

## collision systems

Au+Au @ 200 GeV

Pb+Pb @ 2.76 TeV

Pb+Pb @ 5.02 TeV

## particlization models

Grad

Chapman-Enskog

Pratt-Torrieri-Bernhard

account for model uncertainties

parameter space  $x = (x_1, x_2, ..., x_q)$  (shared by source and target)

source

 $x_1^S x_2^S x_3^S \cdots$ 

high-fidelity at fine design points

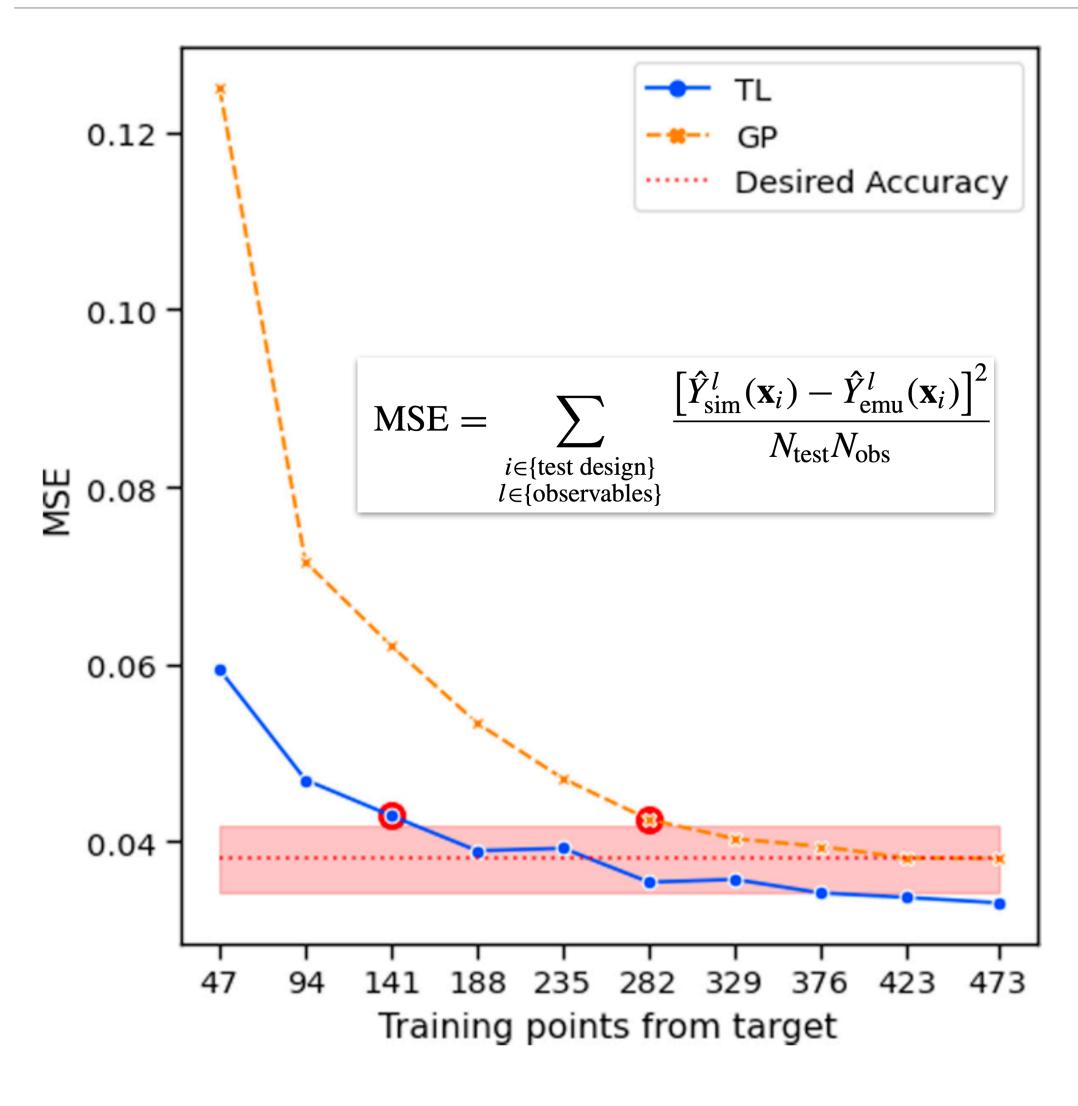
 $f_T(\mathbf{x}) = \rho f_S(\mathbf{x}) + \delta(\mathbf{x})$   $f_S(\mathbf{x}) \sim \text{GP}\{\mu_S, k_S^{\text{SE}}(\cdot, \cdot)\}$   $\delta(\mathbf{x}) \sim \text{GP}\{\mu_\delta, k_\delta^{\text{SE}}(\cdot, \cdot)\}$ 

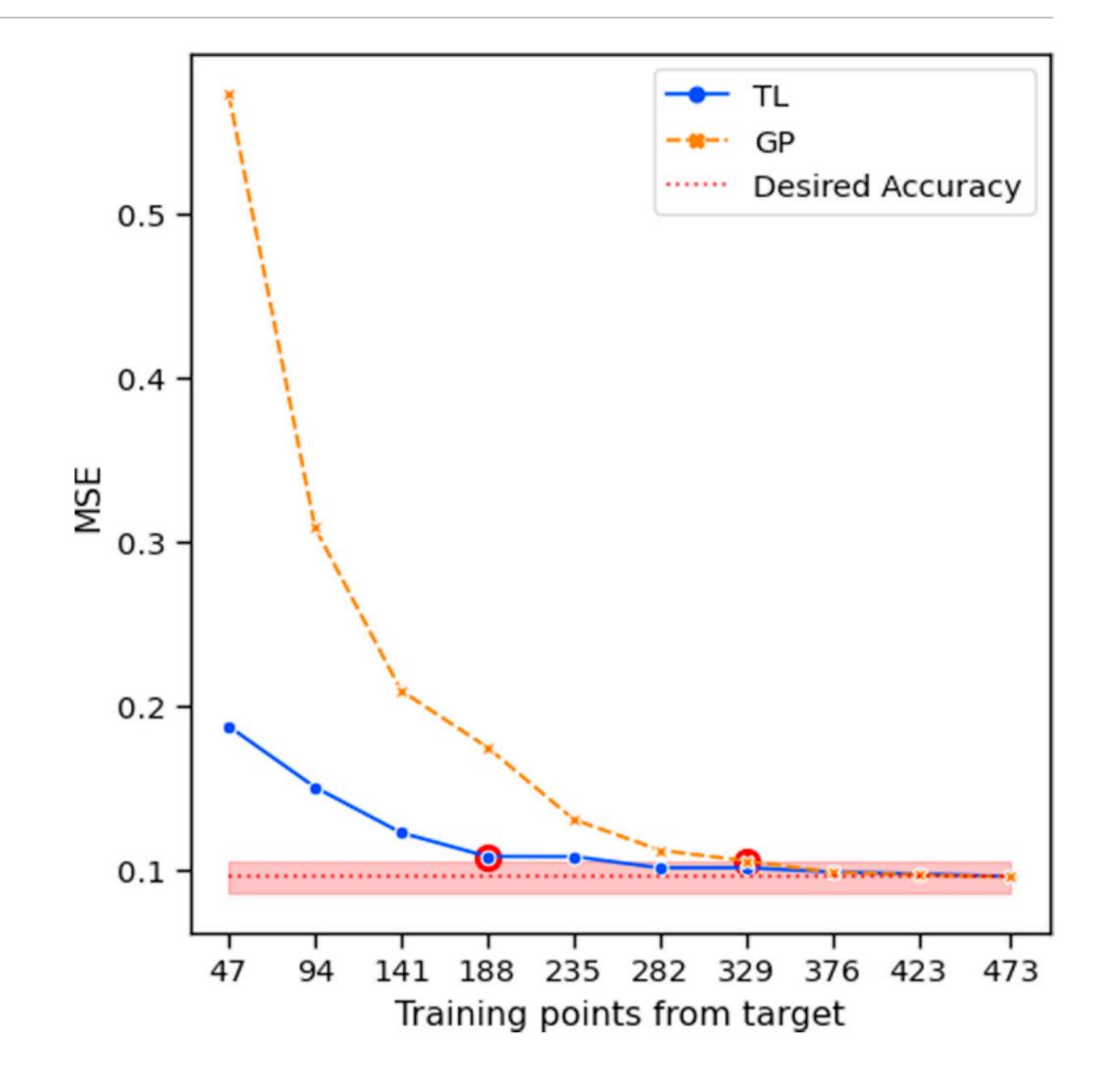
target

 $x_1^T$   $x_2^T$   $x_3^T$  ...

high-fidelity at coarser design points

emulator predicts results at an arbitrary  $\boldsymbol{x}^T$ 







where the posterior mean and variance of the transfer learning emulator model are given by

$$\mu_{T}^{*}(\mathbf{x}_{\text{new}}) = \rho \mu_{S} + \mu_{\delta}$$

$$+ \mathbf{k}_{\text{new}}^{\top} \mathbf{\Sigma}^{-1} \left( \begin{bmatrix} \mathbf{y}_{S} \\ \mathbf{y}_{T} \end{bmatrix} - \begin{bmatrix} \mu_{S} \mathbf{1}_{m} \\ (\rho \mu_{S} + \mu_{\delta}) \mathbf{1}_{n} \end{bmatrix} \right),$$

$$\sigma_{T}^{2*}(\mathbf{x}_{\text{new}}) = \rho^{2} \mathbf{k}_{S}(\mathbf{x}_{\text{new}}, \mathbf{x}_{\text{new}}) + \mathbf{k}_{\delta}(\mathbf{x}_{\text{new}}, \mathbf{x}_{\text{new}})$$

$$- \mathbf{k}_{\text{new}}^{\top} \mathbf{\Sigma}^{-1} \mathbf{k}_{\text{new}},$$
(10)

with  $\mathbf{k}_{\text{new}} = [\mathbf{k}_{\text{new}}^S, \mathbf{k}_{\text{new}}^T]$  and  $\mathbf{k}_{\text{new}}^S = [k(\mathbf{x}_{\text{new}}, \mathbf{x}_i)]_{i=1}^m, \mathbf{k}_{\text{new}}^T = [k(\mathbf{x}_{\text{new}}, \mathbf{x}_j)]_{i=1}^n$ , and

$$\mathbf{\Sigma} = \begin{bmatrix} \mathbf{K}_{S}(\mathbf{X}_{S}) + \gamma_{S}^{2} \mathbf{I}_{m} & \rho \mathbf{K}_{S}(\mathbf{X}_{S}, \mathbf{X}_{T}) \\ \rho \mathbf{K}_{S}(\mathbf{X}_{S}, \mathbf{X}_{T})^{\top} & \rho^{2} \mathbf{K}_{S}(\mathbf{X}_{T}) + \mathbf{K}_{\delta}(\mathbf{X}_{T}) + \gamma_{T}^{2} \mathbf{I}_{n} \end{bmatrix}.$$