# Regge approach to light meson photoproduction

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Spectroscopy analyses

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- Understand production mechanisms  $\rightarrow$ 
  - **Reggeization of pion exchange**
  - **Double Regge exchange** •





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#### [T. Regge, Nuovo Cim. 18 (1960) 947-956]

#### Partial wave expansion

$$A(s,t) = \sum_{\ell=0}^{\infty} (2\ell+1) P_{\ell}(z_t) f_{\ell}(t)$$

#### Sommerfeld-Watson transform

$$A(s,t) = -\frac{1}{2i} \int_{C} d\ell \, \frac{(2\ell+1) \, P_{\ell}(-z_t) \, f(\ell,t)}{\sin \pi \ell}$$



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#### Deform the contour (assuming the partial waves are analytic, only singularities are poles)



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[T. Regge, Nuovo Cim. 18 (1960) 947-956]

Scattering amplitudes are analytic in s and  $t \longrightarrow$ 

## $f_{\ell}(t) = \int \frac{\mathrm{d}z}{2} P_{\ell}(z) A(z,t) \sim \frac{\beta(t)}{\ell - \alpha(t)}$

#### Resonances appear simultaneously as poles in energy and spin!

- Regge trajectories: families with same quantum numbers but different spin
- Almost straight lines (Chew-Frautschi plot)
- In standard Regge theory parameterized by:  $\alpha(t) = \alpha' t + \alpha_0$



Partial waves must be analytic in angular momentum

[V.Mathieu et al., Phys.Rev.D 98 (2018) 1, 014041]

[T. Regge, Nuovo Cim. 18 (1960) 947-956]

 $\pi$ 

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#### **Resonances appear simultaneously as poles in energy and spin!**

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## When do we use Regge theory?





#### Model for diffractive production

 We only need to know the (dominant) crossed-channel exchanges

## Photoproduction of the hybrid $\pi_1(1600)$



Lightest isoscalar with  $J^{PC} = 1^{-+}$ 

Predicted by lattice QCD

Experimental evidence from COMPASS)



## Photoproduction of the hybrid $\pi_1(1600)$





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## **Understanding pion exchange**

[GM, Daniel Winney, et al. (JPAC), Phys. Rev. D 110 (2024) 11, 114012]

Simplest charge-exchange process is pion photoproduction

Pion exchange diagram vanishes in the *t*-channel CM frame

In terms of Born diagrams, **gauge invariance** relates *t*-channel diagram (pion exchange) and *s*-, *u*-channel diagrams (nucleon exchanges)





## **Understanding pion exchange**

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#### What about the Reggeized pion?

$$A_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}(s,t) = \sum_{J} (2J+1) a_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}^{J}(t) \underbrace{d_{\lambda_{\gamma}\lambda_{i}-\lambda_{f}}^{J}(\theta_{t})}_{J \ge |\lambda_{\gamma}| = 1}$$

No pion pole?

#### [GM, Daniel Winney, et al. (JPAC), Phys.Rev.D 110 (2024) 11, 114012]



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## **Reggeization of pion exchange**

#### [GM, Daniel Winney, et al. (JPAC), Phys.Rev.D 110 (2024) 11, 114012]

1. Build an amplitude for the exchange of a particle of arbitrary spin J > 0 (gauge invariant by construction)

$$A^{J}_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}(s,t) = \sum_{\sigma_{J}} \frac{V^{J}_{\lambda_{\gamma}}(\sigma_{J}) V^{J}_{\lambda_{i}\lambda_{f}}(\sigma_{J})}{J - \alpha(t)} = a^{J}_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}(t) d^{J}_{\lambda_{\gamma}\lambda_{i} - \lambda_{f}}(\theta_{t})$$
$$\propto \frac{1}{\sqrt{J}}$$



## **Reggeization of pion exchange**

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- 2. Analytically continue to J = 0
  - Use the hypergeometric function



$$\begin{aligned} d^{J}_{\lambda_{\gamma},0}(\theta_{t}) \propto \sqrt{J} \\ A^{J \to 0}_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}(s,t) \propto \frac{t}{-\alpha(t)} (2\lambda_{i}\lambda_{\gamma}\delta_{\lambda_{i}\lambda_{f}}) \frac{z_{t}}{\sqrt{1-z_{t}}} &\approx i \frac{t}{m_{\pi}^{2}-t} (2\lambda_{i}\lambda_{\gamma}\delta_{\lambda_{i}\lambda_{f}}) \quad \text{The spin } J \to 0 \text{ amplitude is finite!} \end{aligned}$$

 $\propto \frac{1}{\sqrt{J}}$ 

## **Reggeization of pion exchange**

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1. Build an amplitude for the exchange of a particle of arbitrary spin J > 0 (gauge invariant by construction)

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- 2. Analytically continue to J = 0
  - Use the hypergeometric function



3. Sum the tower of exchanges (e.g. Sommerfeld-Watson transform, or using the generating function for the Jacobi polynomials)

 $\propto \frac{1}{\sqrt{J}}$ 

$$A_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}(s,t) = A_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}^{J \to 0}(s,t) + \sum_{J=1} (2J+1) a_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}^{J}(t) d_{\lambda_{\gamma}\lambda_{i}-\lambda_{f}}^{J}(\theta_{t}) \propto t(sR^{2})^{\alpha(t)}$$

 $\pi, \pi_2, \pi_4 \ldots$ 

n

## **Results for pion photoproduction**

[GM, Daniel Winney, et al. (JPAC), Phys.Rev.D 110 (2024) 11, 114012]

#### **Reggeized pion exchange**

 $A^{\text{Regge}}_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}(s,t) \propto t(sR^{2})^{\alpha(t)}$ 



## **Results for pion photoproduction**

#### **Reggeized pion exchange**

 $A^{\text{Regge}}_{\lambda_{\gamma}\lambda_{i}\lambda_{f}}(s,t) \propto t(sR^{2})^{\alpha(t)}$ 



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#### Adding the nucleon magnetic term

- Gauge invariant by itself





#### Baryon resonances



#### Double Regge production







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[COMPASS, Phys.Lett.B 740 (2015) 303-311]



• Clear signals of the a0(980) and a2(1320)



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- Clear signals of the a0(980) and a2(1320) ٠
- Forward-backward asymmetry at high energies •



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[COMPASS, Phys.Lett.B 740 (2015) 303-311]

## Double Regge $\eta^{(\prime)}\pi$ at COMPASS



#### [L. Bibrzycki, C. Fernandez-Ramirez et al. (JPAC), Eur. Phys. J.C 81 (2021) 647]







## Double Regge model $\eta^{(\prime)}\pi$ photoproduction

1. Start from a vector-vector exchange model

$$A_{\lambda_{\gamma}\lambda\lambda'} = \sum_{\text{diagrams}} \left( \frac{g_{\gamma V_1 P_1}}{m_0} \frac{g_{V_1 V_2 P_2}}{m_0} \right) \frac{g_{\lambda_{\gamma},\lambda'-\lambda} K_{\lambda_{\gamma}\lambda\lambda'}}{(m_{V_1}^2 - im_{V_1}\Gamma_{V_1} - t_1)(m_{V_2}^2 - im_{V_2}\Gamma_{V_2} - t_p)}$$

## [GM, Vincent Mathieu, et al. (JPAC), arXiv:2008.XXXX]



2. Reggeize

$$K_{\lambda_{\gamma}\lambda\lambda'} \to K_{\lambda_{\gamma}\lambda\lambda'} \times R\left(\alpha_1(t_{\pi}), \alpha_2(t_p), s_{\eta\pi}, s_{\eta p}, \frac{s}{\alpha' s_{\eta\pi} s_{\eta p}}\right)$$

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2. Reggeize

$$\begin{split} K_{\lambda_{\gamma}\lambda\lambda'} & \rightarrow K_{\lambda_{\gamma}\lambda\lambda'} \times R\left(\alpha_{1}(t_{\pi}), \alpha_{2}(t_{p}), s_{\eta\pi}, s_{\eta p}, \frac{s}{\alpha' s_{\eta\pi} s_{\eta p}}\right) \\ & \text{vertex function} \\ R(\alpha_{1}, \alpha_{2}, s_{1}, s_{2}, \eta) &= \underbrace{\xi_{1}\xi_{21}}_{s_{1}\xi_{21}} \eta^{\alpha_{1}-1} \underbrace{V(\alpha_{1}, \alpha_{2}, \eta)}_{signature factors} + \underbrace{\xi_{2}\xi_{12}}_{signature factors} \underbrace{V(\alpha_{2}, \alpha_{1}, \eta)}_{signature factors} (Shimada, Martin and Irving, Nucl. Phys. B 142 (1978)] \\ \eta &= \frac{s}{\alpha' s_{1} s_{2}} \end{split}$$

## Double Regge model $\eta^{(\prime)}\pi$ photoproduction

1. Start from a vector-vector exchange model

$$A_{\lambda_{\gamma}\lambda\lambda'} = \sum_{\text{diagrams}} \left( \frac{g_{\gamma V_1 P_1}}{m_0} \frac{g_{V_1 V_2 P_2}}{m_0} \right) \frac{g_{\lambda_{\gamma},\lambda'-\lambda} K_{\lambda_{\gamma}\lambda\lambda'}}{(m_{V_1}^2 - im_{V_1}\Gamma_{V_1} - t_1)(m_{V_2}^2 - im_{V_2}\Gamma_{V_2} - t_p)}$$



2. Reggeize

$$K_{\lambda_{\gamma}\lambda\lambda'} \rightarrow K_{\lambda_{\gamma}\lambda\lambda'} \times R\left(\alpha_{1}(t_{\pi}), \alpha_{2}(t_{p}), s_{\eta\pi}, s_{\eta p}, \frac{s}{\alpha' s_{\eta\pi} s_{\eta p}}\right)$$

$$(\text{Shimada, Martin and Irving, Nucl. Phys. B 142 (1978)})$$

$$R(\alpha_{1}, \alpha_{2}, s_{1}, s_{2}, \eta) = \underbrace{\xi_{1}\xi_{21}}_{\text{Signature factors}} \gamma^{\alpha_{1}-1} \underbrace{V(\alpha_{1}, \alpha_{2}, \eta)}_{\text{Signature factors}} + \underbrace{\xi_{2}\xi_{12}}_{\text{Signature factors}} \gamma^{\alpha_{2}-1} \underbrace{V(\alpha_{2}, \alpha_{1}, \eta)}_{\text{Signature factors}} (\alpha' s_{1})^{\alpha_{1}-1} (\alpha' s_{2})^{\alpha_{2}-1} \left[(\alpha_{1}-1)\Gamma(1-\alpha_{1})\right] \left[(\alpha_{2}-1)\Gamma(1-\alpha_{2})\right]$$

In the double Regge limit 
$$(s, s_{\eta,\pi}, s_p \to \infty, \eta \sim \text{ct.}, s_{\eta\pi}/s_{\eta p} \sim \text{ct.})$$
  
 $K_{\lambda_{\gamma}\lambda\lambda'} \sim s_{\eta\pi}s_{\eta p}$  and  $K_{\lambda_{\gamma}\lambda\lambda'}R \sim C_1 s^{\alpha_1(t_{\pi})}s^{\alpha_2(t_p)-\alpha_1(t_{\pi})}_{\eta p} + C_2 s^{\alpha_1(t_{\pi})-\alpha_2(t_p)}_{\eta \pi}s^{\alpha_2(t_p)}$ 

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#### **Forward-Backward asymmetry**

#### (Preliminary results)

 $\frac{d\sigma}{d\Omega_{\rm GJ} dz_{\rm cm} ds_{\eta\pi}} \propto |A_{\lambda_{\gamma}\lambda\lambda'}|^2$ 

The asymmetry is defined as  $(M = \sqrt{s_{\eta\pi}})$ 

 $A(M) = \frac{F(M) - B(M)}{F(M) + B(M)}$ 

The forward and backward intensities contain cuts in kinematic variables

$$F(M) = \int d^2 \Omega_{GJ} dz_{cm} \frac{d\sigma}{d\Omega_{GJ} dz_{cm} dM_{\eta\pi}^2} \theta(t_\eta > -2) \theta(t_p > -2) \theta(s_{\eta\pi} > 4) \theta(s_{\pi p} > 4) \theta(s_{\eta p} > 4.75)$$

$$B(M) = \int d^2 \Omega_{GJ} dz_{cm} \frac{d\sigma}{d\Omega_{GJ} dz_{cm} dM_{\eta\pi}^2} \theta(t_\pi > -2) \theta(t_p > -2) \theta(s_{\eta\pi} > 4) \theta(s_{\pi p} > 4) \theta(s_{\eta p} > 4.75)$$

and the physics model is captured in



[GM, Vincent Mathieu, et al. (JPAC), arXiv:2008.XXXX]



#### **Forward-Backward asymmetry**

#### (Preliminary results)

The asymmetry is defined as  $(M = \sqrt{s_{\eta\pi}})$ 

 $A(M) = \frac{F(M) - B(M)}{F(M) + B(M)}$ 

1.00

0.75

0.50

0.25

0.00

-0.25

-0.50

-0.75

-1.00

5

 $\cos \theta$ 

The forward and backward intensities contain cuts in kinematic variables

0.010

0.008

 $\frac{d\sigma/dt}{d\sigma/dt} (\mu b/{\rm GeV^2})$ 

0.002

0.000

10

$$F(M) = \int d^2 \Omega_{GJ} dz_{cm} \frac{d\sigma}{d\Omega_{GJ} dz_{cm} dM_{\eta\pi}^2} \theta(t_\eta > -2) \theta(t_p > -2) \theta(s_{\eta\pi} > 4) \theta(s_{\pi p} > 4) \theta(s_{\eta p} > 4.75)$$
$$B(M) = \int d^2 \Omega_{GJ} dz_{cm} \frac{d\sigma}{d\Omega_{GJ} dz_{cm} dM_{\eta\pi}^2} \theta(t_\pi > -2) \theta(t_p > -2) \theta(s_{\eta\pi} > 4) \theta(s_{\pi p} > 4) \theta(s_{\eta p} > 4.75)$$

0.7

0.6

0.5

0.4

0.3

0.2

0.1

0.0

-0.1 2.0

Asymmetry

PAC

ector-Vector

2.6

2.4

 $m_{n\pi} \,({\rm GeV})$ 

2.8

Phase Space

2.2

#### [GM, Vincent Mathieu, et al. (JPAC), arXiv:2008.XXXX]





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#### **Summary**

**Regge theory** is a practical tool to model and understand meson production at **high energies** 

- Step forward in understanding pion exchange in pion photoproduction (gauge invariance)
- Interesting physics in  $\eta^{(\prime)}\pi$ , in the resonance region (hybrid meson) but also in the double Regge region

Strong effort from JPAC to **provide theory support to experimental analyses** (GlueX, but also CLAS, COMPASS...)

- Understand the data
- Provide predictions
- Close collaboration with experimentalists