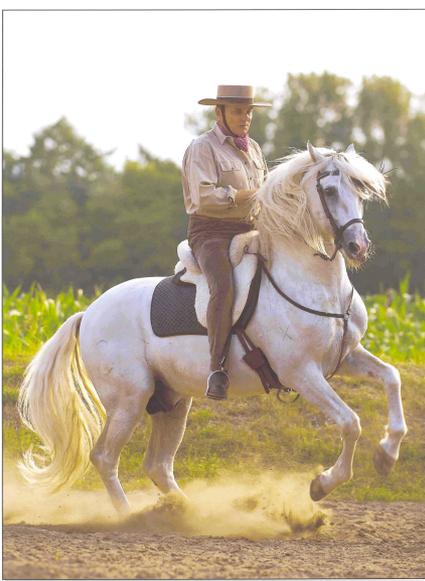


**Collective dynamics in high-energy collisions**

**LBL, May 14-18, 2012**

**Heavy quarkonia  
and  
collective dynamics of  
strongly interacting matter**

**D. Kharzeev**



**Stony Brook University**





Tuesday, May 15, 2012

# Outline

Lecture 1: Heavy quarkonia in QCD matter

Lecture 2: New developments in relativistic hydrodynamics of strongly interacting matter  
(the role of quantum anomalies)

# Heavy quarkonia in QCD matter

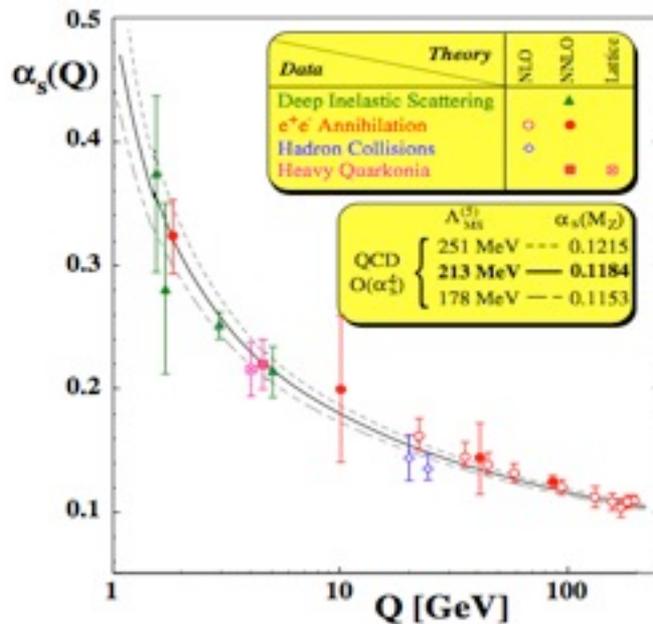
- Why heavy quarks?
- Quarkonium: the “hydrogen atom of QCD”
- Quarkonium production in strong color fields (cold nuclear matter effects in pA, AA)
- Quarkonium in quark-gluon plasma
- Confinement, holography and entanglement

# Why heavy quarks?

Heavy quark masses  $M_H$  are generated at the electroweak scale, and are external parameters in QCD;

Heavy quarks are “heavy” because their masses are large on the typical QCD scale of  $\Lambda_{\text{QCD}}$ :

$$M_H \gg \Lambda_{\text{QCD}}$$



$$\alpha_s(M_H) \ll 1$$

$$\frac{\langle \alpha_s G^2 \rangle}{M_H^4} \ll 1$$

# Why heavy quarks?

QCD matter is characterized by dimensionful parameters: saturation scale  $Q_s$ , density, transport coefficient, ...

$$M_H \leftrightarrow Q_s, Q_s^2/\Lambda_{\text{QCD}}, \rho^{1/3}, T, \sqrt{\hat{q}L}, \dots$$

depending on their values, “heavy” quarks can behave either as heavy or as light !

⇒ Use heavy quarks to extract information about the properties of QCD matter

# November revolution:

VOLUME 33, NUMBER 23

PHYSICAL REVIEW LETTERS

2 DECEMBER 1974

## Experimental Observation of a Heavy Particle $J^\dagger$

J. J. Aubert, U. Becker, P. J. Biggs, J. Burger, M. Chen, G. Everhart, P. Goldhagen, J. Leong, T. McCorriston, T. G. Rhoades, M. Rohde, Samuel C. C. Ting, and Sau Lan Wu  
*Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139*

and

Y. Y. Lee  
*Brookhaven National Laboratory, Upton, New York 11973*  
(Received 12 November 1974)

We report the observation of a heavy particle  $J$ , with mass  $m = 3.1$  GeV and width approximately zero. The observation was made from the reaction  $p + \text{Be} \rightarrow e^+ + e^- + X$  by measuring the  $e^+e^-$  mass spectrum with a precise pair spectrometer at the Brookhaven National Laboratory's 30-GeV alternating-gradient synchrotron.

## Discovery of a Narrow Resonance in $e^+e^-$ Annihilation\*

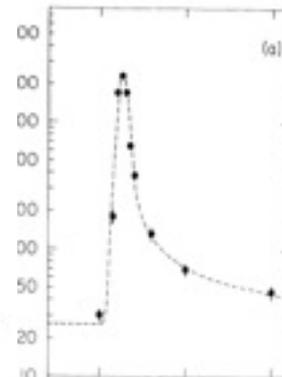
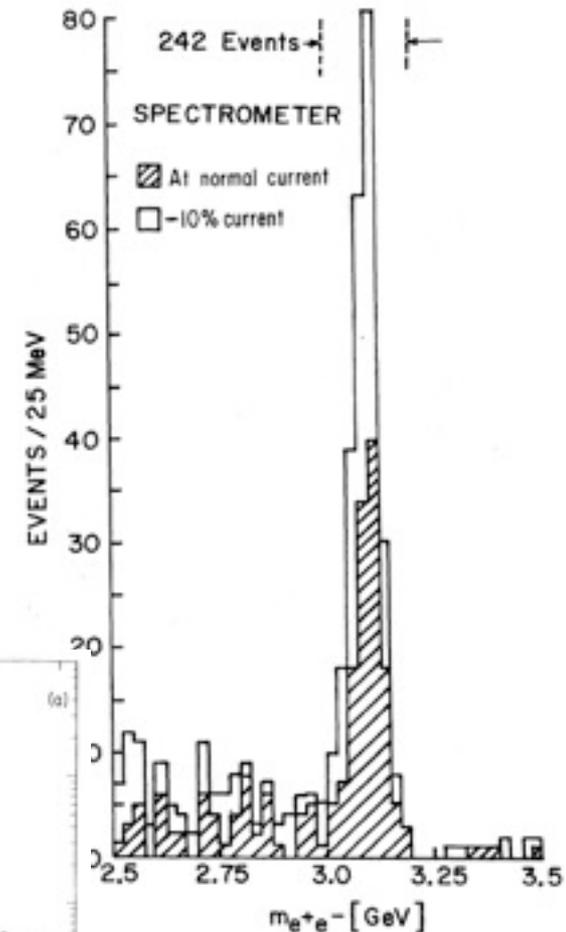
J.-E. Augustin,† A. M. Boyarski, M. Breidenbach, F. Bulos, J. T. Dacia, G. J. Feldman, G. E. Fischer, D. Fryberger, G. Hanson, B. Jean-Marie,† R. R. Larsen, V. Lüth, H. L. Lynch, D. Lyon, C. C. Morehouse, J. M. Paterson, M. L. Perl, B. Richter, P. Rapidis, R. F. Schwitters, W. M. Tanenbaum, and F. Vannucci‡  
*Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305*

and

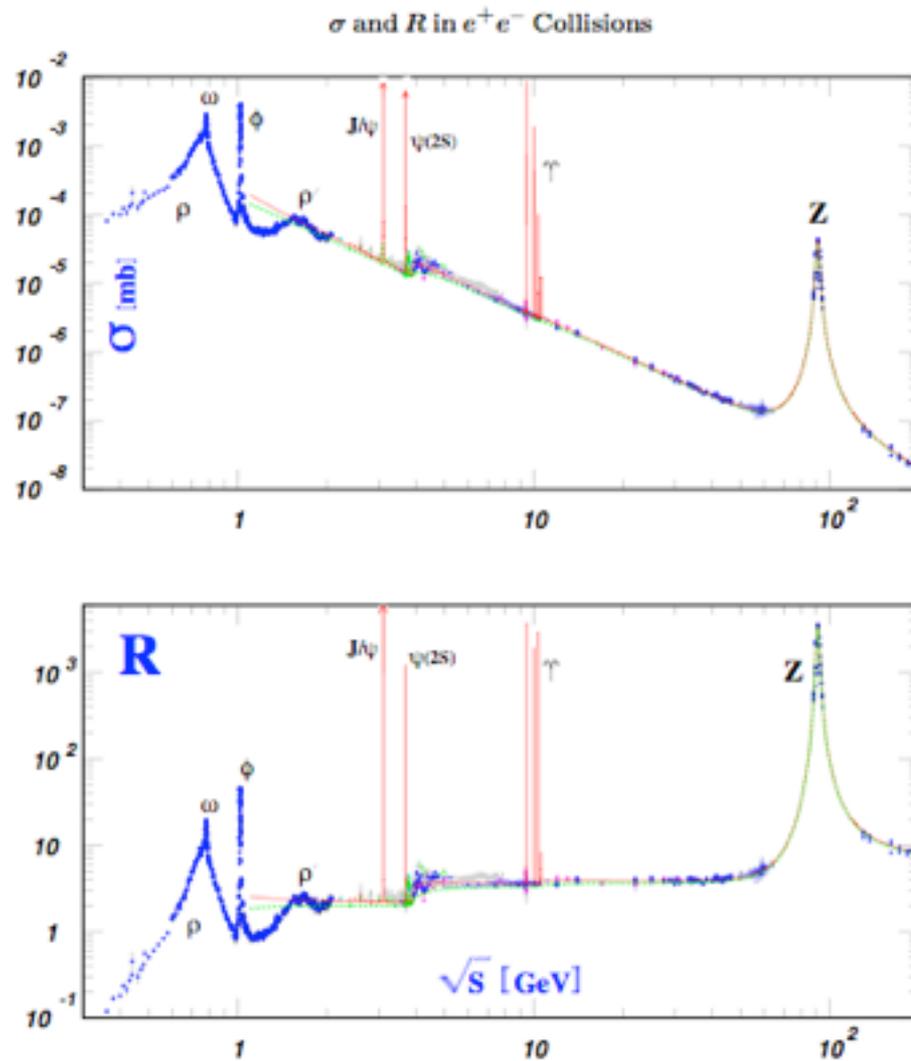
G. S. Abrams, D. Briggs, W. Chinowsky, C. E. Friedberg, G. Goldhaber, R. J. Hollebeek, J. A. Kadyk, B. Lulu, F. Pierre,§ G. H. Trilling, J. S. Whitaker, J. Wiss, and J. E. Zipse

*Lawrence Berkeley Laboratory and Department of Physics, University of California, Berkeley, California 94720*  
(Received 13 November 1974)

We have observed a very sharp peak in the cross section for  $e^+e^- \rightarrow \text{hadrons}$ ,  $e^+e^-$ , and possibly  $\mu^+\mu^-$  at a center-of-mass energy of  $3.105 \pm 0.003$  GeV. The upper limit to the full width at half-maximum is 1.3 MeV.



# Why is heavy quarkonium so narrow?

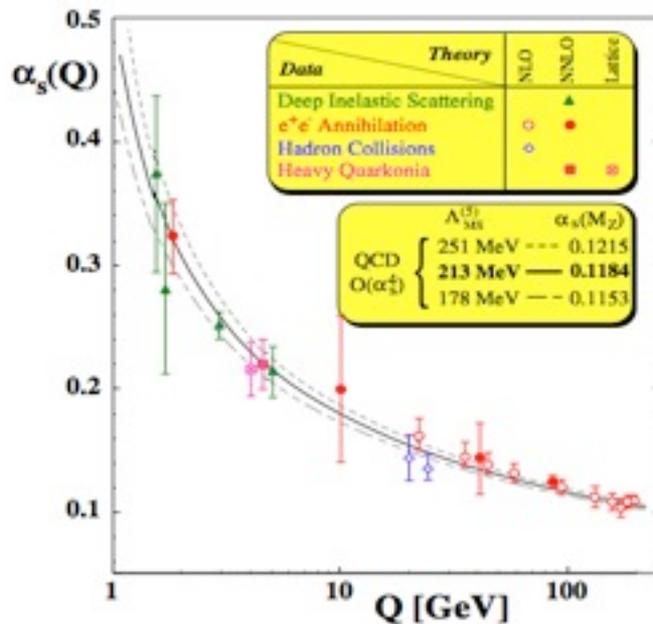


# The annihilation width of heavy quarkonia is small due to the asymptotic freedom

Heavy quark masses  $M_H$  are generated at the electroweak scale, and are external parameters in QCD;

Heavy quarks are “heavy” because their masses are large on the typical QCD scale of  $\Lambda_{\text{QCD}}$ :

$$M_H \gg \Lambda_{\text{QCD}}$$



$$\alpha_s(M_H) \ll 1$$

$$\frac{\langle \alpha_s G^2 \rangle}{M_H^4} \ll 1$$

# Quarkonium and asymptotic freedom (Coulomb potential)

Spectral representation in the t-channel:  $V(R) = \sum_m \sigma(m^2) \frac{\exp(-mR)}{R}$

$$\text{Disc}_t \left( \begin{array}{c} | \\ \text{---} \text{---} \text{---} \\ | \end{array} \text{---} \text{---} \text{---} \begin{array}{c} \text{---} \text{---} \text{---} \\ | \\ \text{---} \text{---} \text{---} \\ | \end{array} \text{---} \text{---} \text{---} \begin{array}{c} | \\ \text{---} \text{---} \text{---} \\ | \end{array} \right) = \begin{array}{c} | \\ \text{---} \text{---} \text{---} \\ | \end{array} \text{---} \text{---} \text{---} \begin{array}{c} \text{---} \text{---} \text{---} \\ | \\ \text{---} \text{---} \text{---} \\ | \end{array} \text{---} \text{---} \text{---} \begin{array}{c} | \\ \text{---} \text{---} \text{---} \\ | \end{array} \propto \sigma \left( \left( \begin{array}{c} | \\ \text{---} \text{---} \text{---} \\ | \end{array} \text{---} \text{---} \text{---} \begin{array}{c} \text{---} \text{---} \text{---} \\ | \\ \text{---} \text{---} \text{---} \\ | \end{array} \right) \right)$$

If physical particles can be produced (positive spectral density),  
then unitarity implies screening

$$\left\{ \frac{d \alpha_s^{-1}(R)}{d \ln R} \right\}^{\text{phys}} \propto \frac{1}{3} N + \frac{2}{3} n_f$$

Gluons Quarks  
(transverse)

# Coulomb potential in QCD - II

Missing non-Abelian effect: instantaneous Coulomb exchange dressed by (zero modes of) transverse gluons

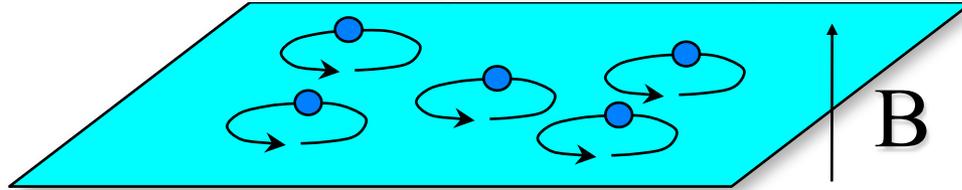
$$\sum_n [0 + \perp \rightarrow 0]^n = \left| \begin{array}{c} 0 \quad 0 \\ \text{---} \bullet \text{---} \\ \text{---} \perp \end{array} \right| + \left| \begin{array}{c} 0 \quad 0 \quad 0 \\ \text{---} \bullet \text{---} \bullet \text{---} \\ \text{---} \perp \quad \text{---} \perp \end{array} \right| + \dots$$

Negative sign  
(the shift of the ground level  
due to perturbations - **unstable vacuum!** ):

$$\delta E \equiv E - E_0 = \sum_n \frac{|\langle 0 | \delta V | n \rangle|^2}{E_0 - E_n} < 0$$

**Anti-screening**  $\left\{ \frac{d \alpha_s^{-1}(R)}{d \ln R} \right\}^{\text{stat}} \propto -4N$

# Asymptotic freedom and the instability of the perturbative vacuum



The effective potential: sum over 2D Landau levels

$$V_{\text{pert}}(H) = \frac{g H}{4 \pi^2} \int dp_z \sum_{n=0}^{\infty} \sum_{s_z=\pm 1} \sqrt{2 g H (n + 1/2 - s_z) + p_z^2}.$$

Paramagnetic response of the vacuum:

$$\text{Re } V_{\text{pert}}(H) = \frac{1}{2} H^2 + (g H)^2 \frac{b}{32 \pi^2} \left( \ln \frac{g H}{\mu^2} - \frac{1}{2} \right)$$



1. The lowest level  $n=0$  of radius  $\sim (gH)^{-1/2}$  is **unstable!**

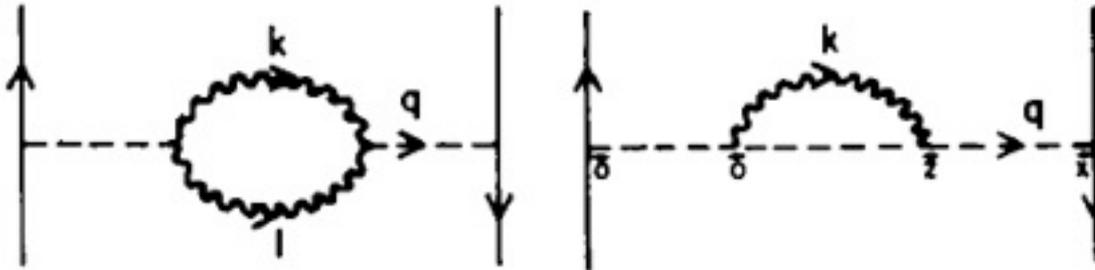
2. Strong fields  $\longleftrightarrow$  Short distances

Instability of perturbative  
QCD vacuum;  
What is the true ground state?

# Quarkonia: the potential problems...

$$D_{\mu\nu}^{ab} = i \delta^{ab} \frac{1}{\bar{k}^2} \quad \mu = \nu = 0 \quad \text{Coulomb gauge}$$

$$= i \delta^{ab} \left( \delta_{ij} - \frac{k_i k_j}{\bar{k}^2} \right) \frac{1}{k^2 + i\epsilon} \quad \mu = i, \nu = j.$$



Screening

Anti-Screening

## THE STATIC POTENTIAL IN QUANTUM CHROMODYNAMICS

Thomas APPELQUIST<sup>1,2</sup> and Michael DINE<sup>1</sup>

*J. Willard Gibbs Laboratory, Yale University, New Haven, CT 06520, USA*

and

I.J. MUZINICH<sup>3</sup>

*Brookhaven National Laboratory, Upton, N.Y. 11973, USA*

Received 18 May 1977

# Quarkonia: the potential problems...

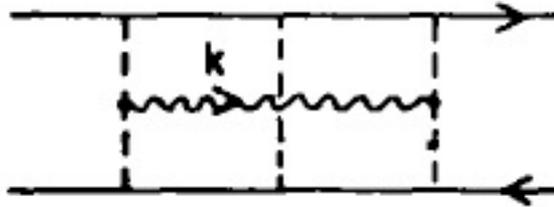
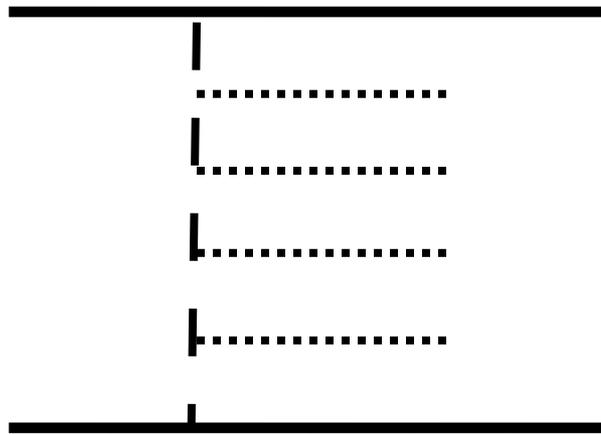


Fig. 4. A three loop graph with a singular static limit.

Higher Fock states; classified in NRQCD

Bodwin, Braaten, Lepage; ...



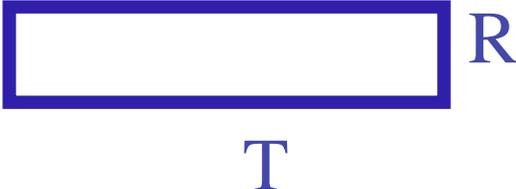
energy of transverse gluons -  
constant per unit of length  
(planar, large N limit);  
... a string?

... can be seen as parts of the QCD string?

e.g., the “gluon chain” model

Greensite and Thorn

# Scale invariance and confinement

Consider a rectangular Wilson loop: 

$$W(C) = \exp \left( ig \int_C A_\mu dx^\mu \right)$$

It is related to the potential  $V(R)$  acting between the charges  $Q$  and  $\bar{Q}$ :

$$W(C) \rightarrow \exp(-TV(R))$$

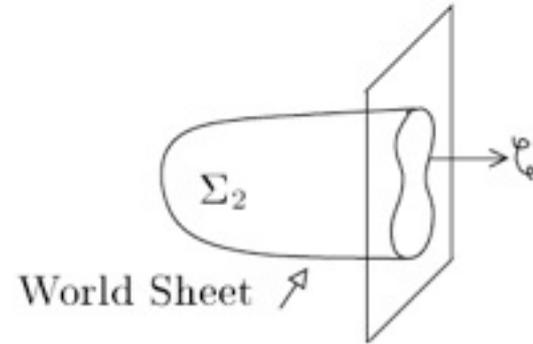
Scale transformation:  $T \rightarrow \lambda T$ ;  $R \rightarrow \lambda R$ ;

the only solution: Coulomb potential

$$V(R) \sim \frac{1}{R}$$

# Insights from holography

$$V(L) = - \lim_{T \rightarrow \infty} \frac{1}{T} \ln \langle W(C_{L \times T}) \rangle .$$



Of course, no confinement in N=4 SYM: scale invariance dictates that the expectation value of  $W$  must scale with  $T/L$  - thus Coulomb potential

$$V(L) \sim 1/L$$

Nevertheless, an interesting lesson: solving for the minimal surface in super-gravity and evaluating its area, one finds

$$V(L) = - \frac{4\pi^2 \sqrt{\lambda}}{\Gamma^4(1/4) L} .$$
$$N \rightarrow \infty, \quad \lambda = g_{YM}^2 N .$$

**Why square root?**

“not your grandfather’s Coulomb potential”, a weaker one! screening?

# Insights from holography

$$\alpha(\lambda) = \begin{cases} \frac{\lambda}{4\pi} + \dots, & \text{for } \lambda \rightarrow 0; \\ \frac{4\pi^2 \sqrt{2\lambda}}{\Gamma^4(1/4)} + O(1), & \text{for } \lambda \rightarrow \infty. \end{cases} \quad V(L) = -\frac{\alpha(L)}{L}$$

Indeed, the square root of the coupling (but not the pre-factor) can be reproduced on the Field Theory side by resummation of planar diagrams:

Erickson, Semenoff  
Szabo, Zarembo,  
hep-th/9911088

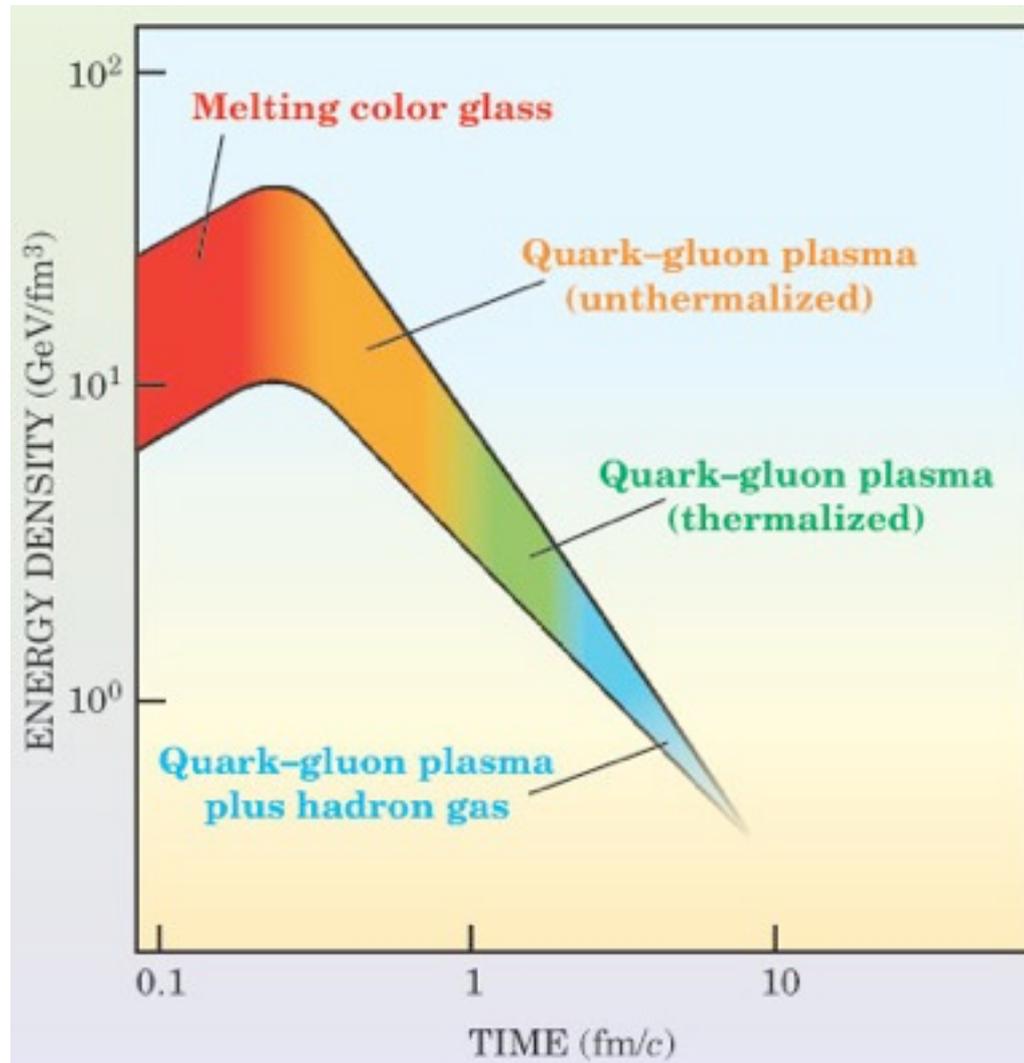
$$-\ln \left\{ 1 + \text{diagram}_1 + \text{diagram}_2 + \dots \right\} = \frac{\lambda T}{4\pi L} - \frac{\lambda^2 T}{(2\pi)^3 L} \ln \frac{T}{L} + \dots$$

$$\sum_{\text{ladders}} \text{diagram}_A = 1 + \sum_{\text{ladders}} \text{diagram}_B$$

$$\alpha(\lambda) = \frac{\sqrt{\lambda}}{\pi} - 1 + O(1/\sqrt{\lambda}),$$

Infinite number of higher Fock states, but their effect may be resummed?

# Quarkonium production in nuclear collisions



T. Ludlam,  
L. McLerran,  
Physics Today  
October 2003

# Heavy quarks and the Color Glass Condensate

Lecture by L. McLerran

In CGC, heavy quarks can behave either as “light” or “heavy”

Naïve consideration:

DK & K. Tuchin, hep-ph/0310358

CGC is characterized by the chromo-electric field

$$E \sim \frac{Q_s^2}{g}$$

when the strength of the field is

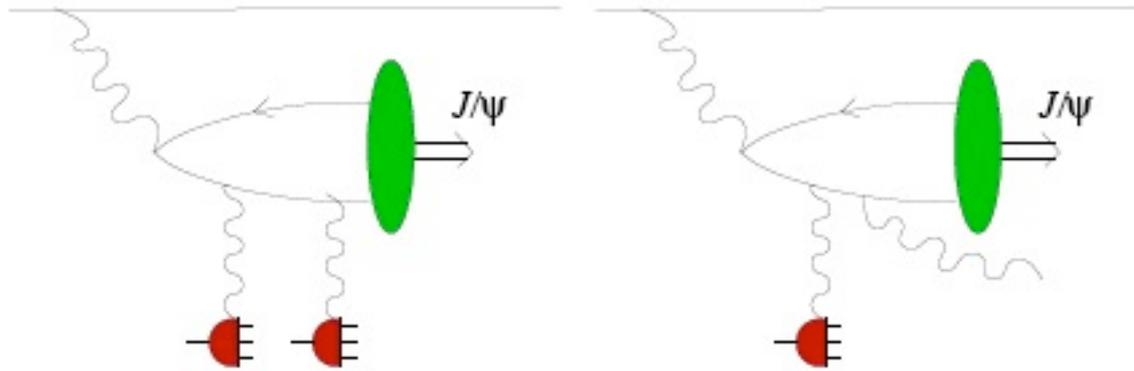
$$gE \sim \frac{M}{1/M} = M^2$$

or

$$Q_s^2 \geq M^2$$

heavy quarks no longer decouple  $\Rightarrow$  they are not really “heavy”

# J/Ψ production in strong color fields



At high parton density, when  $\alpha_s^2 A^{1/3} \sim 1$

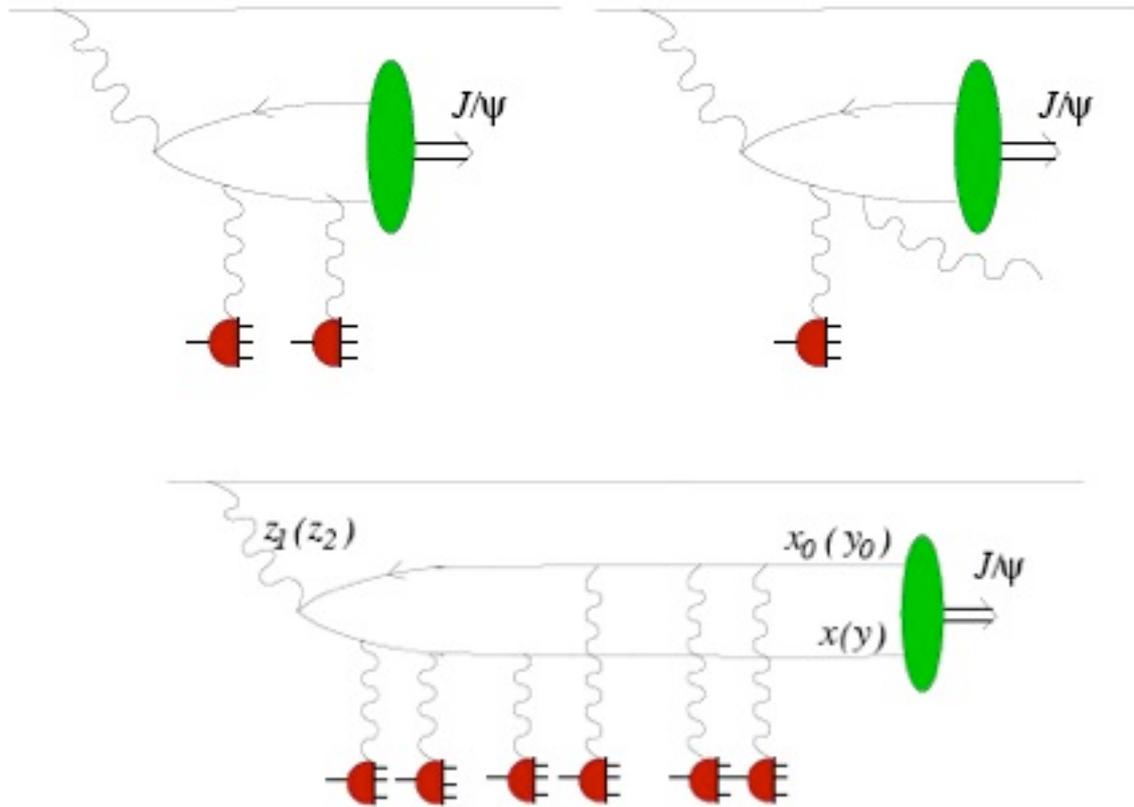
$$\alpha_s^6 A^{2/3} \sim \alpha_s^2$$

$$\alpha_s^5 A^{1/3} \sim \alpha_s^3$$

this diagram is  
the leading one

DK, K.Tuchin,  
hep-ph/0510358

# $J/\psi$ production in strong color fields



DK, K.Tuchin,  
hep-ph/0510358

# J/ $\Psi$ production in strong color fields

At high enough energy (LHC?), high parton density is reached even in pp collisions - expect the change in the scaling of J/psi yield with associated multiplicity:

$$\alpha_s^5 A^{1/3} \sim \alpha_s^3 \quad \longrightarrow \quad \alpha_s^6 A^{2/3} \sim \alpha_s^2.$$

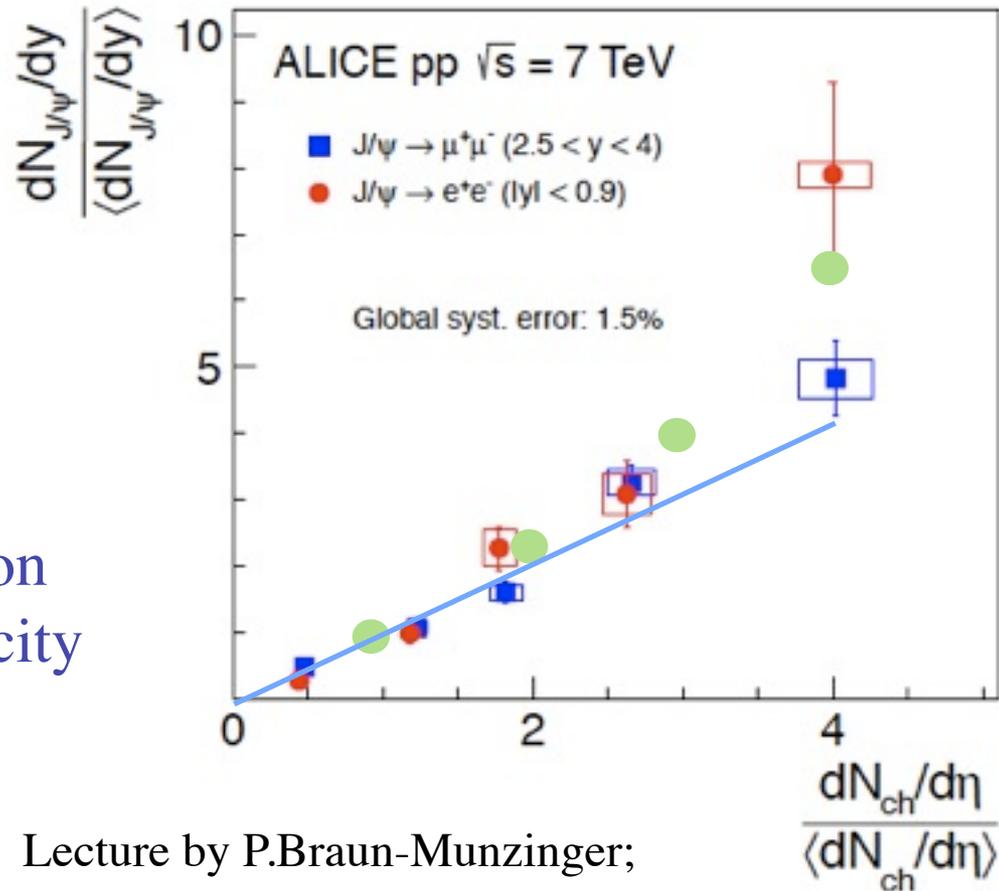
$$\frac{dn_J}{dy} \sim Q_s^2 S \sim \frac{dn}{dy} \quad \frac{dn_J}{dy} \sim Q_s^4 S \sim \left( \frac{dn}{dy} \right)^{4/3}$$

# J/Ψ production as a function of associated multiplicity in pp collisions: the ALICE data

●  $\frac{dn_J}{dy} \sim Q_s^4 S \sim \left(\frac{dn}{dy}\right)^{4/3}$

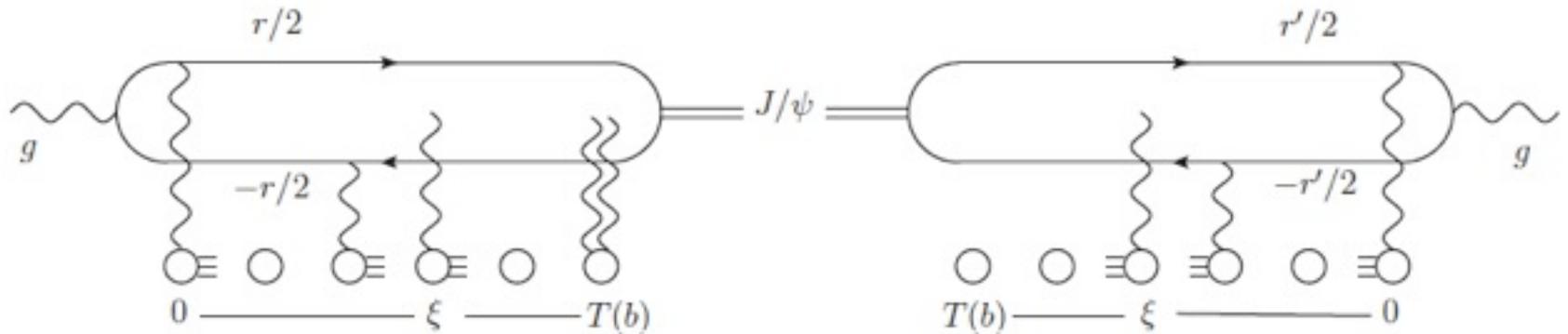
Indication for high parton density in high multiplicity pp collisions?

$$Q_s^2 \quad m_c^2$$



Lecture by P.Braun-Munzinger;  
ALICE Coll., arxiv:1202.5864;

# J/ψ production in strong color fields



Sample diagram contributing to J/ψ production in pA collisions

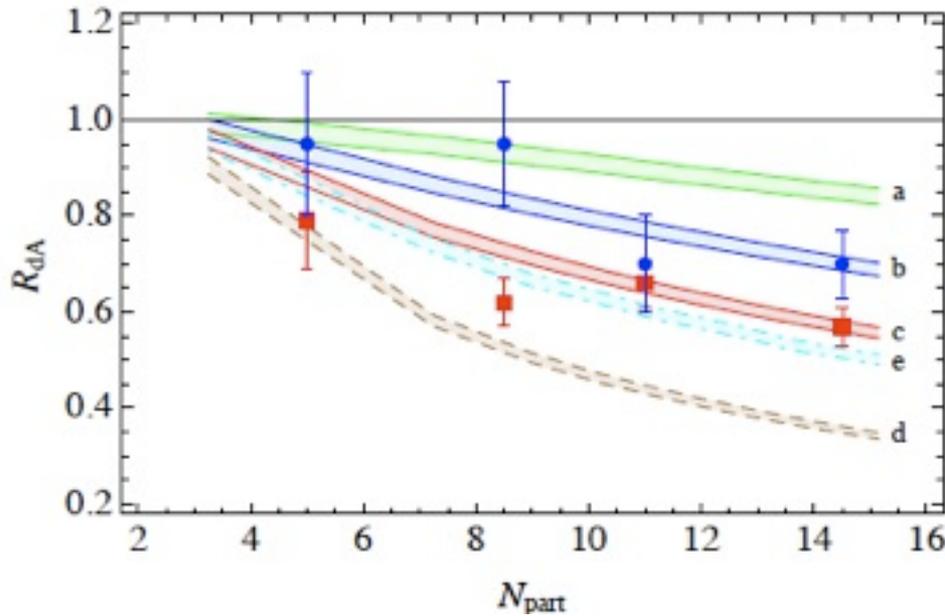
$$\frac{d\sigma_{pA \rightarrow J/\psi X}}{dy d^2b} = x_1 G(x_1, m_c^2) \int_0^1 dz \int \frac{d^2r}{4\pi} \Phi(\mathbf{r}, z) \int_0^1 dz' \int \frac{d^2r'}{4\pi} \Phi^*(\mathbf{r}', z')$$

$$\times \frac{4\mathbf{r} \cdot \mathbf{r}'}{(\mathbf{r} + \mathbf{r}')^2} \left( e^{-\frac{Q_s^2}{16}(\mathbf{r}-\mathbf{r}')^2} - e^{-\frac{Q_s^2}{8}(\mathbf{r}^2+\mathbf{r}'^2)} \right).$$

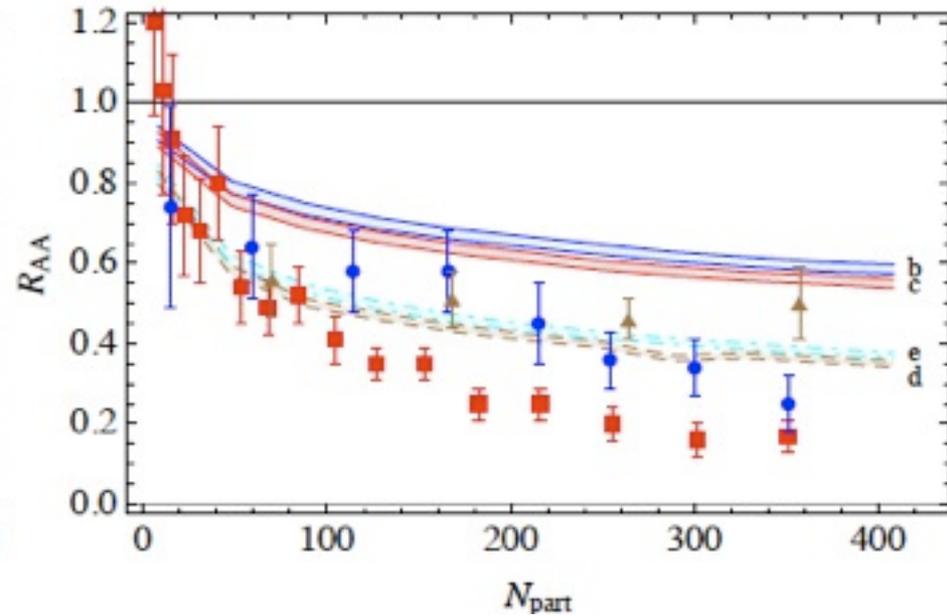
F. Dominguez,<sup>1</sup> D.E. Kharzeev,<sup>2,3</sup> E.M. Levin,<sup>4,5</sup> A.H. Mueller,<sup>1</sup> and K. Tuchin<sup>6</sup>

Phys. Lett. B710 (2012) 182

# J/ $\Psi$ production in strong color fields



Reasonable agreement with  
p(d)A data

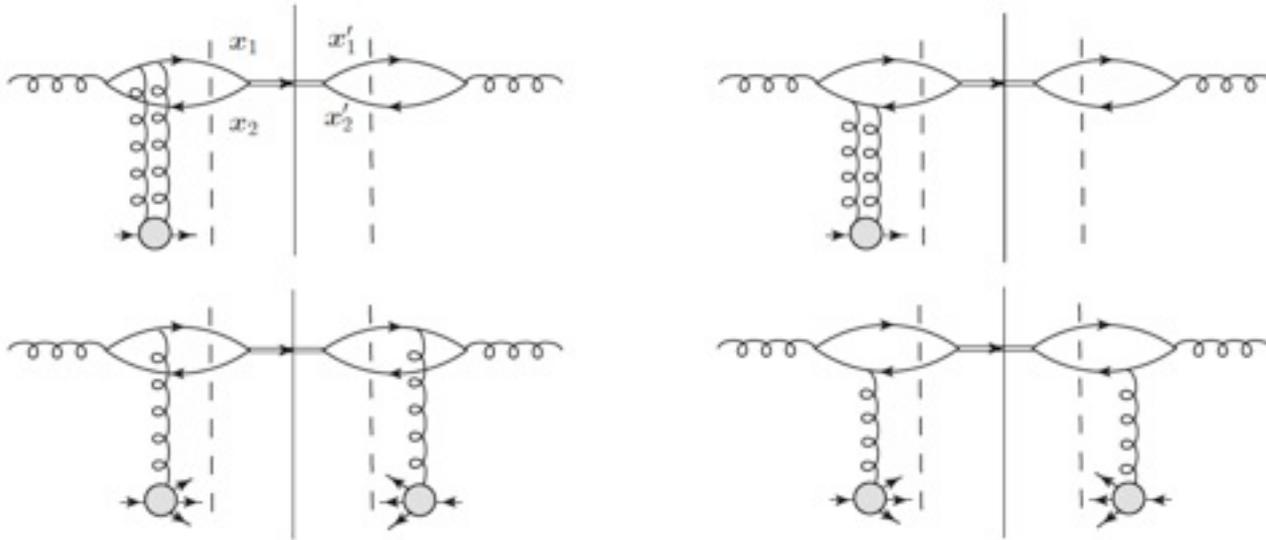


but the AA data indicate  
additional suppression,  
stronger at forward rapidity!

F. Dominguez,<sup>1</sup> D.E. Kharzeev,<sup>2,3</sup> E.M. Levin,<sup>4,5</sup> A.H. Mueller,<sup>1</sup> and K. Tuchin<sup>6</sup>

Phys. Lett. B710 (2012) 182

# The transverse momentum spectra of $J/\Psi$



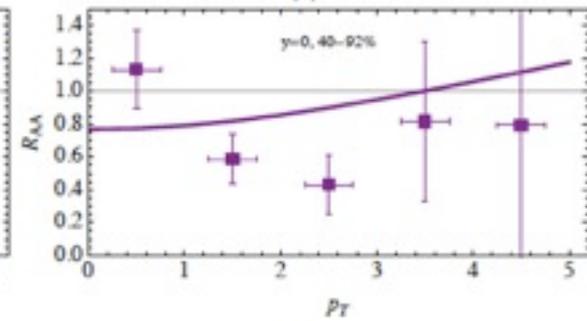
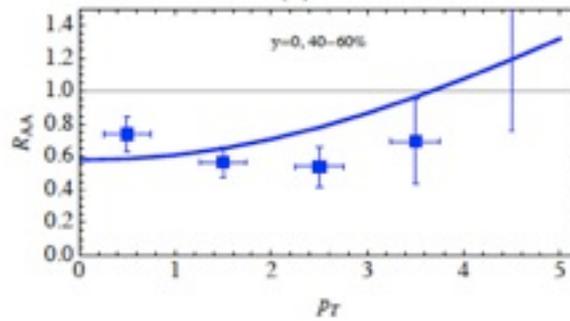
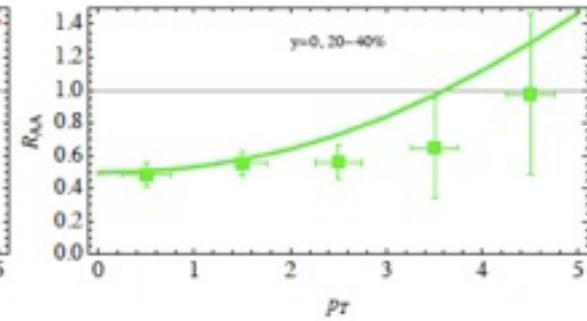
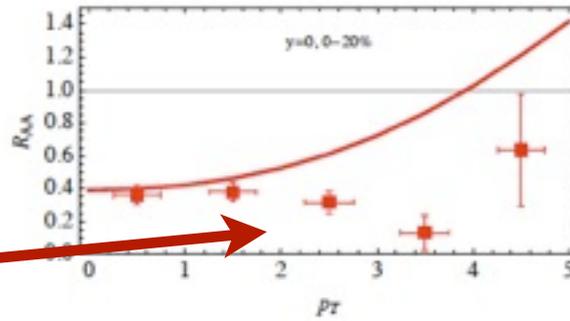
DK, E.Levin, K.Tuchin,  
arxiv: 1205.1554

$$\begin{aligned}
 \frac{d\sigma_{A_1 A_2 \rightarrow J/\psi X}}{d^2 p_\perp dy d^2 B_1 d^2 B_2} &= \int_0^1 dz \int \frac{d^2 r}{4\pi} \Phi(r, z) \int_0^1 dz' \int \frac{d^2 r'}{4\pi} \Phi(r', z') \int d^2 k_\perp \int_0^1 d\xi' \\
 &\times \frac{C_F}{\alpha_s \pi^2} \frac{Q_{s1}^2 Q_{s2}^2}{Q_{s1}^2 + Q_{s2}^2} F_k \frac{\mathbf{r} \cdot \mathbf{r}'}{16\pi \xi'} e^{-\frac{p_\perp^2 + k_\perp^2}{(Q_{s1}^2 + Q_{s2}^2)\xi'}} \\
 &\times I_0 \left( \frac{2p_\perp k_\perp}{(Q_{s1}^2 + Q_{s2}^2)\xi'} \right) e^{-\frac{1}{4}(Q_{s1}^2 + Q_{s2}^2)\frac{1}{4}(r-r')^2 \xi'} e^{-\frac{1}{8}(Q_{s1}^2 + Q_{s2}^2)(r^2 + r'^2)(1-\xi')}
 \end{aligned}$$

# The transverse momentum spectra of $J/\Psi$ comparison to the RHIC data: $y=0$

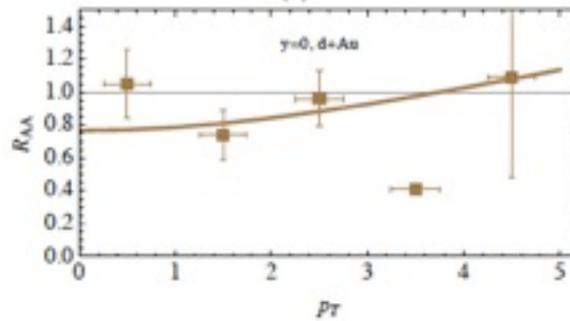
AuAu

Large discrepancy  
at semi-hard  
transverse  
momenta



dAu

PHENIX  
data



DK, E.Levin, K.Tuchin,  
arxiv: 1205.1554

# The transverse momentum spectra of $J/\Psi$ comparison to the RHIC data: $y=1.7$

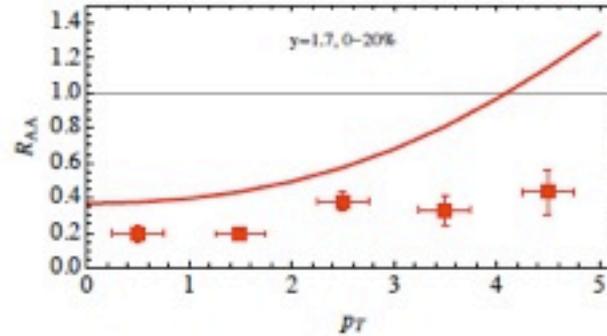
AuAu

Discrepancy  
increases at  
forward  $y$ !

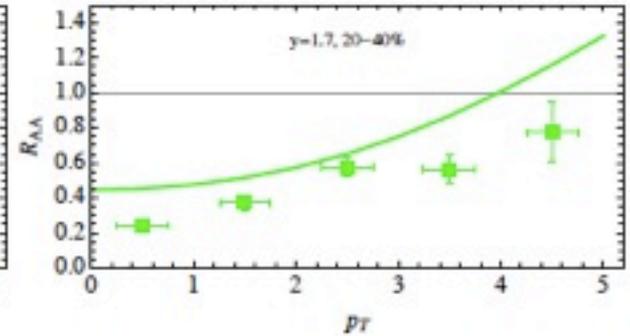
dAu data  
described  
well:

dAu

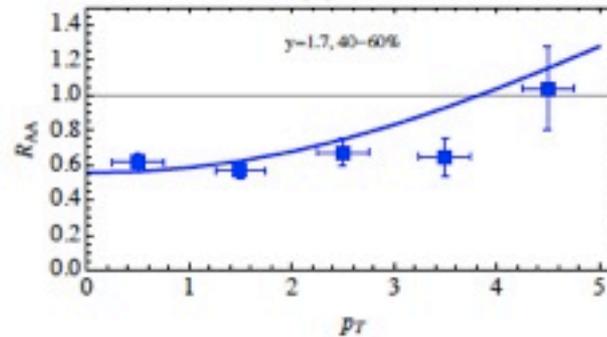
PHENIX  
data



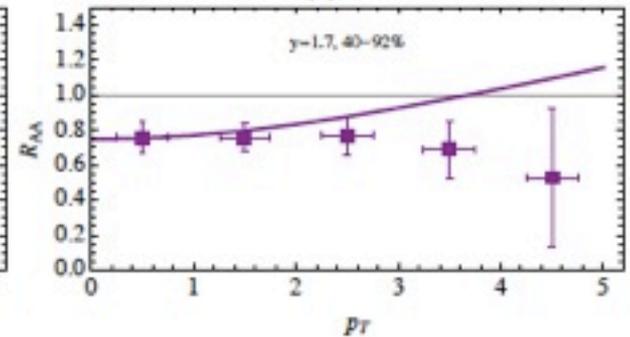
(a)



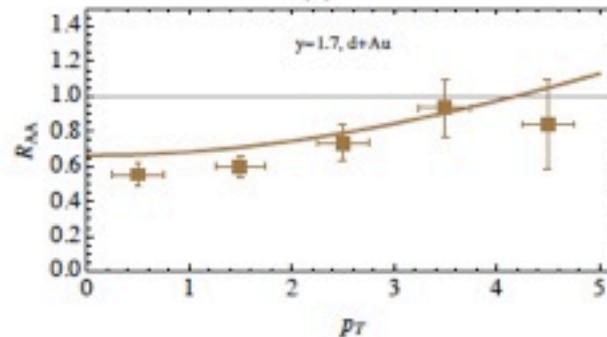
(b)



(c)



(d)



DK, E.Levin, K.Tuchin,  
arxiv: 1205.1554

# The transverse momentum spectra of $J/\Psi$ : predictions for LHC

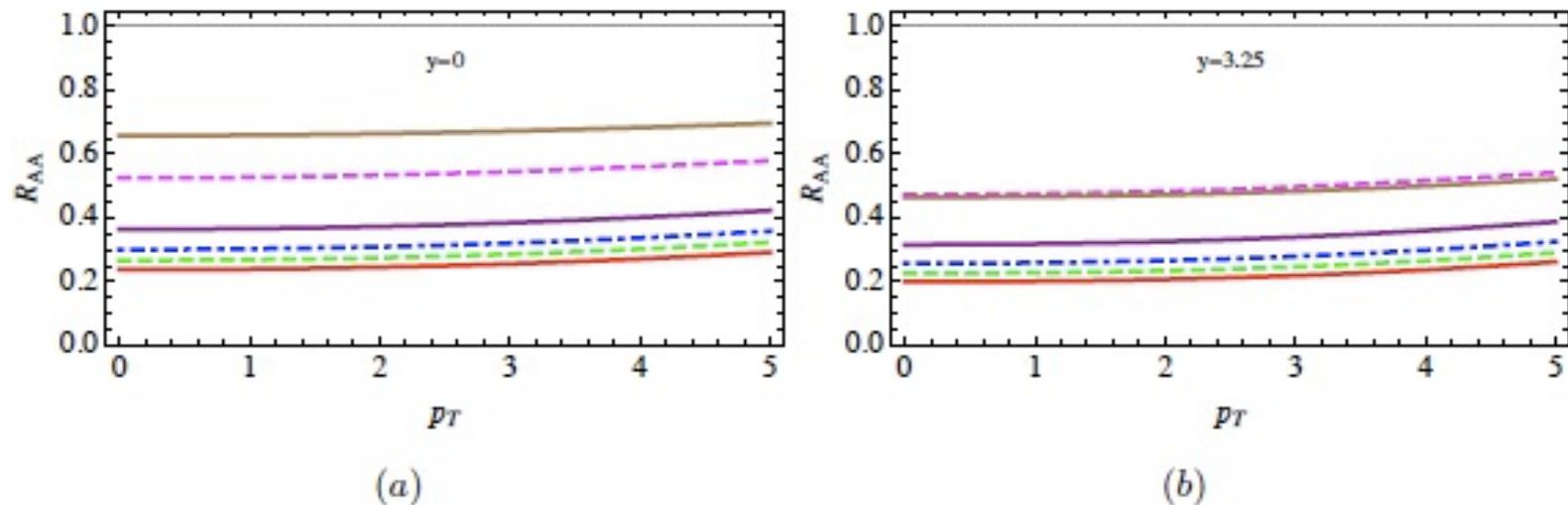
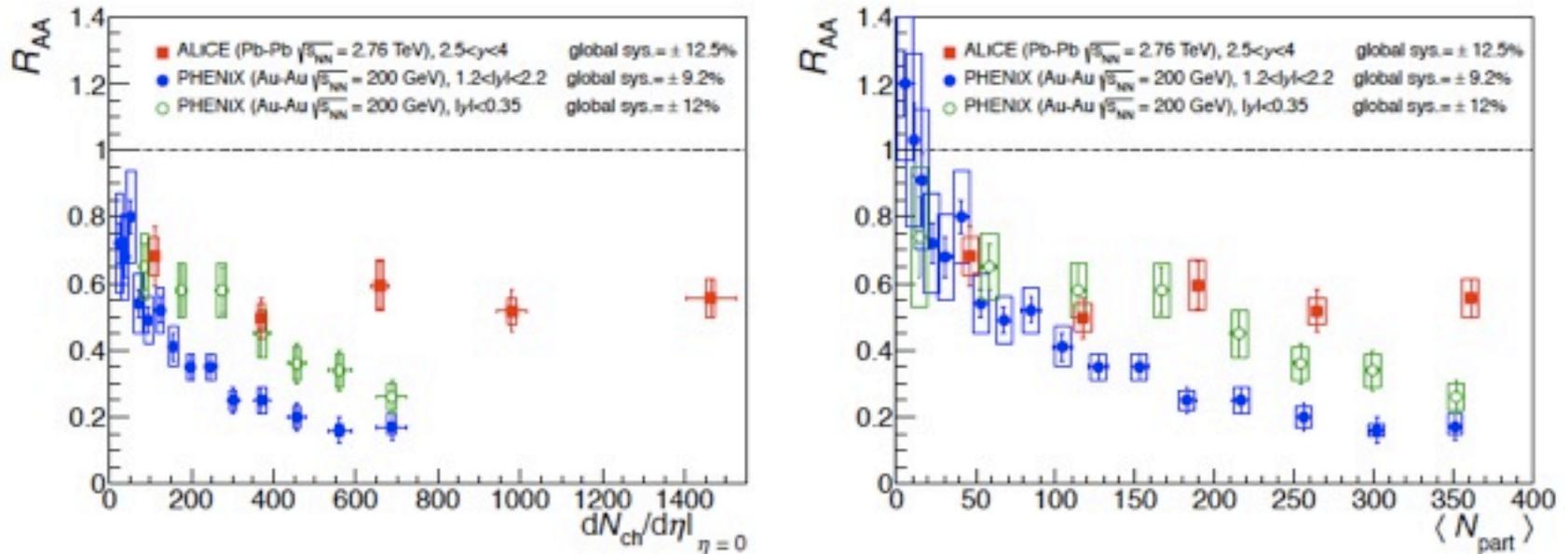


FIG. 6: (Color online). Nuclear modification factor for  $J/\psi$ 's vs  $p_{\perp}$  in GeV at  $\sqrt{s} = 7$  TeV in  $PbPb$  for rapidities (a)  $y = 0$  and (b)  $y = 3.25$ . Each line corresponds to a different centrality bin; from bottom to top: 0-10% (solid red), 10-20% (dashed green), 20-30% (dash-dotted blue), 30-50% (solid purple), 50-80% (dashed magenta) and in minbias  $pPb$  (solid brown).

DK, E.Levin, K.Tuchin,  
arxiv: 1205.1554

# The $J/\Psi$ production at LHC

Lecture by P. Braun-Munzinger



**Fig. 1:** (Color online) Inclusive  $J/\Psi$   $R_{AA}$  as a function of the mid-rapidity charged-particle density (left) and the number of participating nucleons (right) measured in Pb-Pb collisions at  $\sqrt{s_{NN}} = 2.76$  TeV compared to PHENIX results in Au-Au collisions at  $\sqrt{s_{NN}} = 200$  GeV at mid-rapidity and forward rapidity [4, 5, 20].

**Weaker suppression at LHC  
than at RHIC !?**

ALICE Coll.,  
arxiv: 1202.1383

# $J/\psi$ as a probe of QGP

Volume 178, number 4

PHYSICS LETTERS B

9 October 1986

## $J/\psi$ SUPPRESSION BY QUARK–GLUON PLASMA FORMATION ☆

T. MATSUI

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If high energy heavy ion collisions lead to the formation of a hot quark–gluon plasma, then colour screening prevents  $c\bar{c}$  binding in the deconfined interior of the interaction region. To study this effect, the temperature dependence of the screening radius, as obtained from lattice QCD, is compared with the  $J/\psi$  radius calculated in charmonium models. The feasibility to detect this effect clearly in the dilepton mass spectrum is examined. It is concluded that  $J/\psi$  suppression in nuclear collisions should provide an unambiguous signature of quark–gluon plasma formation.

# Helmut Satz and Tetsuo Matsui at BNL



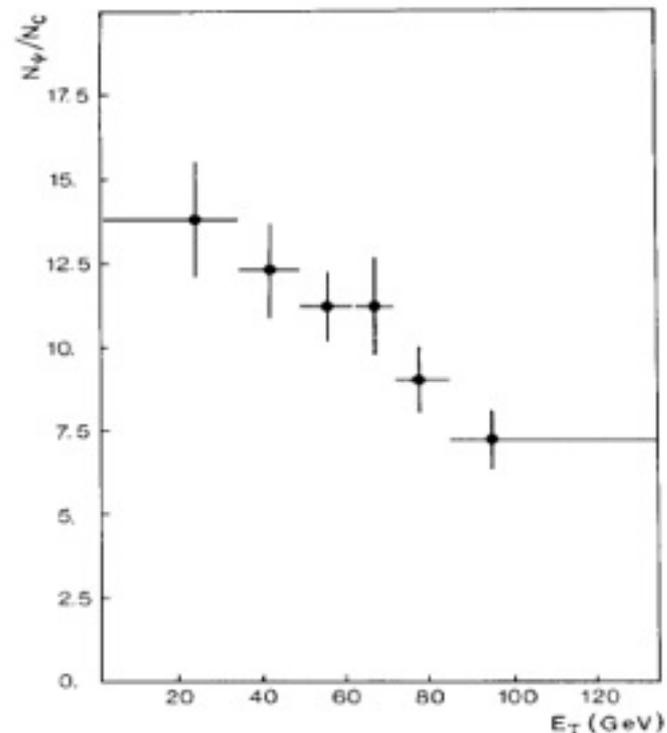
Tuesday, May 15, 2012

T. Matsui & H. Satz:

We thus conclude, that there appears to be no mechanism for  $J/\psi$  suppression in nuclear collisions except the formation of a deconfining plasma, and if such a plasma is produced, there seems to be no way to avoid  $J/\psi$  suppression.

NA38: the first observation of  $J/\psi$  suppression

6 April 1989

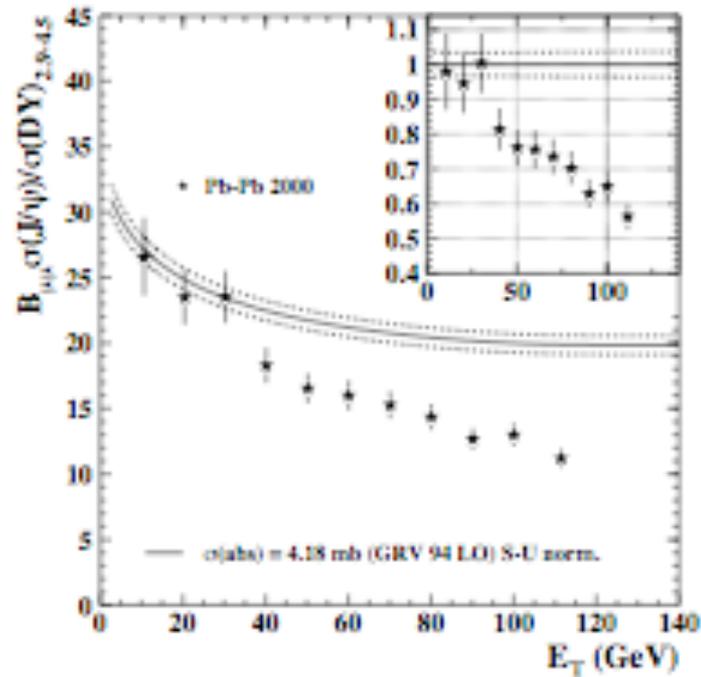
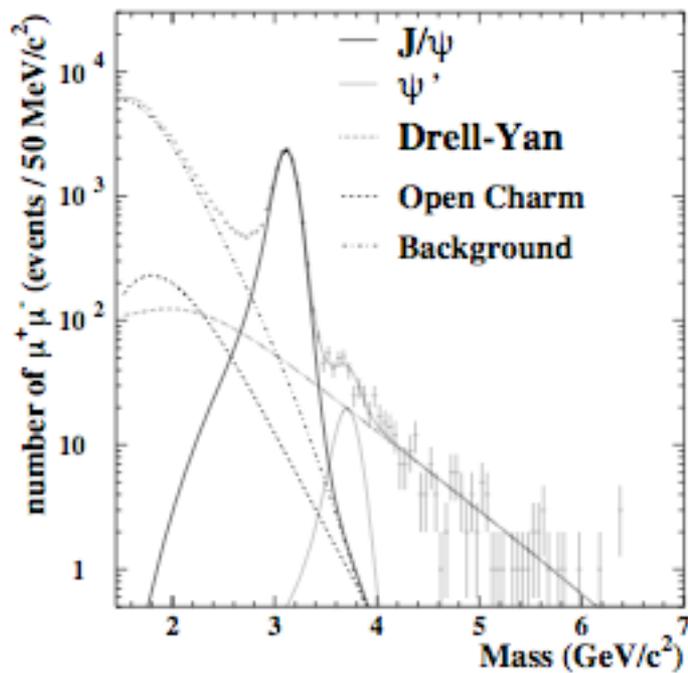


THE PRODUCTION OF  $J/\psi$   
IN 200 GeV/NUCLEON OXYGEN-URANIUM INTERACTIONS

NA38 Collaboration

# Experimental information

CERN: NA38/50/60 experiments



NA50 Coll., hep-ex/0412036

# J/Ψ suppression in the plasma

Heavy quarkonia are very sensitive to the properties of QCD matter; when Debye length becomes smaller than the size of quarkonium,

$$R_{\text{Debye}}(T) \sim 1/(gT) < R_{\text{Quarkonium}} \sim 1 / (\alpha_s M_H),$$

quarkonia are screened out of existence T. Matsui & H. Satz '86  
this happens when  $T \sim g M_H$

(what is the corresponding formula for strong coupling?)

However, even before that, when  $T \sim \varepsilon \sim \alpha_s^2 M_H$ ,  
quarkonia can be dissociated due to thermal activation

# What is the mechanism of dissociation?

In cold matter, dissociation rate is relatively small due to the softness of gluon distributions in confined matter, but it is large,  $O(1 \text{ fm}^{-1})$ , in hot QCD matter

DK & H. Satz '94

Dissociation mechanism - gluo-effect

E.Shuryak '78

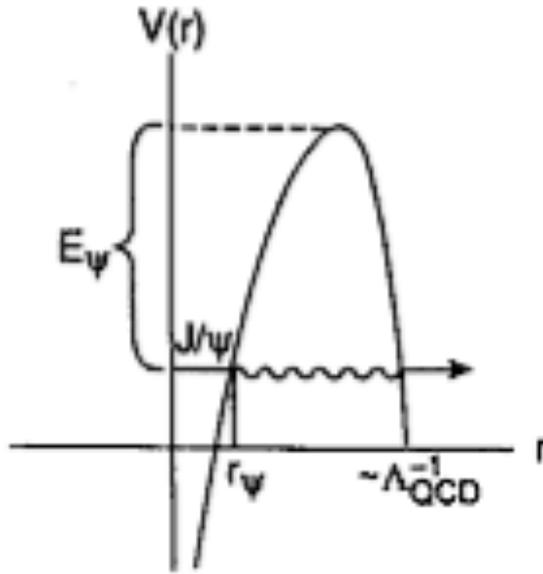
G.Bhanot, M.Peskin '79

dominates if  $\frac{\epsilon}{T} \gg 1$  (strong coupling regime)

Screening dominates if  $\frac{\epsilon}{T} \ll 1$  (weak coupling)

# What mechanism is more important?

DK, L.McLerran, H.Satz  
 hep-ph/9504338



$$R_{act} = \frac{1}{Z(T)} \frac{V}{L} \left( \frac{c}{\pi^2} MT^2 \right) e^{-\frac{E_{J/\psi}}{T}}$$

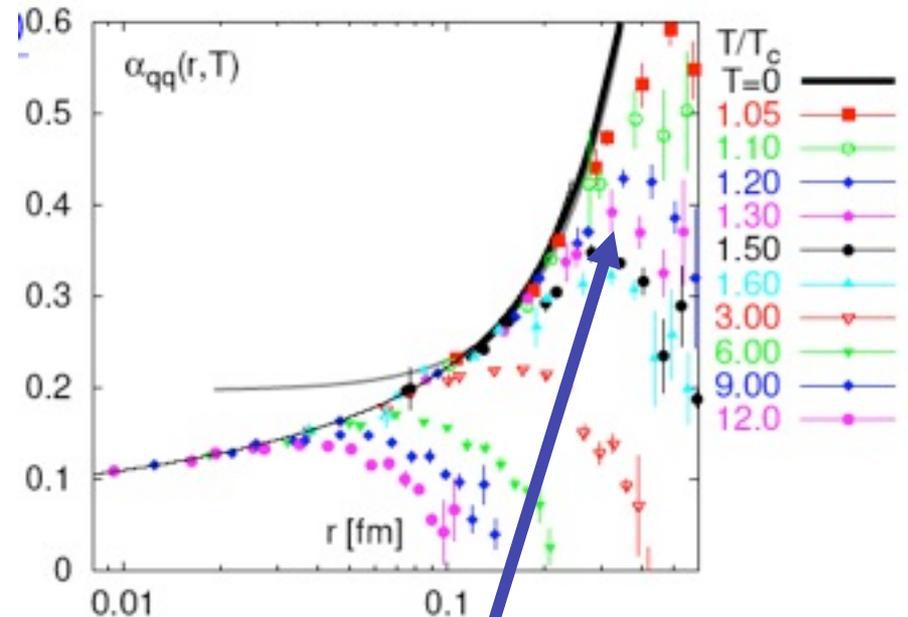
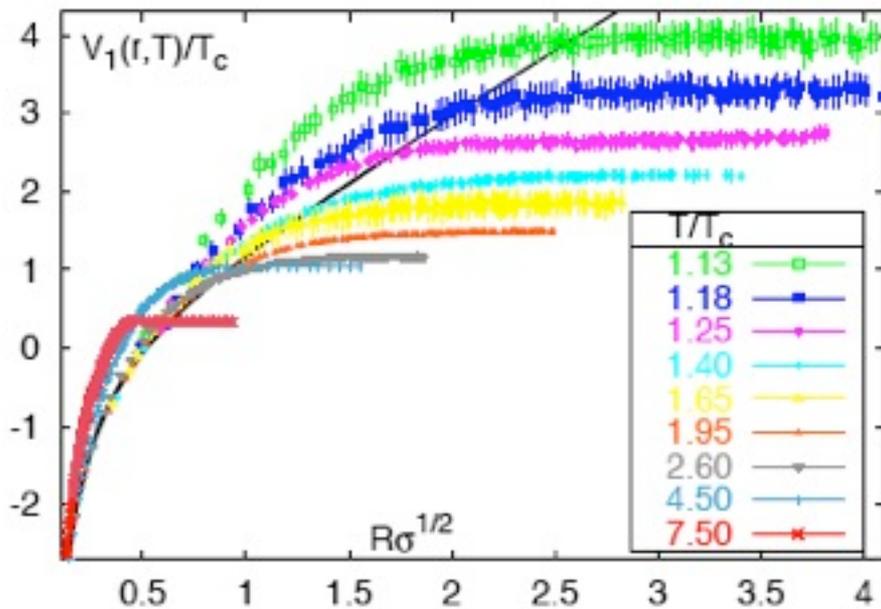
Weak coupling:

$$R_{act} = \frac{4}{L} \sqrt{\frac{T}{2\pi M}} = \frac{v(T)}{L}$$

Strong coupling:

$$R_{act} = \frac{(LT)^2}{3\pi} M e^{-E_{J/\psi}/T}$$

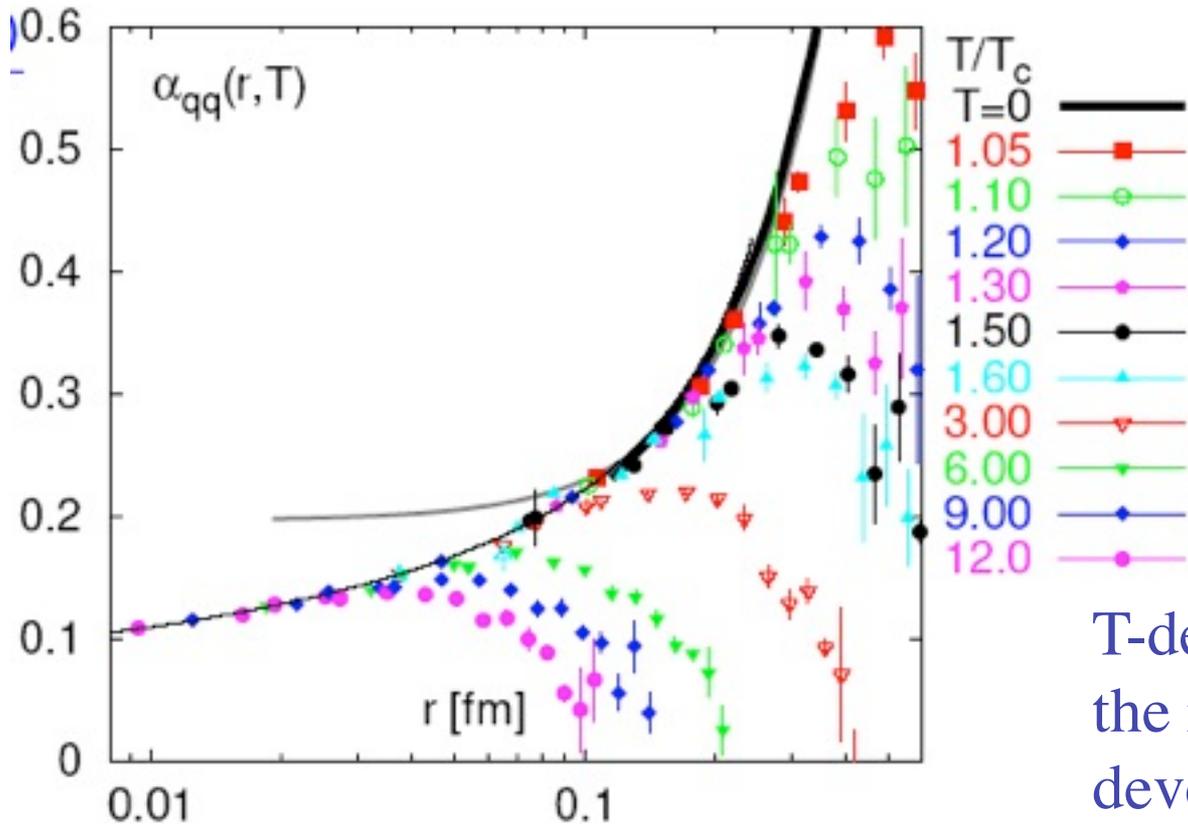
# Color screening and $J/\Psi$ suppression: lattice QCD results



O.Kaczmarek, F. Karsch, P.Petreczky,  
F. Zantow, hep-lat/0309121

Interaction energy  
exceeds the temperature -  
strong coupling!

# Screening in QGP

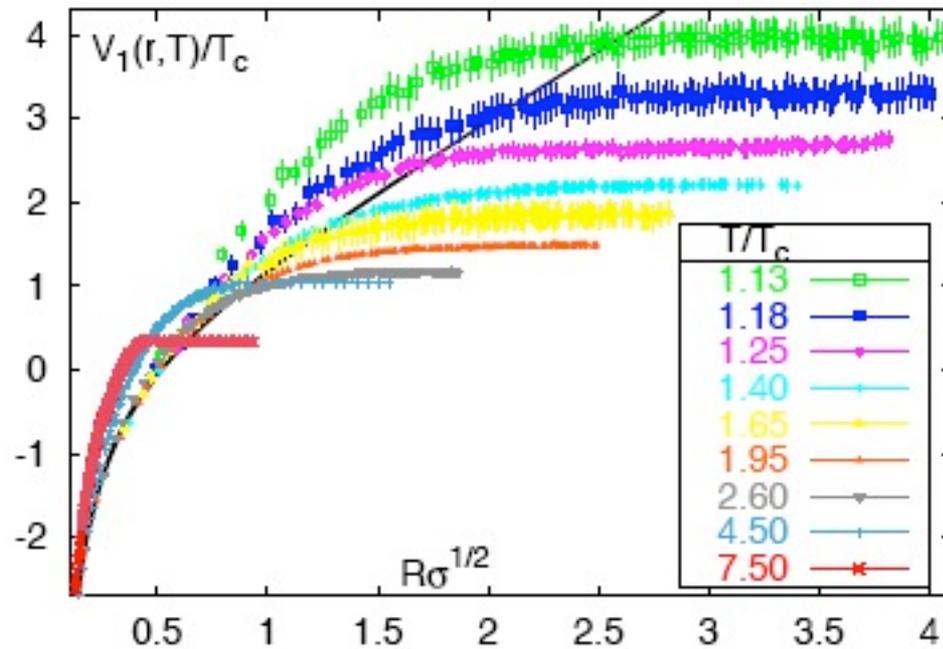


Strong force is  
**screened** by  
 the presence of  
 thermal gluons  
 and quarks

T-dependence of  
 the running coupling  
 develops in  
 the non-perturbative region  
 at  $T < 3 T_c$  ;  $\Delta E/T > 1$   
 - **“cold” plasma**

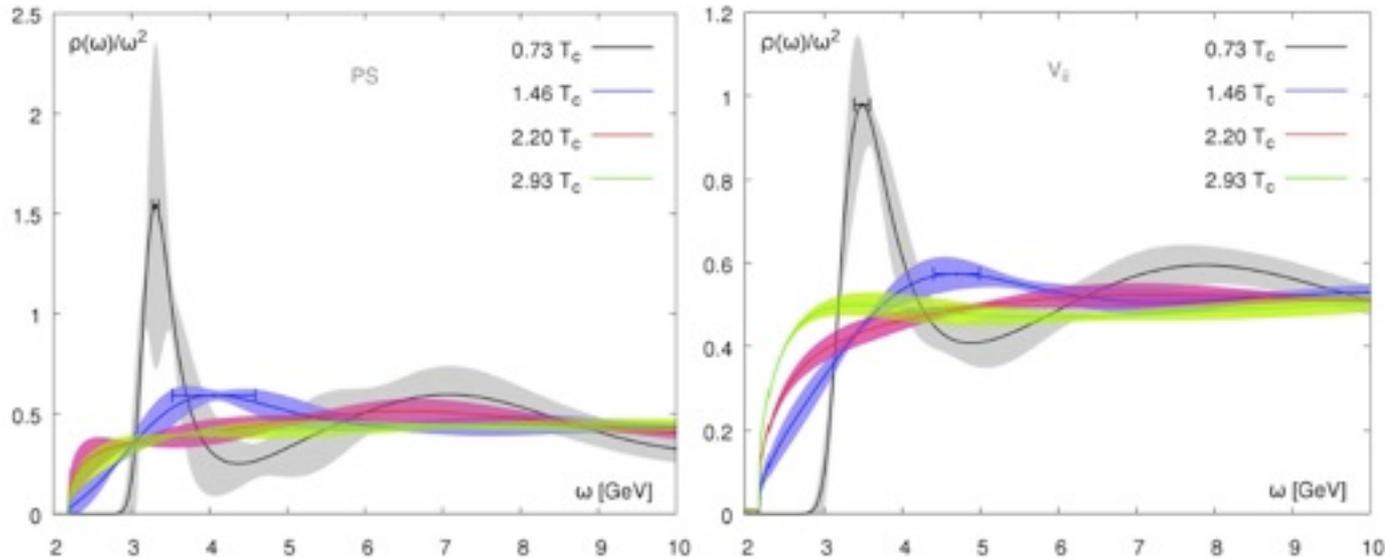
O.Kaczmarek, F. Karsch, P.Petreczky,  
 F. Zantow, hep-lat/0309121

# Heavy quark internal energy above $T_c$



O.Kaczmarek, F. Karsch, P.Petreczky,  
F. Zantow, hep-lat/0309121

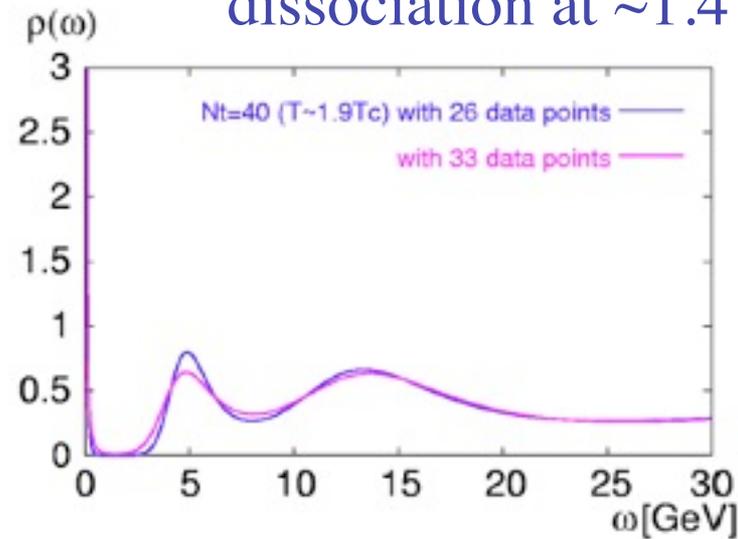
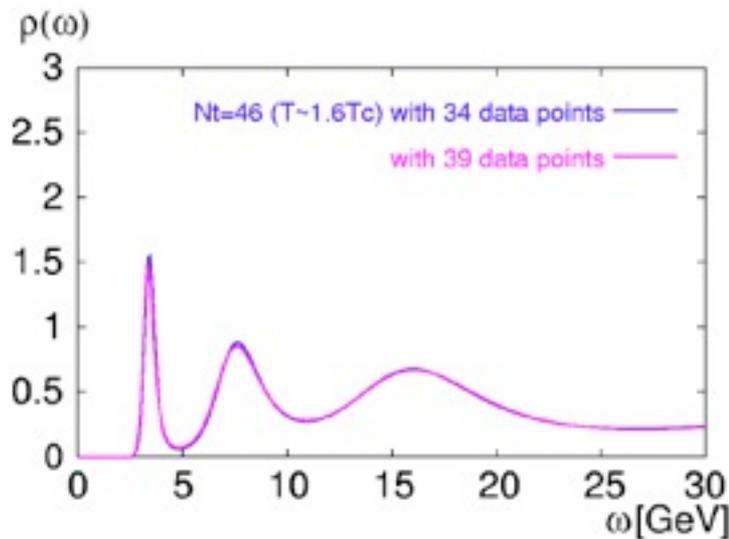
# J/Ψ above T<sub>c</sub>: lattice QCD



Lectures by  
H.-T. Ding,  
F.Karsch

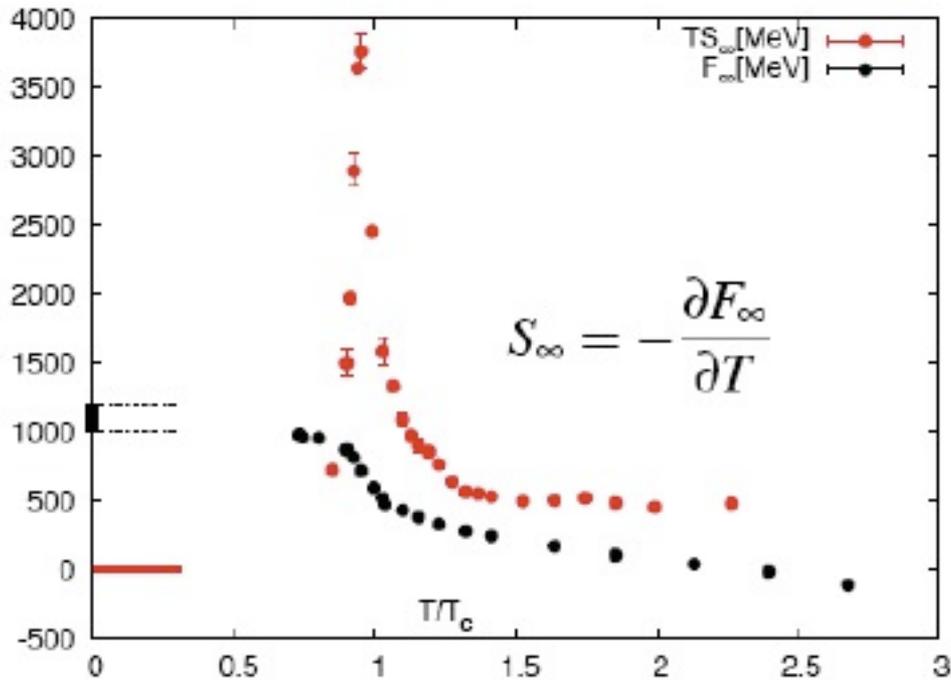
H.T.Ding et al,  
arxiv:1204.4945

dissociation at  $\sim 1.4 T_c$  ?



M.Asakawa,  
T.Hatsuda

Entropy: coupling to real states =>  
 non-instantaneous, non-local effective potential

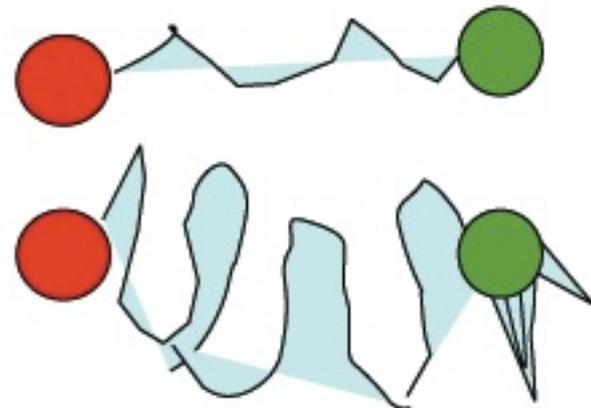


String contribution to  
 the black hole entropy:  
 a hint for understanding  
 better quarkonia  
 in the QCD plasma?

$$F = U - TS$$

$$\delta F = \left( \frac{\partial U}{\partial l} - T \frac{\partial S}{\partial l} \right) \delta l = 0$$

Kosterlitz-Thouless phase transition:  
 Frautschi, Polyakov



# AdS/CFT Correspondence:

## Conformal gauge theory is dual to gravity

The chain of ideas:

1. String model pre-dates QCD as a description of hadron spectrum and hadron scattering amplitudes  
(Regge poles, Veneziano amplitude, Hagedorn spectrum,...)
2. Quantum theory of strings cannot be made consistent in (3+1) dimensions; the minimum number of dimensions is 5.  
Also: massless spin 2 state - graviton?
3. It has long been expected that QCD in the strong coupling and large  $N$  is described by string theory  
(at large  $N$ , planar diagrams dominate;  
they describe worldsheets of strings)

4. How to make this string description consistent on the quantum level?

Add a 5th dimension to QCD and let gravity live there  
BUT: what is the metric?

$$ds^2 = R^2 w^2(z) ( dx^2_{3+1} + dz^2 )$$

what is the form of  $w(z)$ ?

5. Consider instead a conformal theory, such as maximally super-symmetric N=4 Yang-Mills; then the requirement of conformal invariance fixes the metric of the 5th dimension uniquely - it is an Anti- de Sitter space  $AdS_5$ :

invariance w.r.t.  $x \rightarrow \lambda x$  fixes  $w(z) = \frac{1}{z}$

supersymmetry -  $S_5$ , so the theory lives in  $AdS_5 \times S_5$

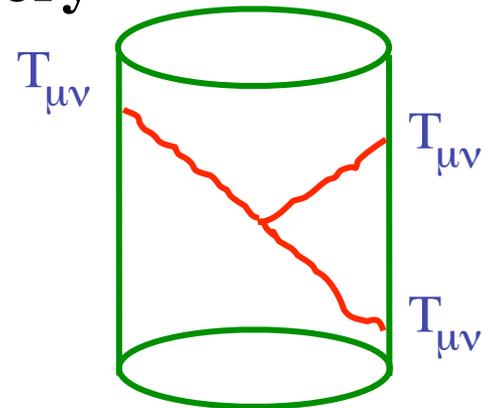
$$\boxed{N = 4 \text{ SU}(N) \text{ Yang-Mills theory}} = \boxed{\text{String theory on AdS}_5 \times S^5}$$

Radius of curvature

$$R_{S^5} = R_{AdS_5} = (g_{YM}^2 N)^{1/4} l_s$$

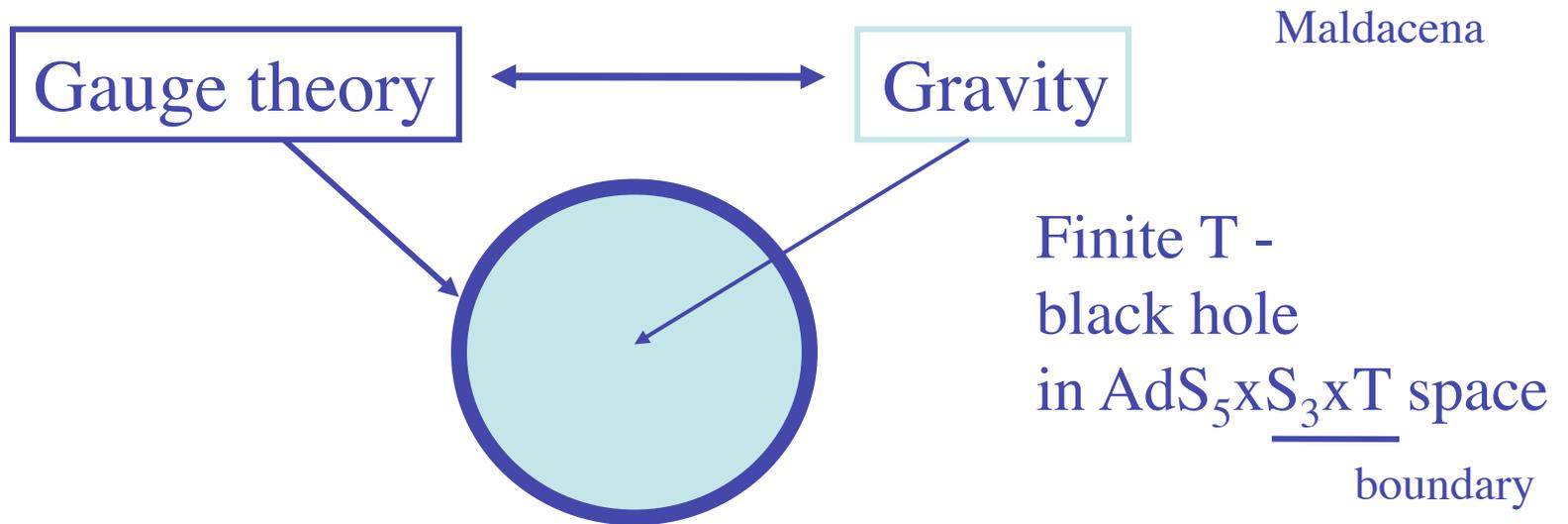
### Duality:

$g^2 N$  small  $\rightarrow$   $R$  small  $\rightarrow$  perturbation theory  
 $g^2 N$  large  $\rightarrow$   $R$  large  $\rightarrow$  classical gravity



# Color screening and black holes?

One new idea: use a mathematical correspondence between a conformal gauge theory and gravity in AdS space

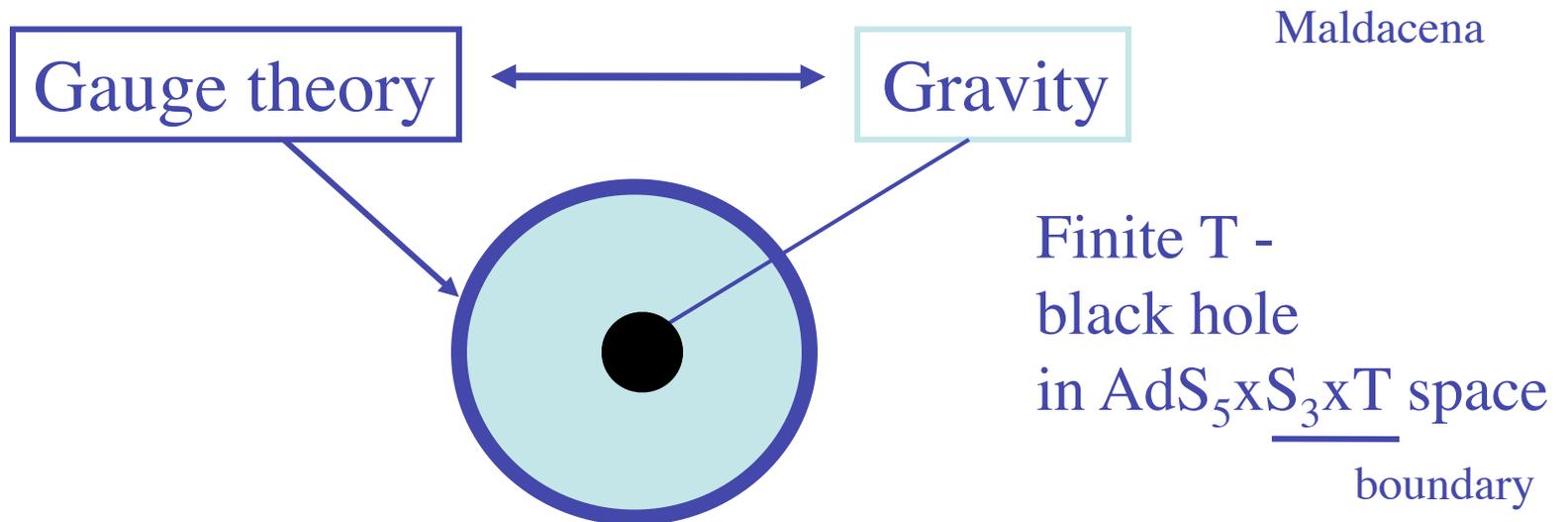


Anti de Sitter space - solution of Einstein's equations with a negative cosmological constant  $\Lambda$   
(de Sitter space - solution with a positive  $\Lambda$  (inflation))

Witten; Polyakov;  
Gubser, Klebanov;  
Son, Starinets, Kovtun...

# Color screening and black holes?

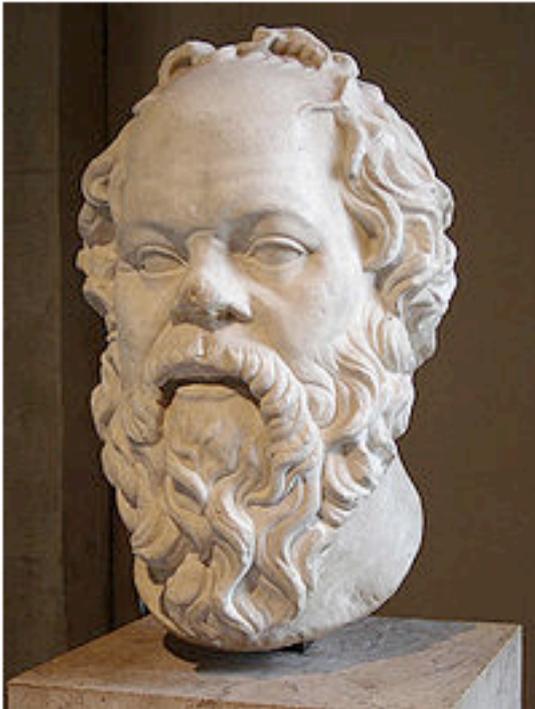
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# The metaphor of the cave, 380 B.C.



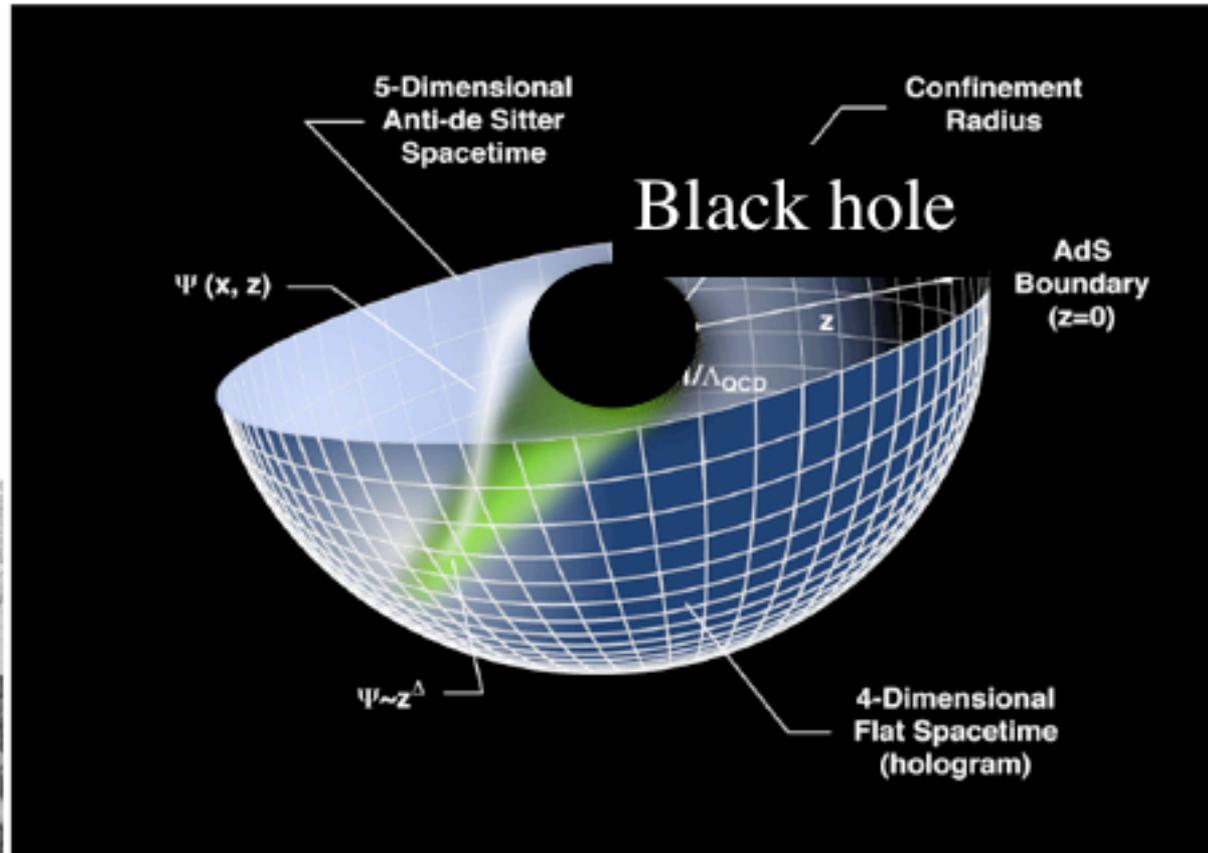
**Socrates (Σωκράτης)**  
**469 - 399 B.C.**

“Physical objects and physical events are only "shadows" of their ideal or perfect forms, and exist only to the extent that they instantiate the perfect versions of themselves”  
Socrates, in Plato’s “Republic”



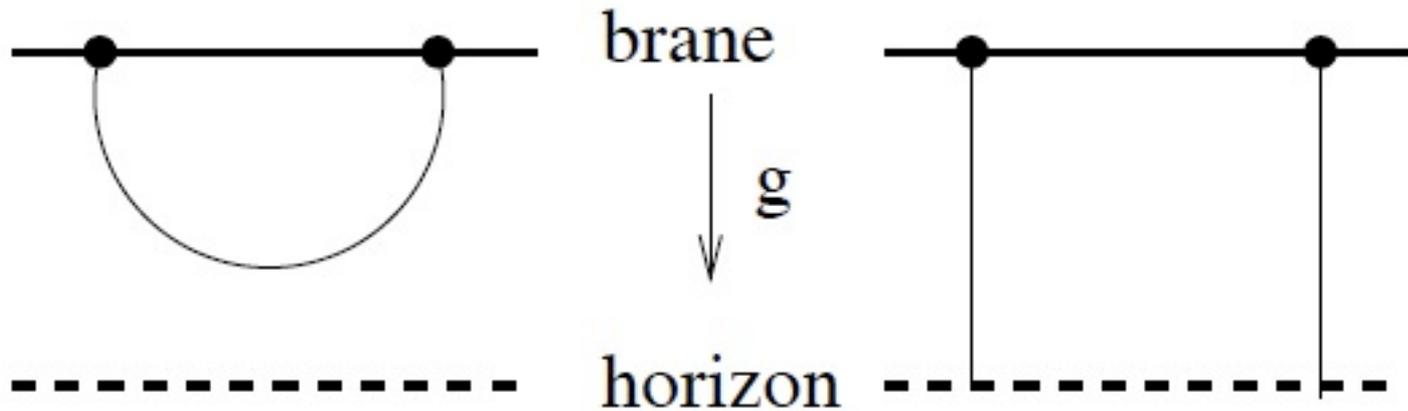
“The prisoners would take the shadows to be real things and the echoes to be real sounds, not just reflections of reality, since they are all they had ever seen or heard.”

# The metaphor of the cave, 2011 A.D.



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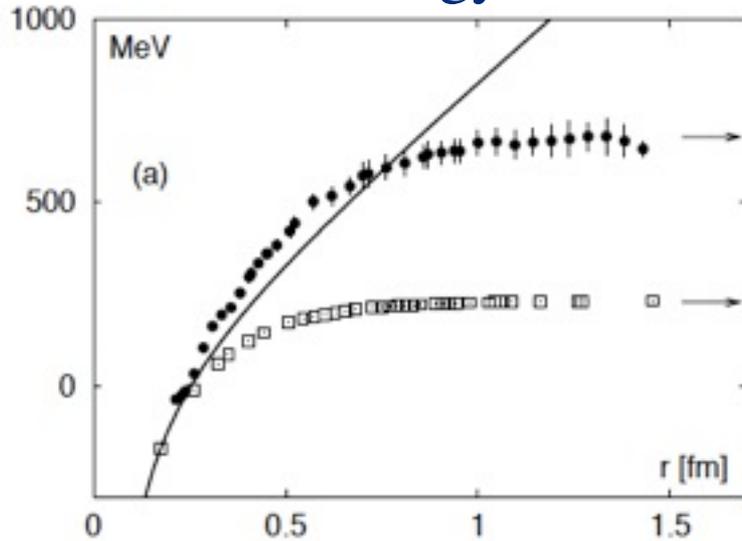
# Entropy and color screening: an insight from holography



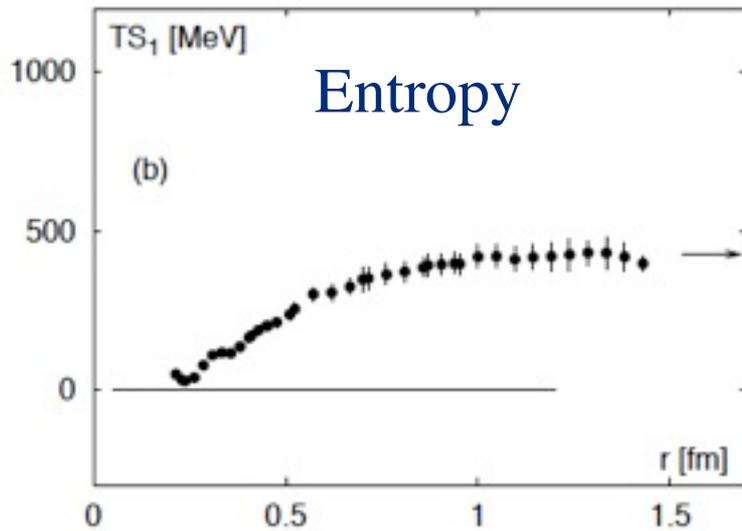
e.g., Shuryak, Zahed

# Color screening and entropy

## Internal energy



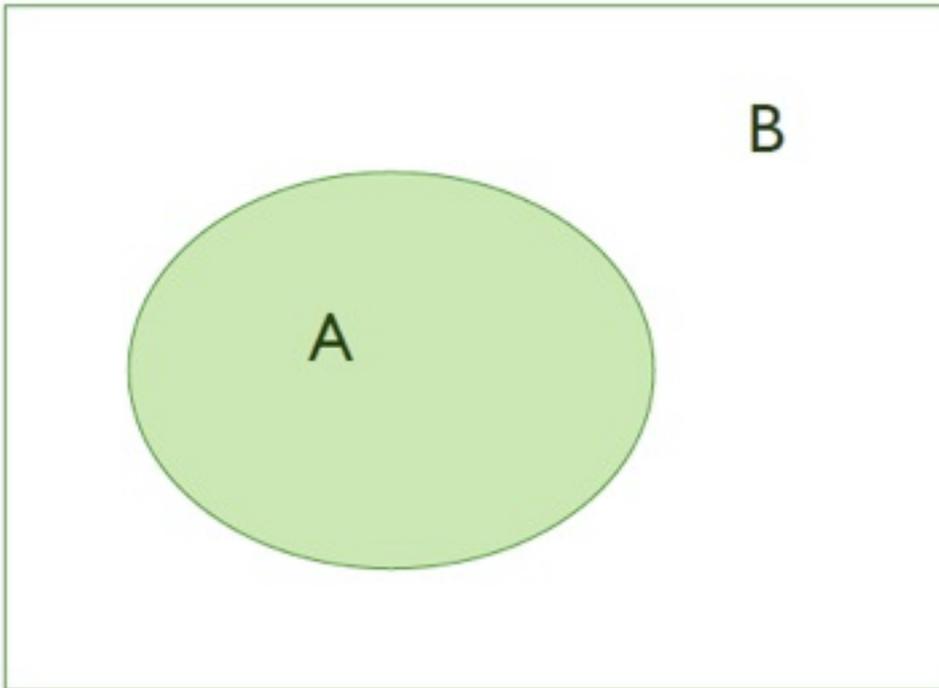
## Entropy



Kaczmarek, Zantow,  
arxiv:0506019

# Confinement and entanglement entropy

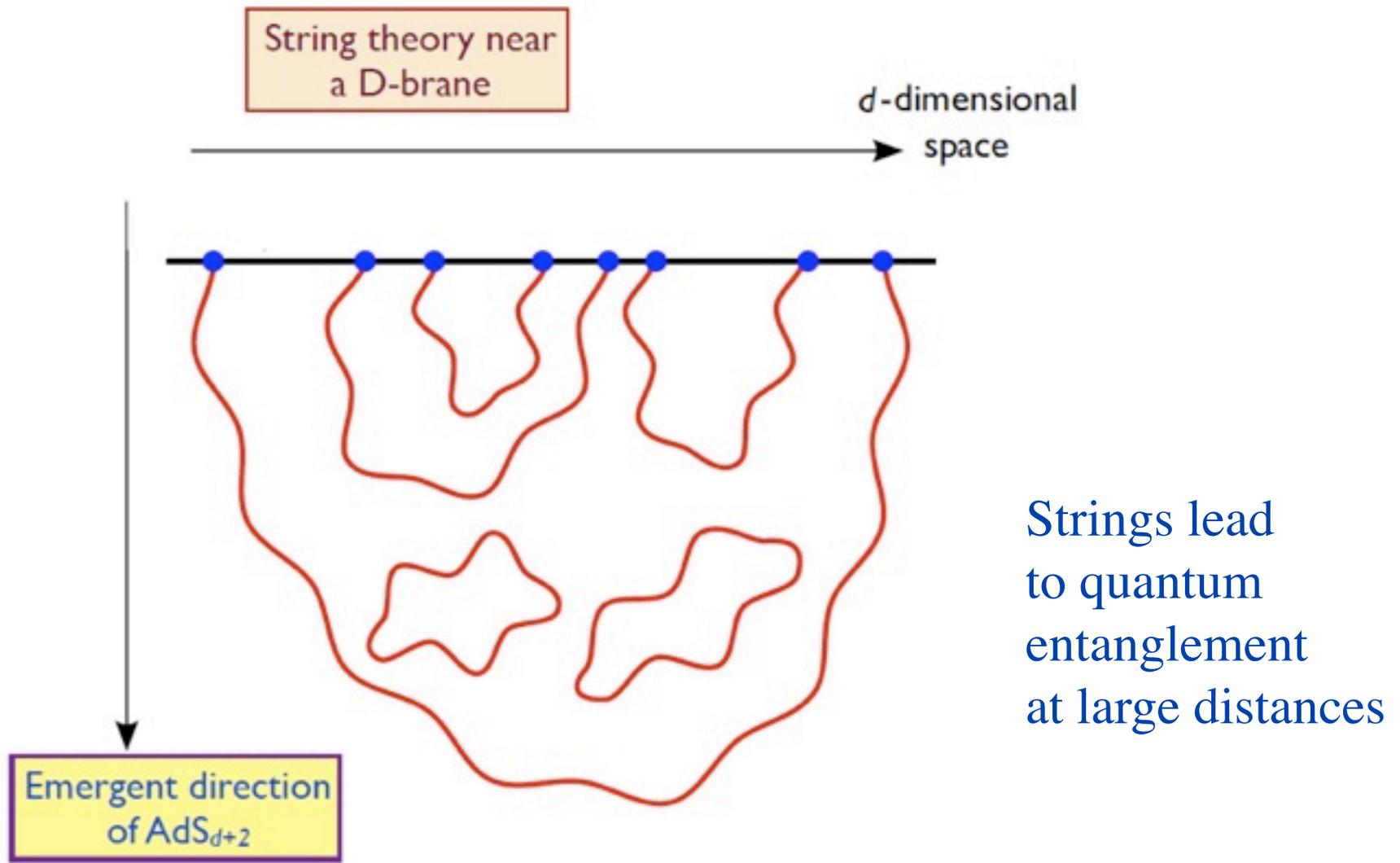
$$\rho_A = \text{Tr}_B \rho, \text{ where } \rho = |\Psi\rangle\langle\Psi|$$



Entanglement entropy:

$$S_E = -\text{Tr}(\rho_A \ln \rho_A)$$

# Entanglement entropy and holography

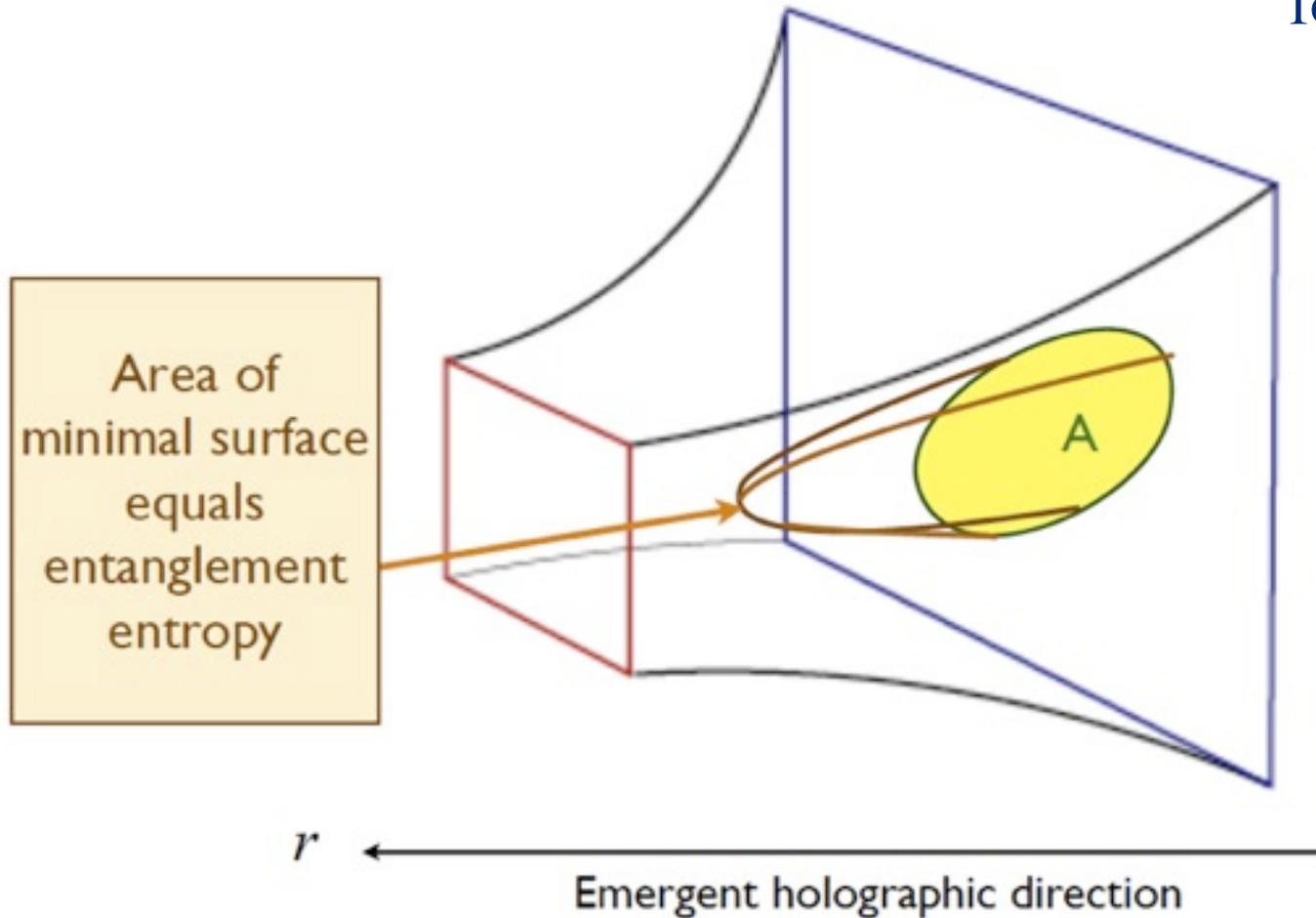


S. Sachdev, arxiv:1203.4565

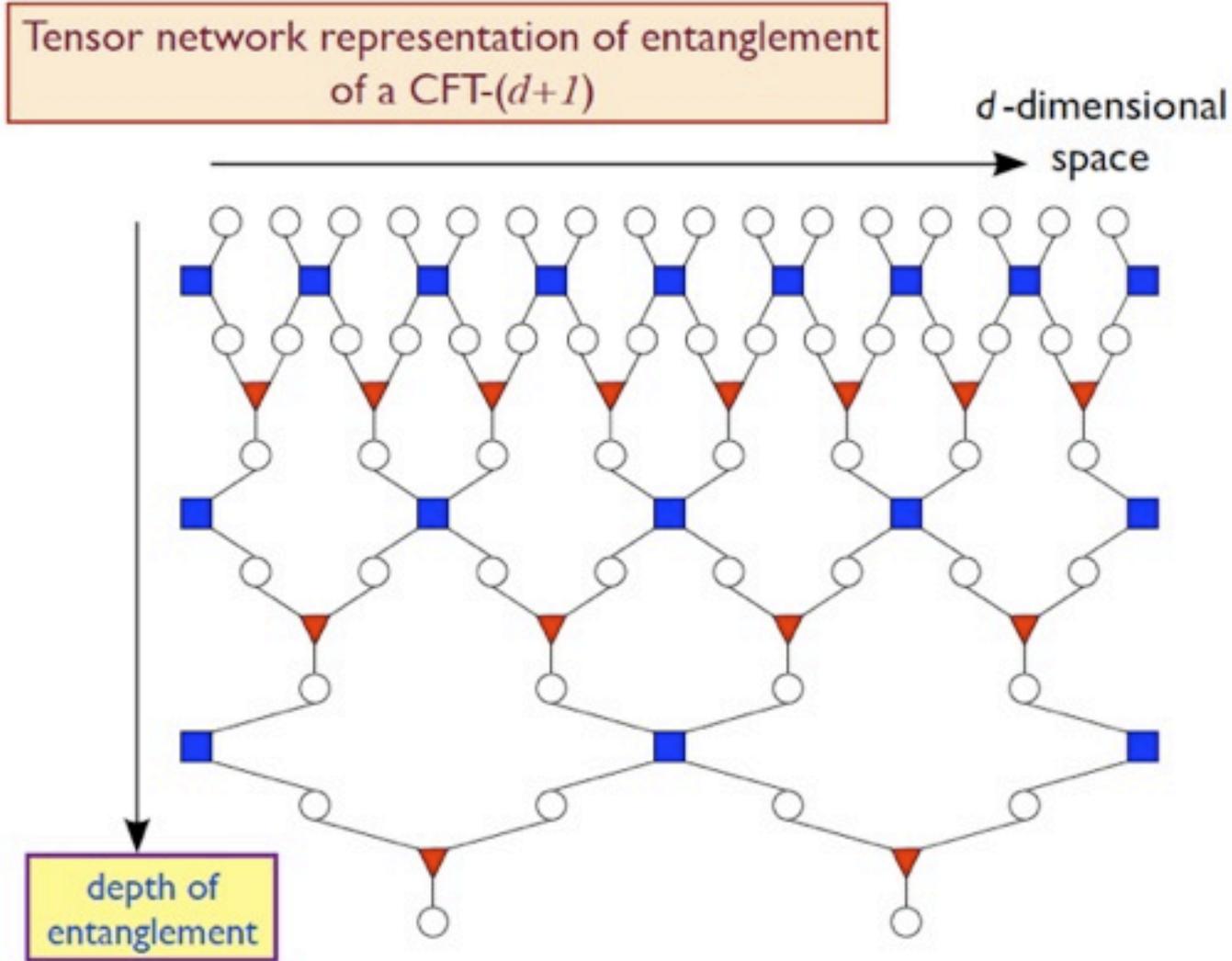
52

# Entanglement entropy and holography

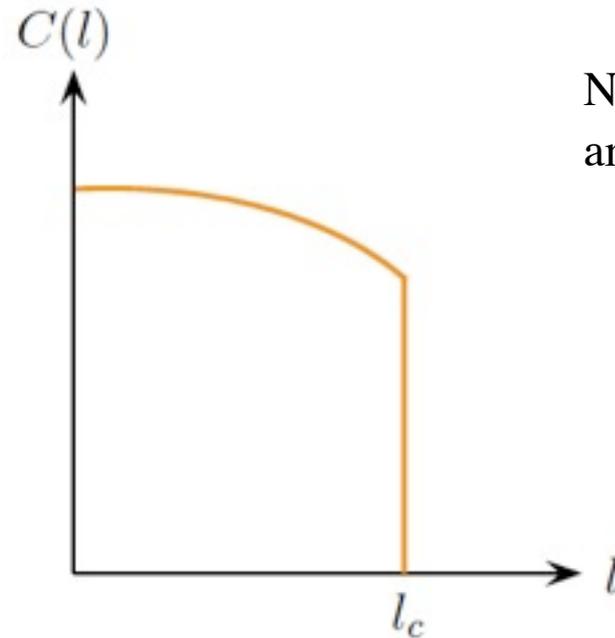
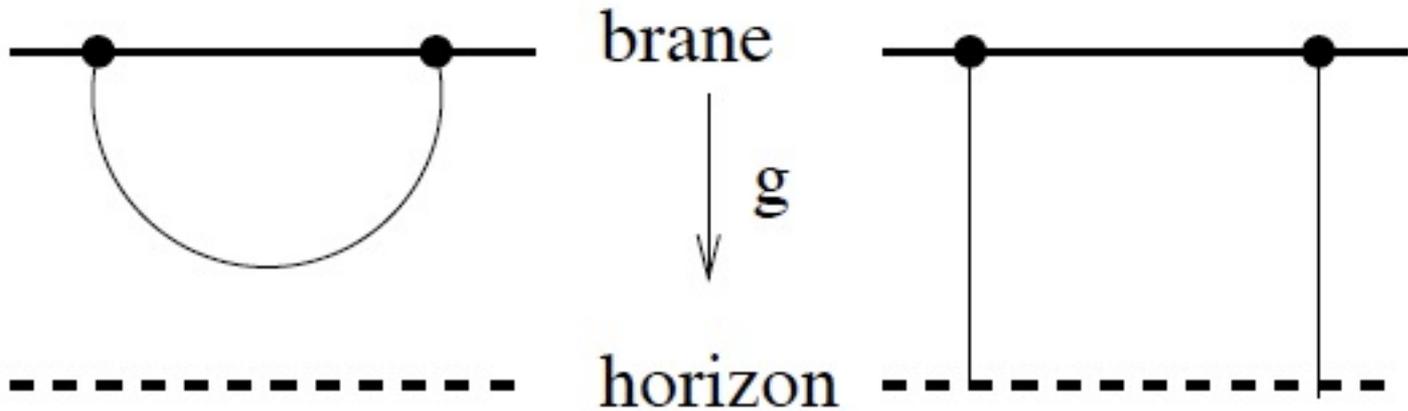
Ryu-Takanayagi  
formula



# Entanglement entropy and holography



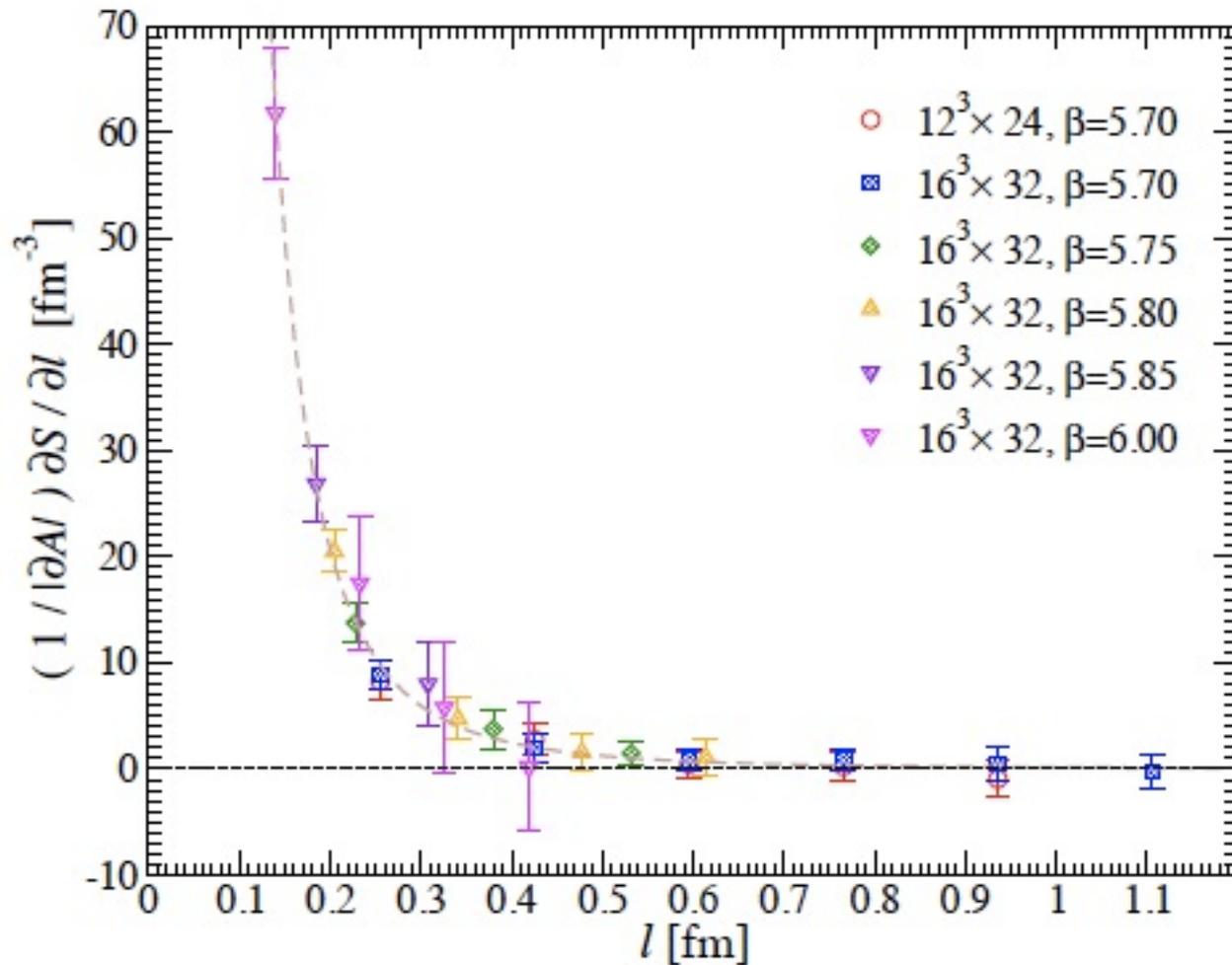
# Entanglement entropy and color screening



Nishioka,Ryu,Takayanagi,  
arxiv:0905.0932

$$C(l) \equiv \frac{l^d}{V} \frac{dS_A(l)}{dl}$$

# Entanglement entropy and deconfinement



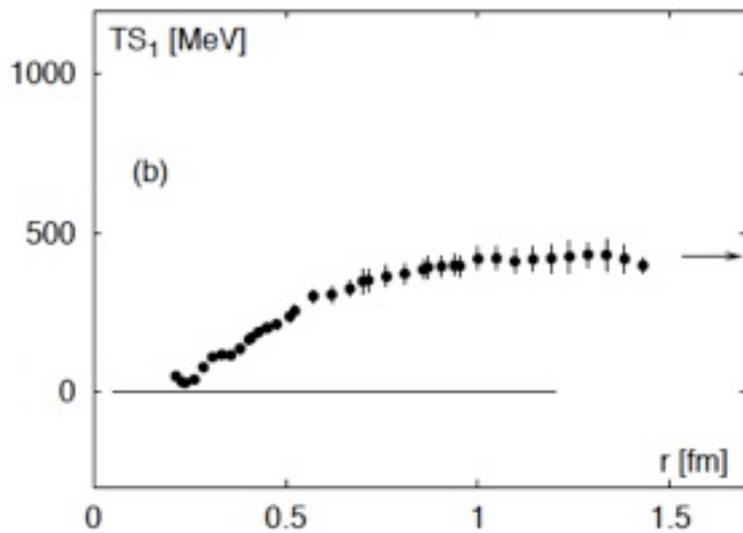
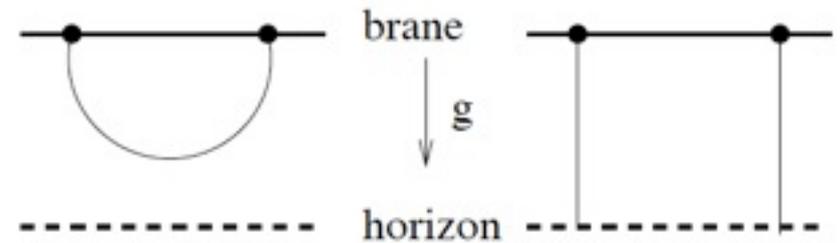
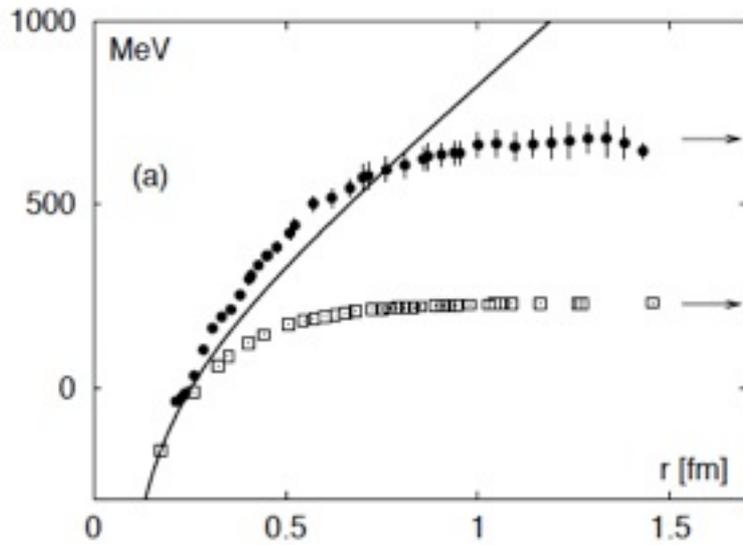
Nakagawa, Nakamura,  
Motoki, Zakharov,  
arxiv:0911.2596

also:

Buividovich, Polikarpov;

Velytsky; ....

# Entanglement entropy and deconfinement



# Summary

- **Using the heavy quarkonium as a probe of QCD matter appeared to be a very productive idea**
- **25 years later, still a very active field of research**

# Summary

- **Using the heavy quarkonium as a probe of QCD matter appeared to be a very productive idea**
- **25 years later, still a very active field of research**

**In other words, we still do not understand a thing....**

**but we are not losing hope!**