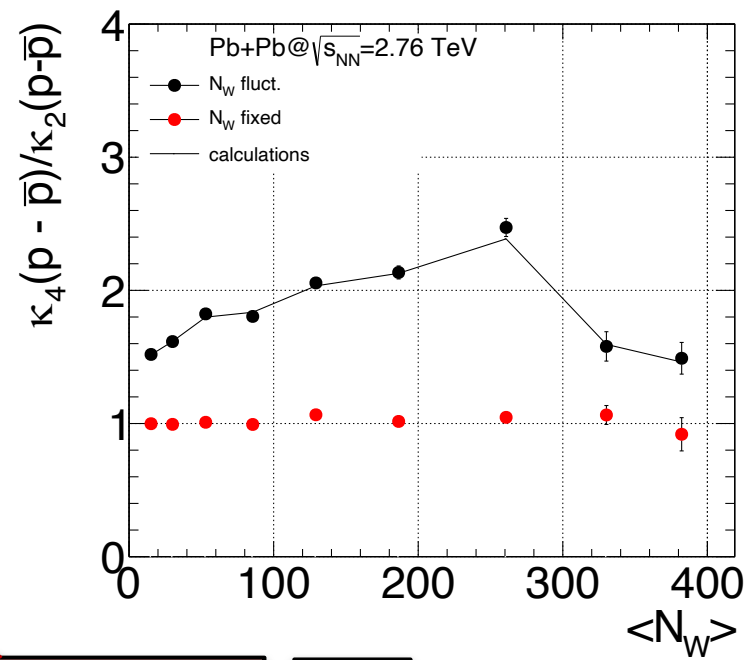
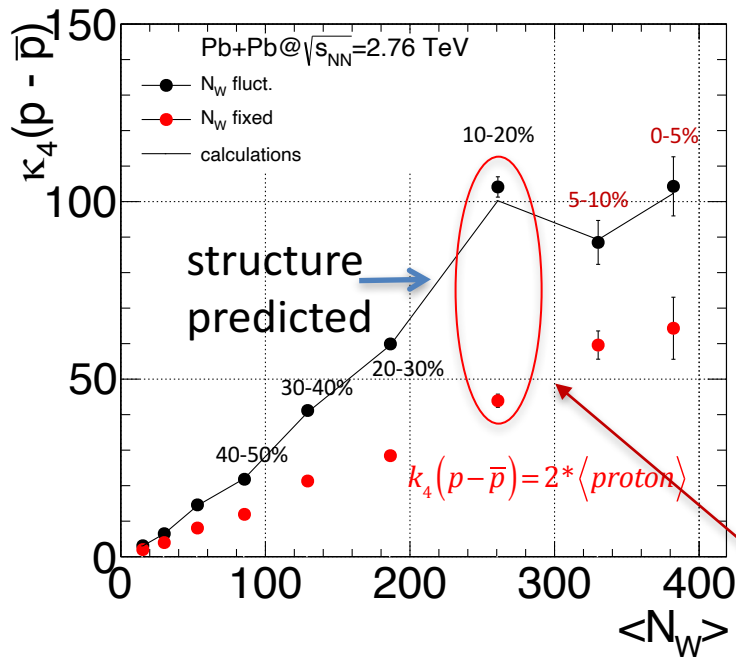
$$k_3(p) = \langle N_w \rangle k_3(n) + \langle n \rangle (\dots)$$

↓
does not vanish

PBM, A. R., J. Stachel, arXiv:1612.00702

Volume fluctuations: TOY model at LHC

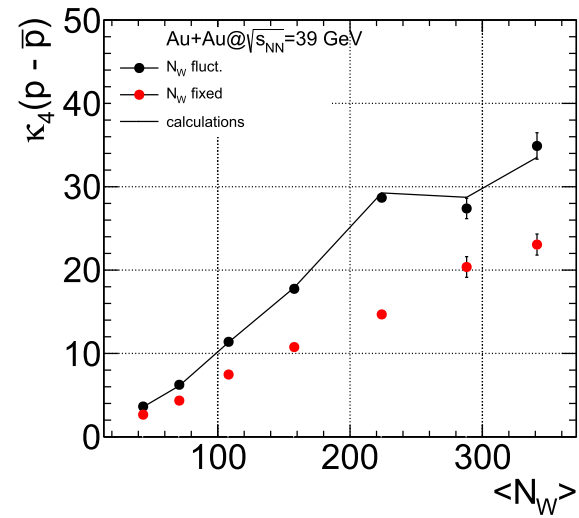
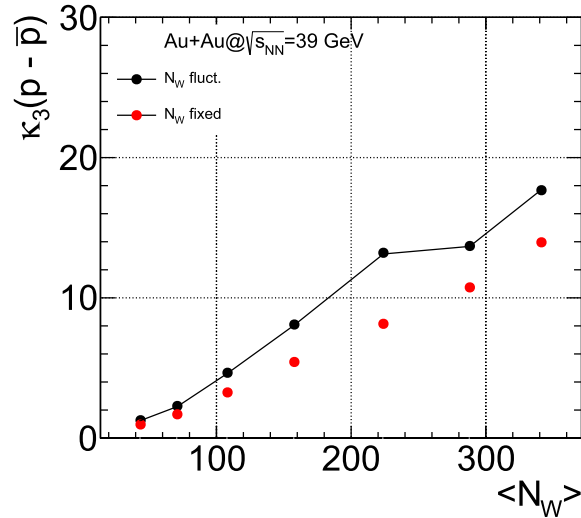
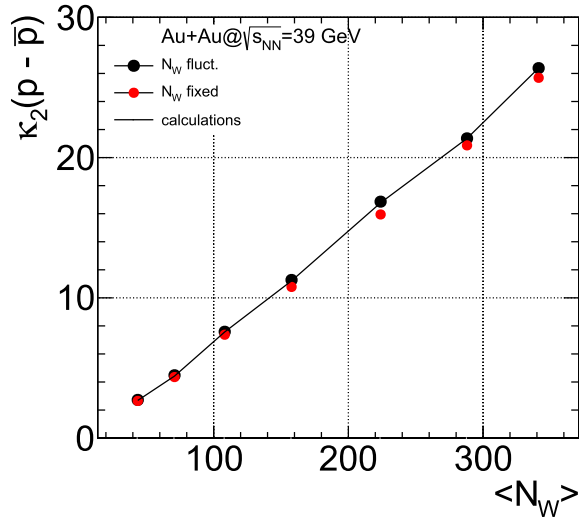
150*10⁶ Events



$$k_4(p - \bar{p}) = \langle N_w \rangle k_4(n - \bar{n}) + \boxed{3k_2(n - \bar{n})^2 k_2(N_w)} + \boxed{\langle n - \bar{n} \rangle} (\dots)$$

Vanishes at LHC

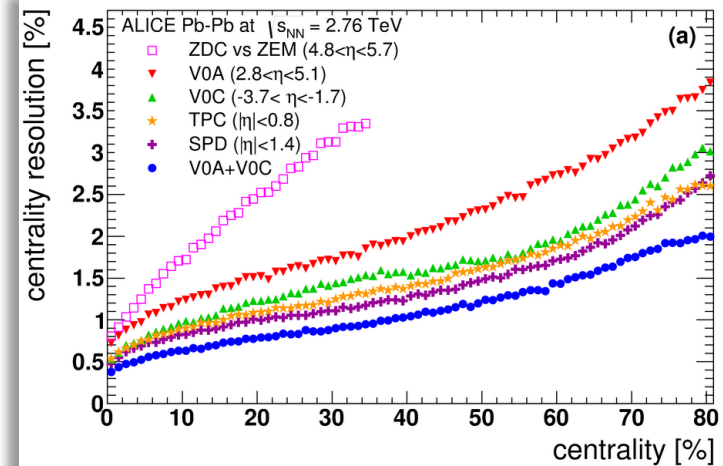
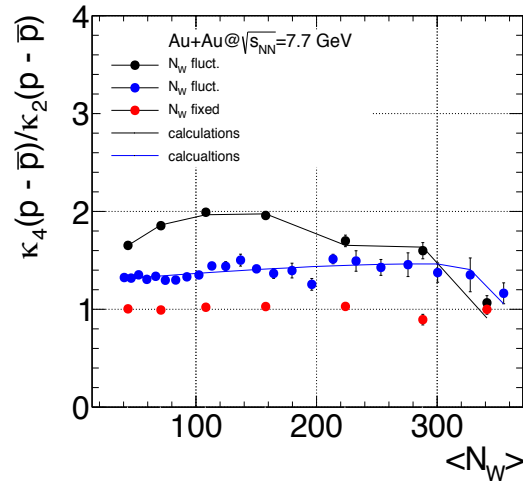
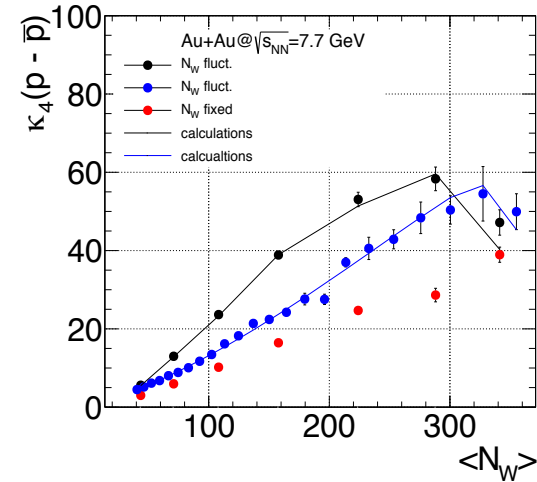
Volume fluctuations: TOY model at RHIC



$$k_4(p - \bar{p}) = \langle N_w \rangle k_4(n - \bar{n}) + 3k_2(n - \bar{n})^2 k_2(N_w) + \langle n - \bar{n} \rangle (\dots)$$

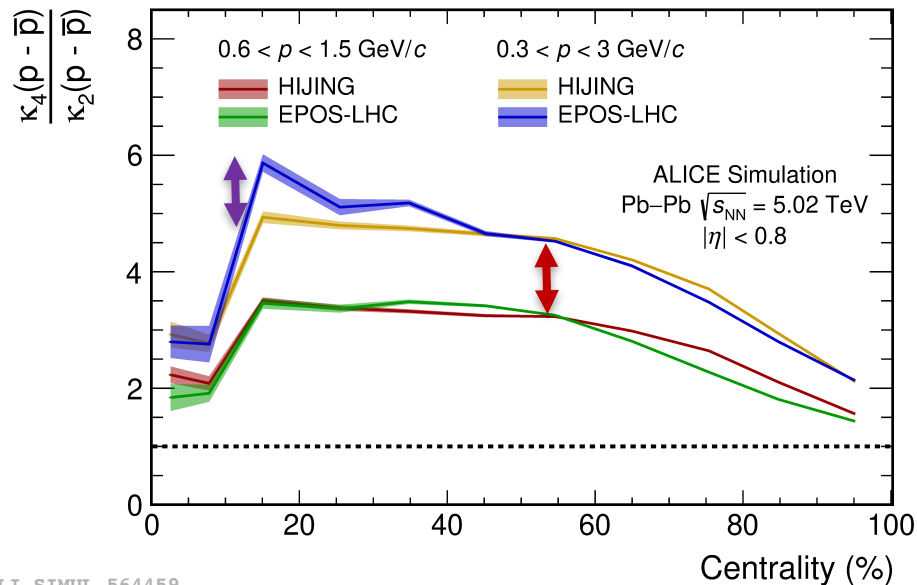
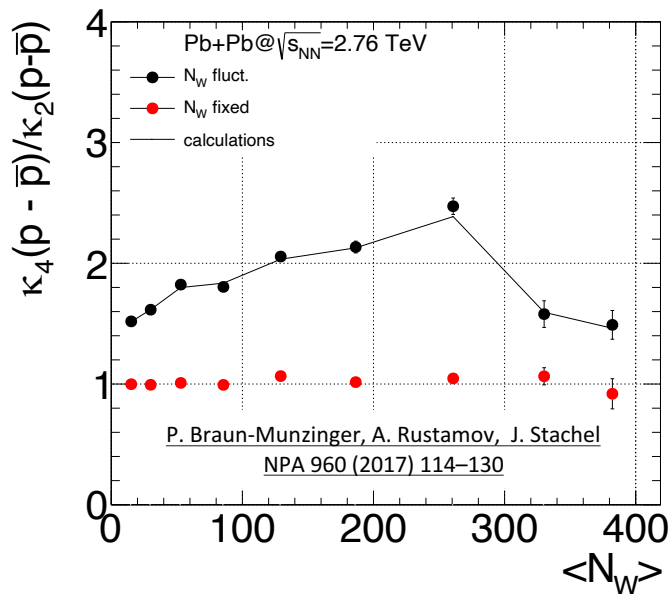
➤ At lower energies **none of these terms cancel**

Volume fluctuations: CBWC vs centrality resolution



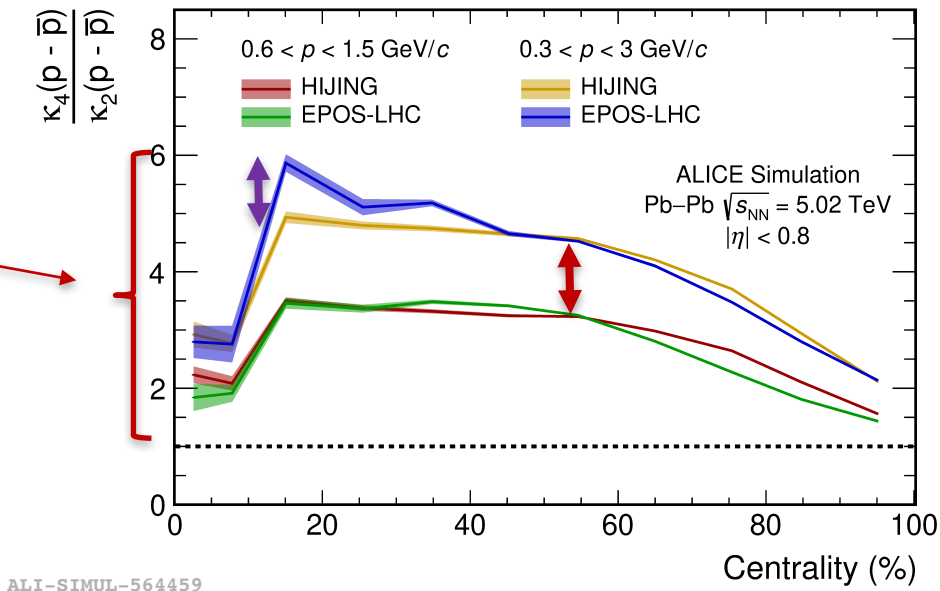
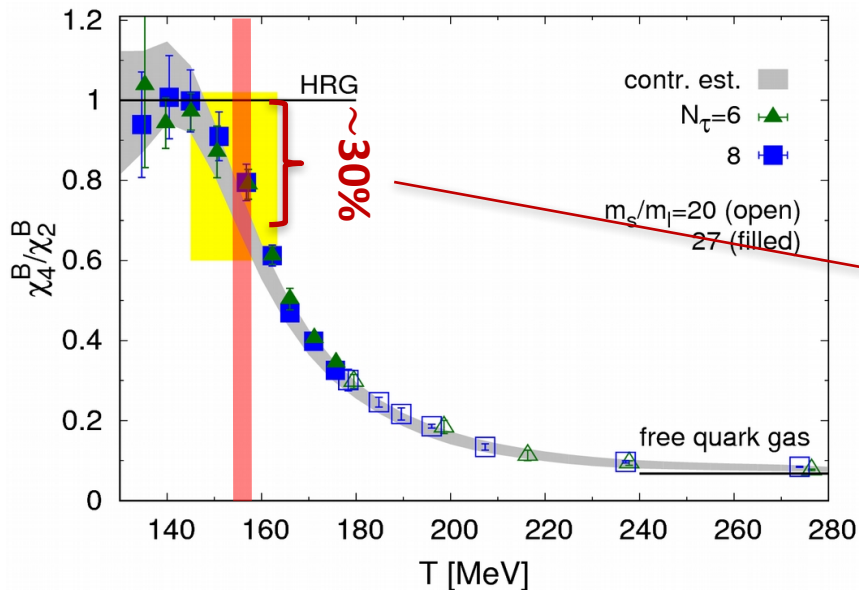
Centrality dependent resolution or centrality bias → Can this have an impact on the performance of CBWC

Volume fluctuations at LHC energies



- For the 2nd and 3rd order cumulants it cancels out at LHC
- Strongly depends on the particle multiplicity within the **kinematic acceptance** and the **underlying physics**

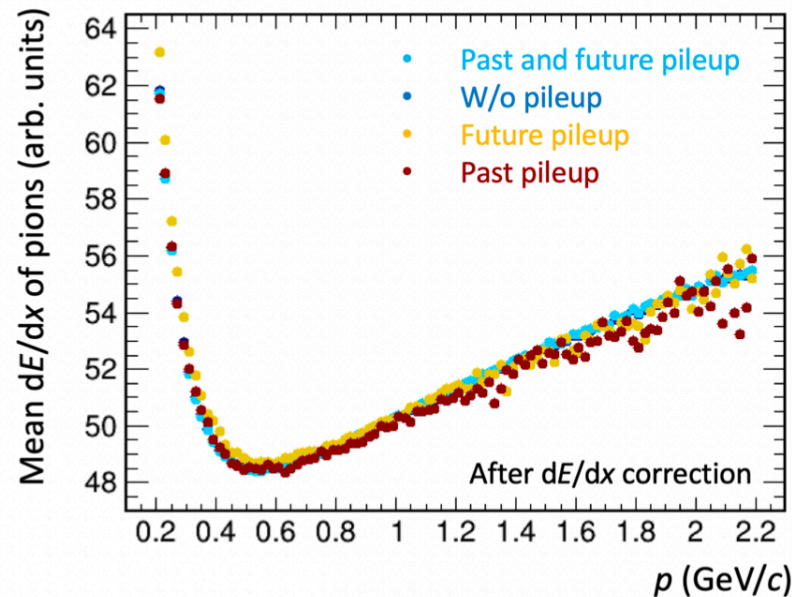
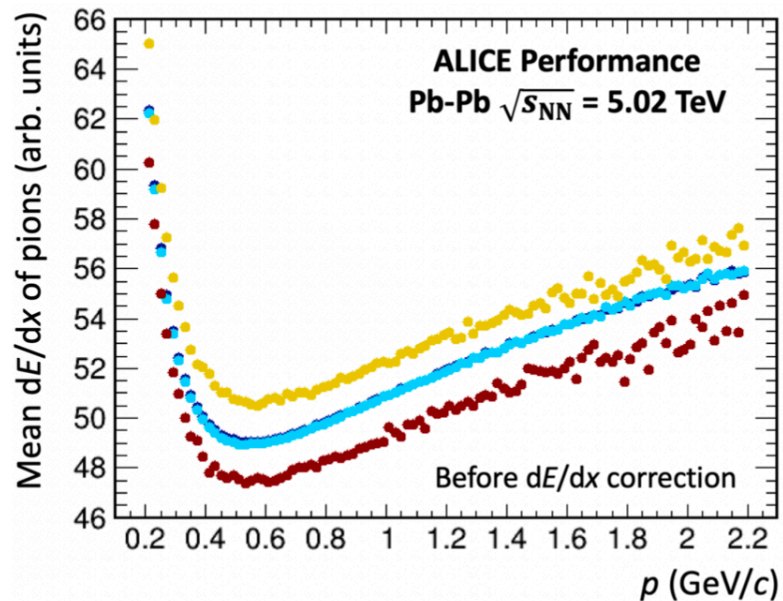
Volume fluctuations at LHC energies



ALI-SIMUL-564459

- For the 2nd and 3rd order cumulants it cancels out at LHC
- Strongly depends on the particle multiplicity within the **kinematic acceptance** and the **underlying physics**
- **LQCD expectation** → for the 4th order the effect can be more than **an order of magnitude larger than the signal**
- **Ultimate solution** → R. Holzmann, V. Koch, A. Rustamov, J. Stroh arXiv:2403.03598

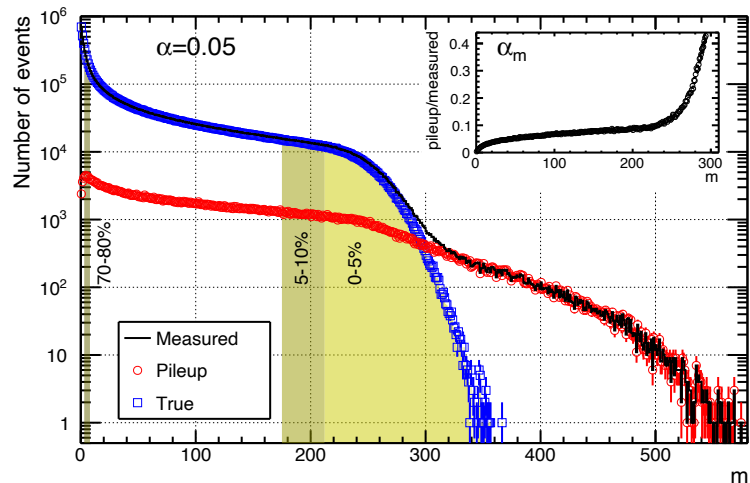
Experimental challenges: E.g. effect of event pileup



Effect of in-bunch pileup

Y. Zhang, Y., T. Nonaka, X. Luo, arXiv:2108.10134

T. Nonaka, M. Kitazawa, S. Esumi, Nucl.Instrum.Meth. A984 (2020)



➤ In-bunch pileup

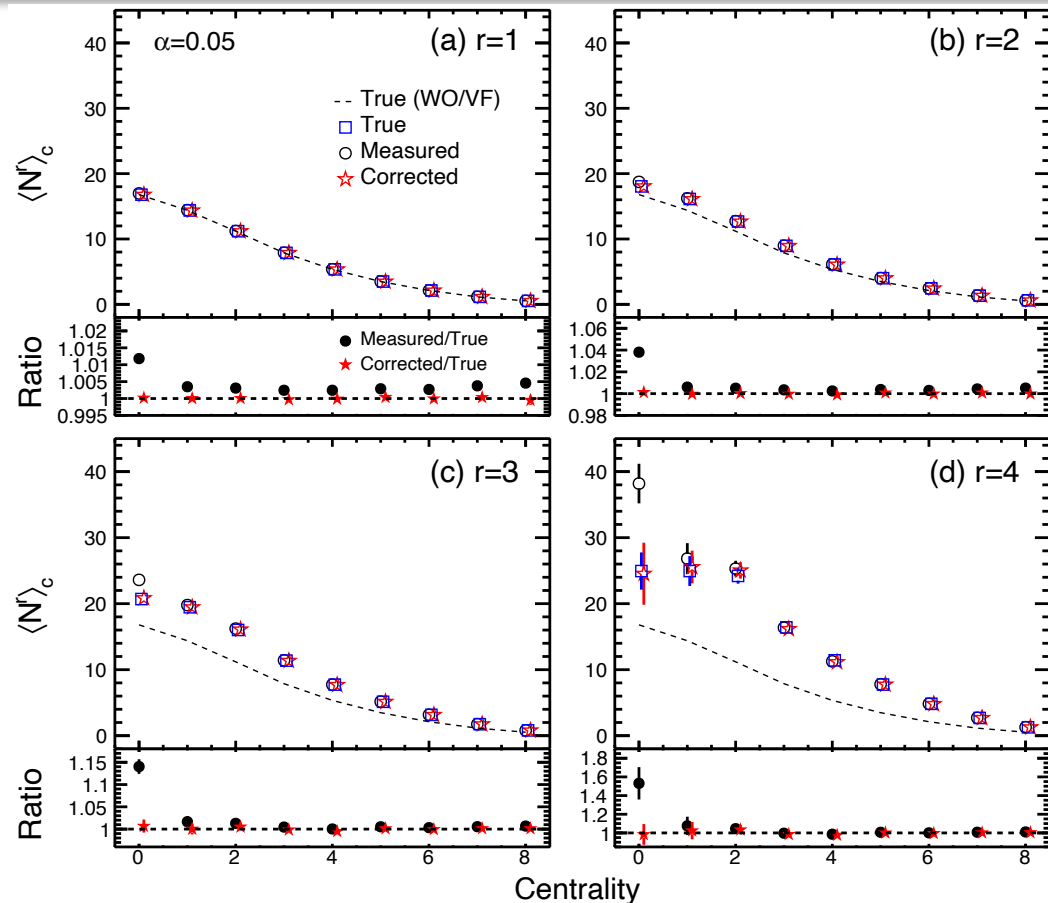
→ Significant impact on the higher order cumulants

→ **Less than 0.1% → negligible**

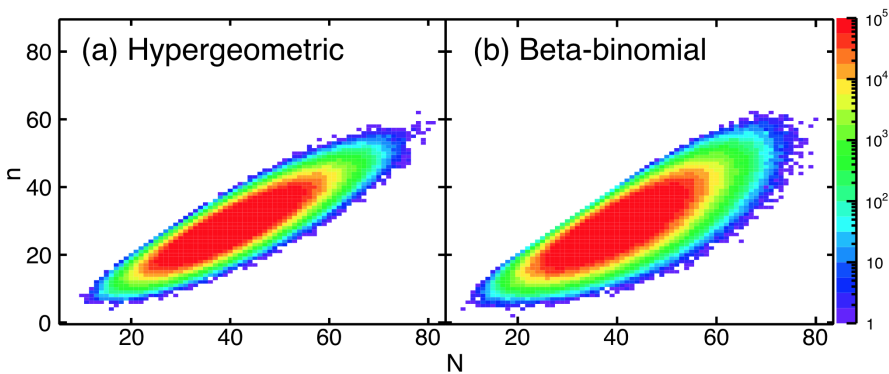
➤ Out-of-bunch pileup

→ Significant impact on the detector response

→ **Effect is corrected to a large extent**



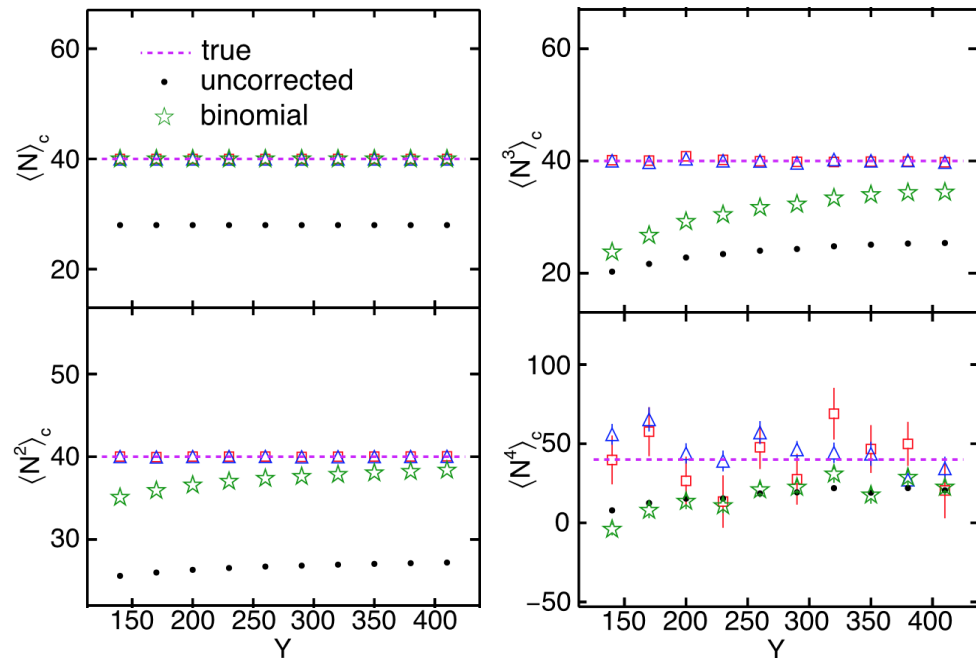
What if efficiency loss is not binomial?



Draw N balls from the urn without returning balls to the urn

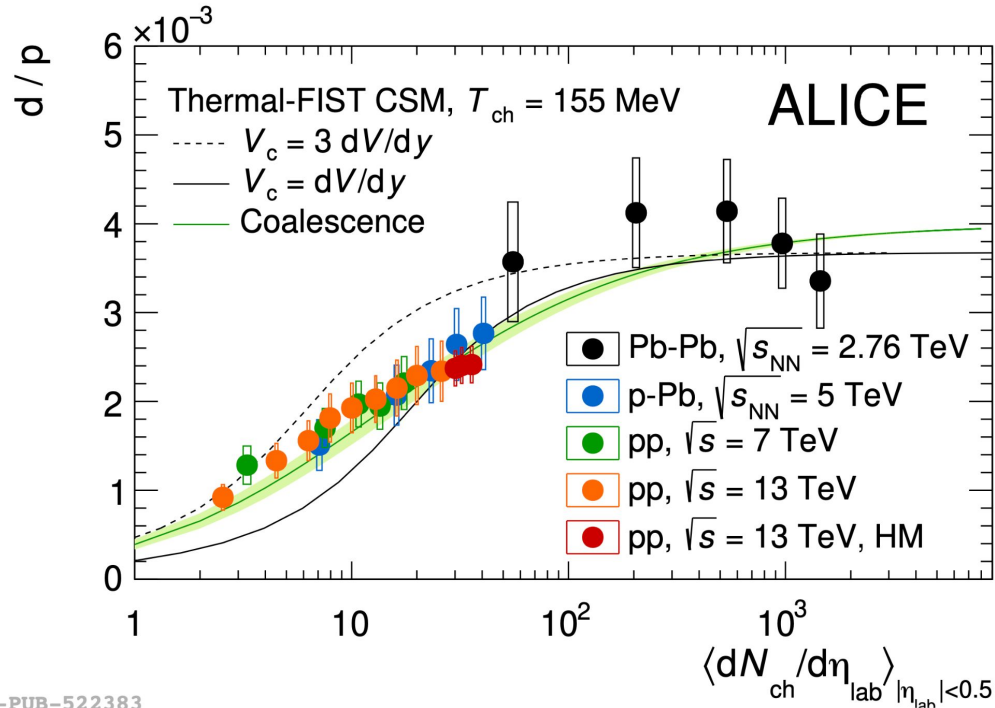
In each draw, when one draws a white ball, two white balls are returned to the urn

Hypergeometric



T. Nonaka, M. Kitazawa, S. Esumi, Nucl.Instrum.Meth. A906 (2018) 10-17
 T. Nonaka, M. Kitazawa, S. Esumi, Phys. Rev. C 95, 064912 (2017)
 Adam Bzdak, Volker Koch, Phys. Rev. C86, 044904 (2012)

Light nuclei production



Reduction in small systems due either to
baryon conservation (CSM) or to source vs. deuteron size (coalescence)

Correlation and cumulant of net-particles

Charged kaons and Ξ baryons

- Same- and opposite-charge correlations \rightarrow 2 species
- **No autocorrelation**
 - Negligible resonance feeddown
- Negligible uncorrelated weak feeddown from Ω
- **Experimentally** \rightarrow high purity via PID (K) and machine learning selections (Ξ)

Net-kaon net-xi correlation

- Includes both same and opposite strangeness
- Cancellation of initial volume fluctuation

A. Rustamov et al., Nucl. Phys. A 960 (2017) 114-130

$$\rho(\Delta\Xi, \Delta K) = \kappa_{11}(\Delta\Xi, \Delta K) / \sqrt{(\kappa_2(\Delta\Xi)\kappa_2(\Delta K))}$$

with $\Delta\Xi = \Xi^+ - \Xi^-$ and $\Delta K = K^+ - K^-$

$$\kappa_{11}(\Delta\Xi, \Delta K) = \kappa_{11}(\Xi^+, K^+) + \kappa_{11}(\Xi^-, K^-) - \kappa_{11}(\Xi^-, K^+) - \kappa_{11}(\Xi^+, K^-)$$

$$\kappa_2(\Delta n) = \kappa_2(n^+) + \kappa_2(n^-) - 2\kappa_{11}(n^+, n^-)$$

Net-xi cumulant ratio

- E-by-e fluctuations of $\Delta\Xi$ multiplicity distribution

$$\kappa_2 / \kappa_1(\Delta\Xi) = \kappa_2(\Delta\Xi) / \kappa_1(\Xi^+ + \Xi^-)$$

Canonical statistical model

