

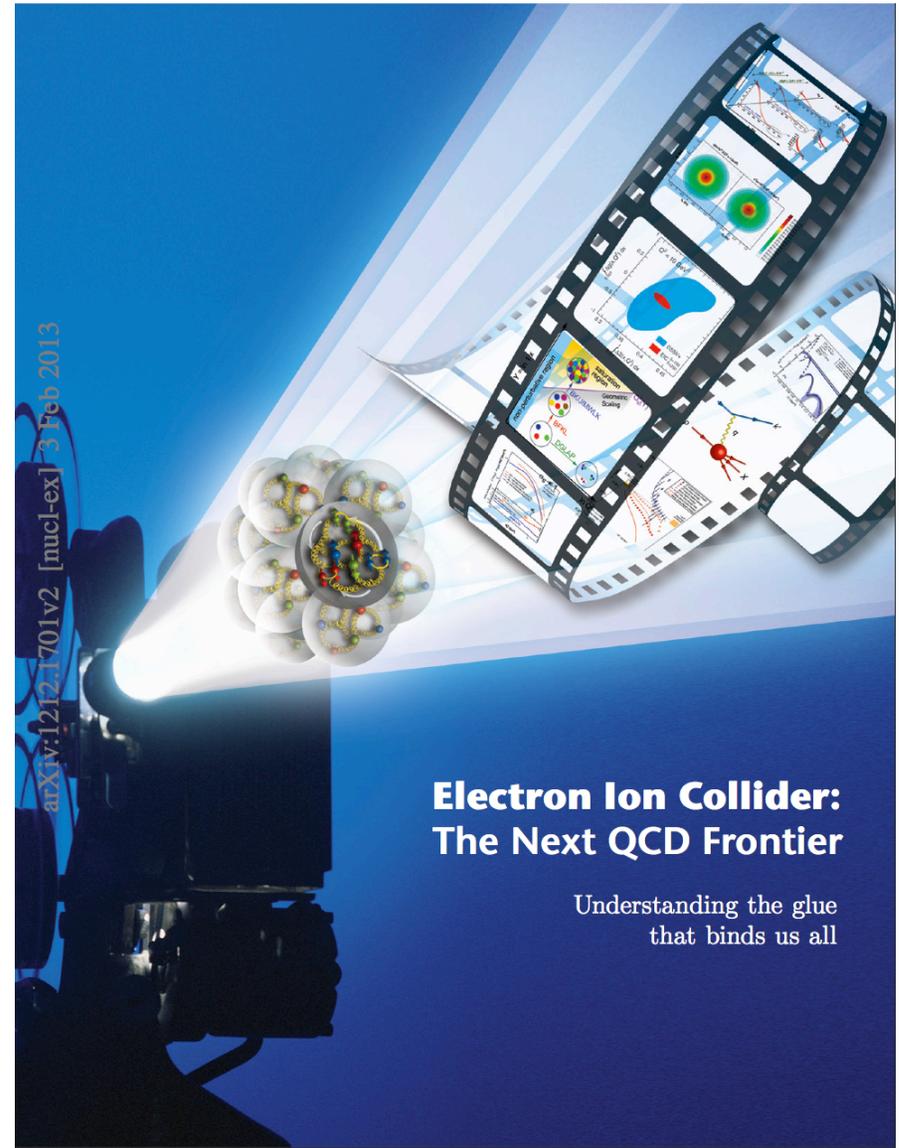
# QCD at EIC

Yuri Kovchegov

The Ohio State University

# Electron-Ion Collider (EIC) White Paper

- EIC WP was finished in late 2012 + 2<sup>nd</sup> edition in 2014
- A several-year effort by a 19-member committee + 58 co-authors
- arXiv:1212.1701 [nucl-ex]
- EIC can be realized as eRHIC (BNL) or as ELIC (JLab)



# QCD at EIC Physics Topics

- Spin and Nucleon Structure
  - Spin of a nucleon
  - Transverse momentum distributions (TMDs)
  - Spatial imaging of quarks and gluons (GPDs)
- QCD Physics in a Nucleus
  - High gluon densities and saturation
  - Quarks and Gluons in the Nucleus
  - Connections to  $p+A$ ,  $A+A$ , and cosmic ray physics

# The Big Picture

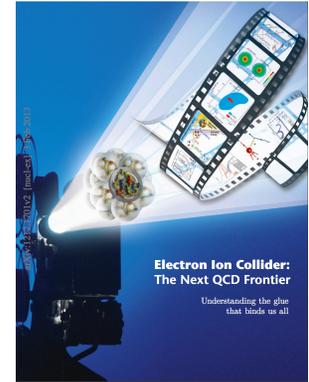
# Fundamental Questions in QCD

- Confinement, chiral symmetry breaking, quantitative understanding of hadron masses, structure of the proton and the nucleus.
- QCD under extreme conditions: finite- $T$  (heavy ions, Early Universe), finite- $\mu$  (neutron stars), high energy QCD asymptotics.

# Fundamental Questions of QCD **at EIC**

- Confinement, chiral symmetry breaking, quantitative understanding of hadron masses, **structure of the proton and the nucleus.**
- QCD under extreme conditions: finite-T (heavy ions, Early Universe), finite- $\mu$  (neutron stars), **high energy QCD asymptotics.**

# Big Questions EIC Would Address



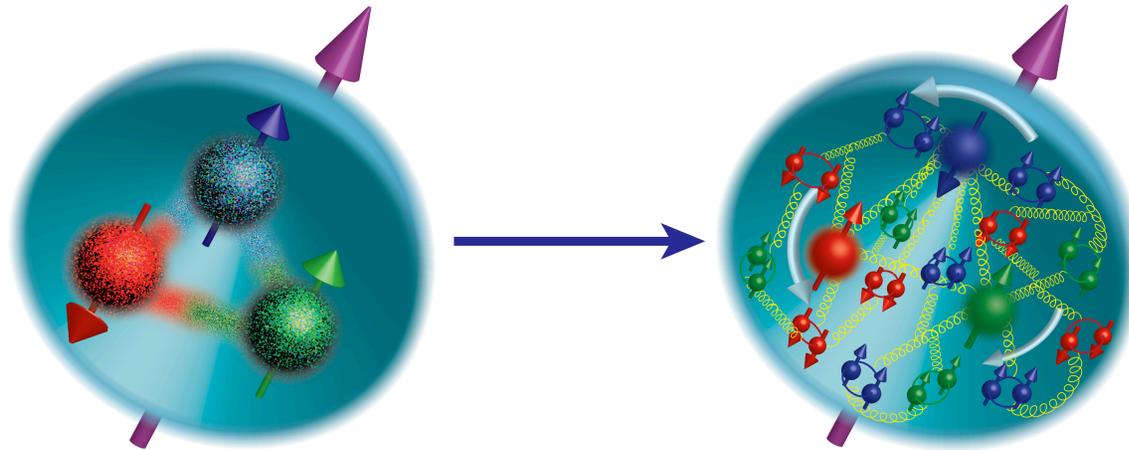
- How are the sea quarks and gluons, and their spins, distributed in space and momentum inside the nucleon?
- Where does the saturation of gluon densities set in? What is the dynamics? Is it universal?
- How does the nuclear environment affect the distribution of quarks and gluons and their interactions in nuclei?

# Spin and Nucleon Structure

# Fundamental Questions in Spin and Nucleon Structure

- What is the dynamical origin of sea quarks and gluons inside the proton?
- How does the proton spin originate at the microscopic level?
- How is hadron structure influenced by chiral symmetry and its breaking?
- How does confinement manifest itself in the structure of hadrons?

# Proton Spin



Our understanding of nucleon spin structure has evolved:

- In the 1980's the proton spin was thought of as a sum of constituent quark spins (left panel)
- Currently we believe that the proton spin is a sum of the spins of valence and sea quarks and of gluons, along with the orbital angular momenta of quarks and gluons (right panel)

# Proton Spin Puzzle

- Helicity sum rule:  $\frac{1}{2} = S_q + L_q + S_g + L_g$

with the net quark and gluon spin

$$S_q(Q^2) = \frac{1}{2} \int_0^1 dx \Delta\Sigma(x, Q^2) \quad S_g(Q^2) = \int_0^1 dx \Delta G(x, Q^2)$$

- The helicity parton distributions are

$$\Delta f(x, Q^2) \equiv f^+(x, Q^2) - f^-(x, Q^2)$$

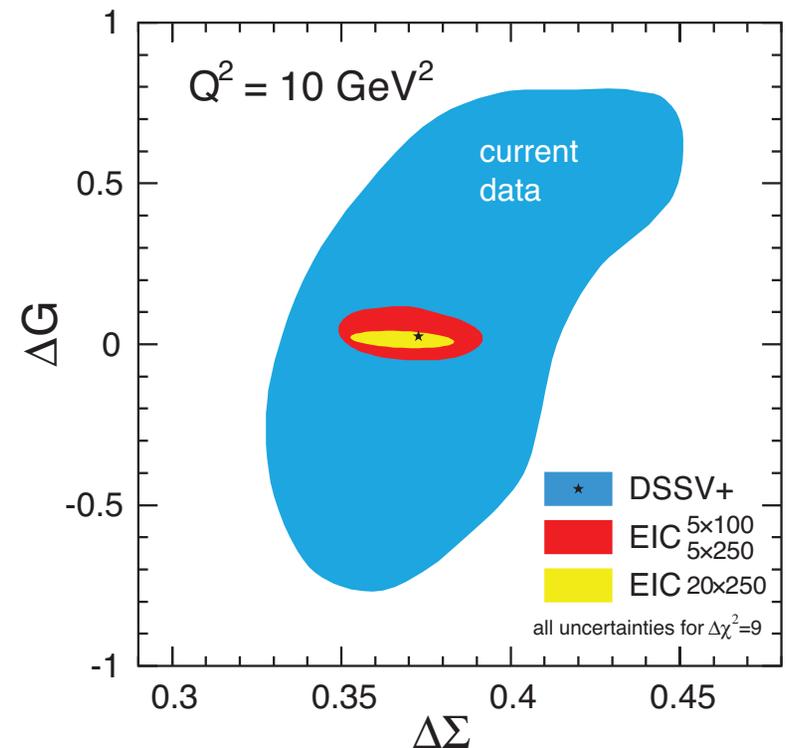
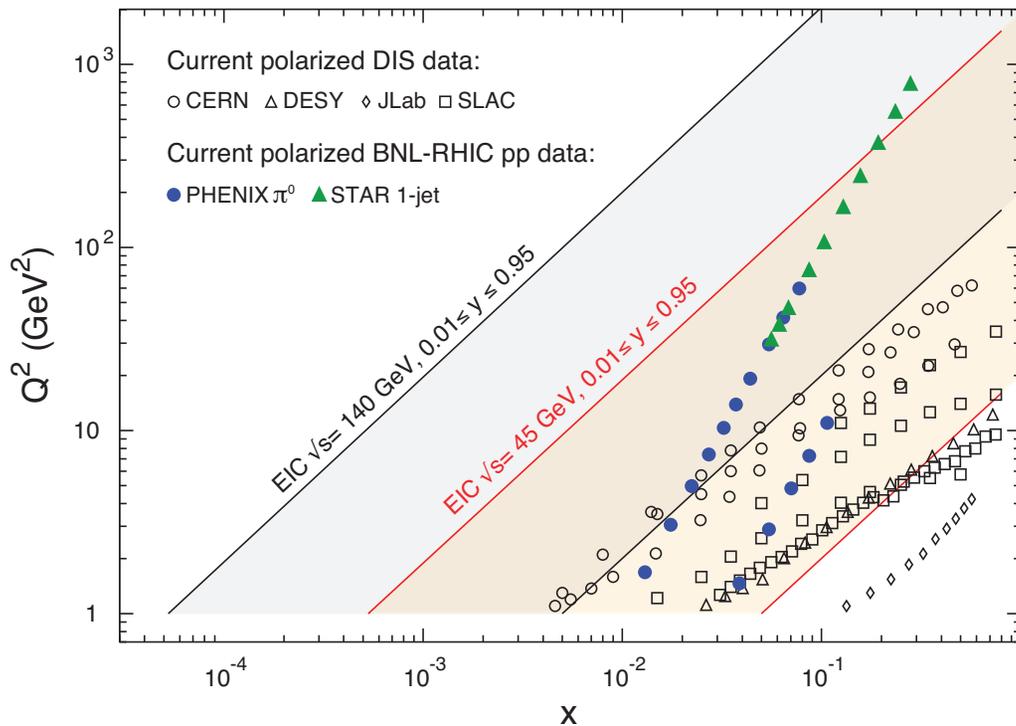
with the net quark helicity distribution

$$\Delta\Sigma \equiv \Delta u + \Delta\bar{u} + \Delta d + \Delta\bar{d} + \Delta s + \Delta\bar{s}$$

- $L_q$  and  $L_g$  are the quark and gluon orbital angular momenta

# EIC & Spin Puzzle

- Parton helicity distributions are sensitive to low-x physics.
- EIC would have an unprecedented low-x reach for a spin DIS experiment, allowing to pinpoint the values of quark and gluon contributions to proton's spin:

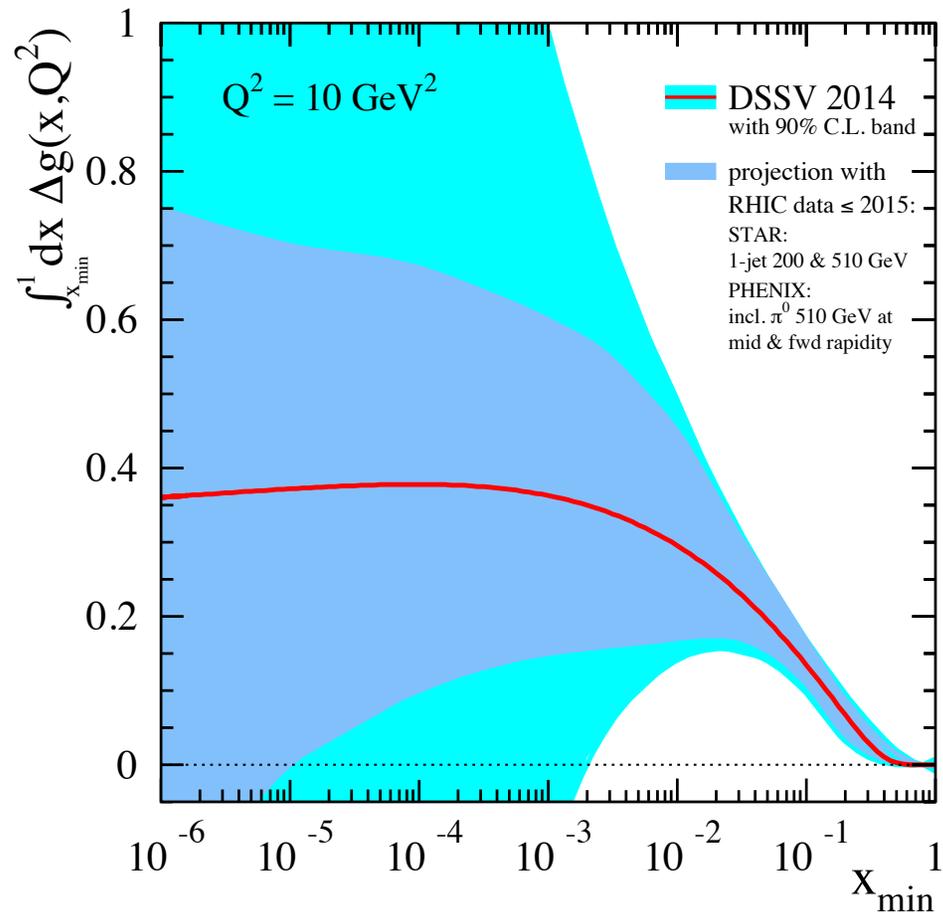


- $\Delta G$  and  $\Delta \Sigma$  are integrated over  $x$  in the  $0.001 < x < 1$  interval.

# Gluon Polarization

Recent data from RHIC appears to indicate that the net proton spin carried by the gluons  $S_g$  is non-zero, and in fact mainly comes from the small- to moderate- $x$  region. EIC would help to measure gluon polarization at small  $x$  with unprecedented precision.

$$S_g(Q^2) = \int_0^1 dx \Delta G(x, Q^2)$$



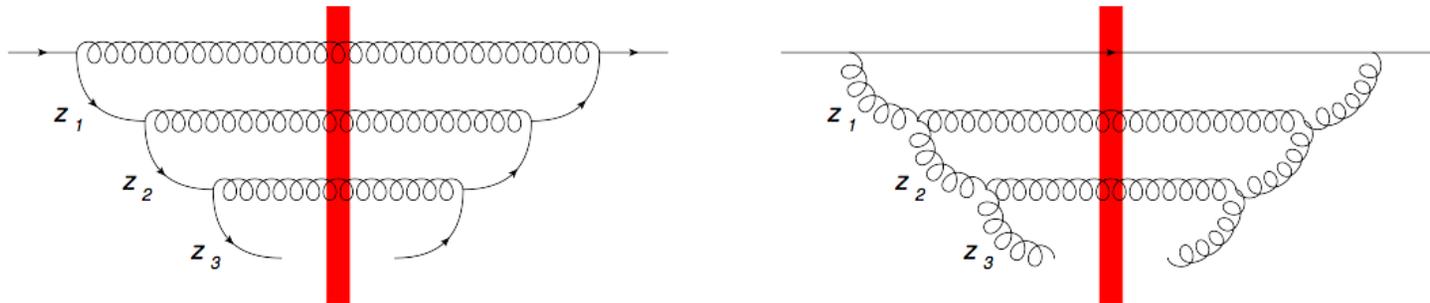
# Helicity PDFs at Small x: Theory Expectations

- Summing up mixing quark and gluon ladders yields

$$\Delta\Sigma \sim \left(\frac{1}{x}\right)^{\omega_+} \quad S_q(Q^2) = \frac{1}{2} \int_0^1 dx \Delta\Sigma(x, Q^2)$$

with

$$\omega_+ = \sqrt{\frac{\alpha_s}{2\pi N_c}} \sqrt{9 N_c^2 - 1 + \sqrt{(1 + 7 N_c^2)^2 + 16 N_c N_f (1 - N_c^2)}}$$



- The numbers are encouraging ( $\alpha_s=0.3$ ,  $N_c=N_f=3$ ):  $\Delta\Sigma \sim \left(\frac{1}{x}\right)^{1.46}$
- But: need to include the non-ladder graphs (see talk by M. Sievert).

# What to Expect

- Small- $x$  evolution for the  $g_1$  structure function was considered by Bartels, Ermolaev and Ryskin in '96.

- Including the mixing of quark and gluon ladders, they obtained

$$\Delta\Sigma \sim g_1 \sim \left(\frac{1}{x}\right)^{z_s \sqrt{\frac{\alpha_s N_c}{2\pi}}}$$

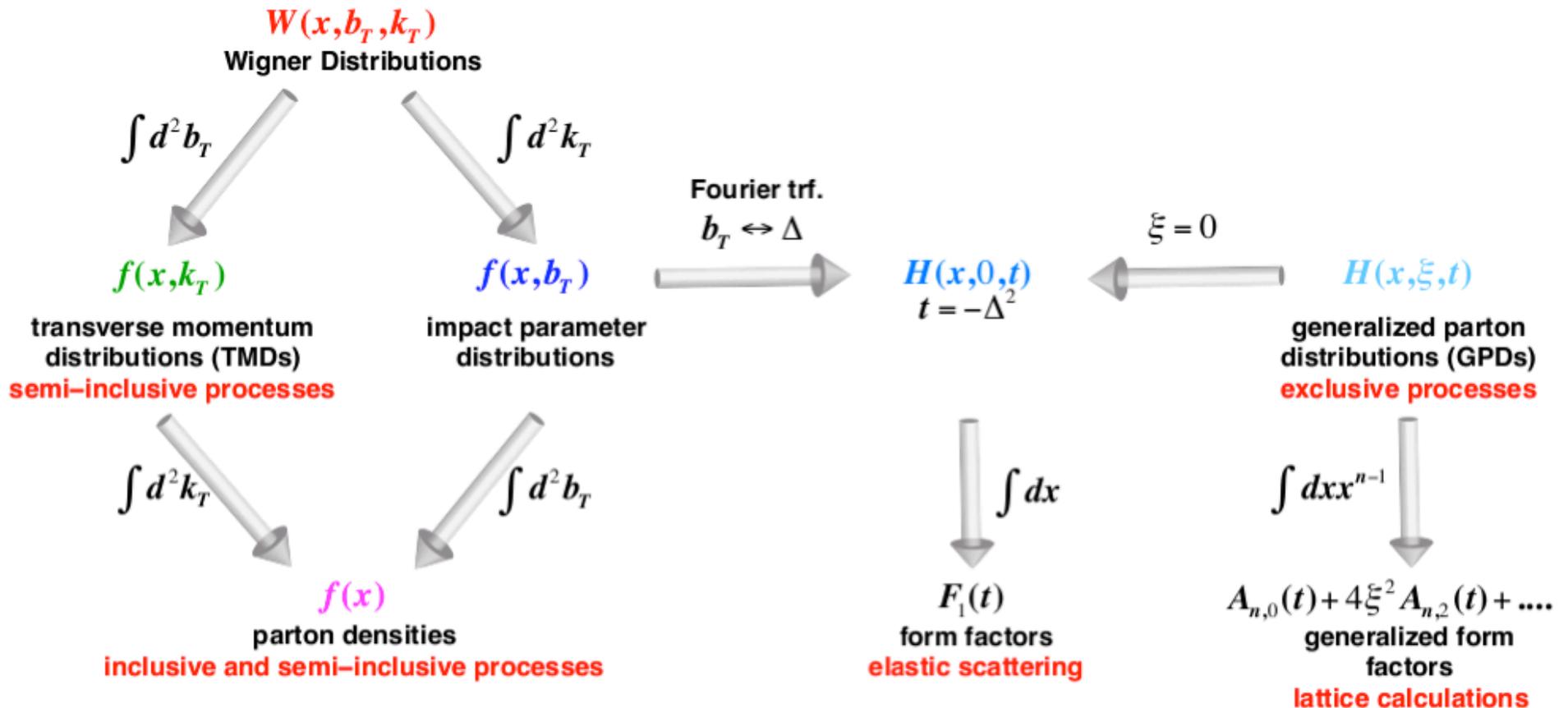
with  $z_s = 3.45$  for 4 quark flavors.

$$S_q(Q^2) = \frac{1}{2} \int_0^1 dx \Delta\Sigma(x, Q^2)$$

- The power is large and negative, and can easily become large enough to make the net power of  $1/x$  larger than 1 for the realistic strong coupling of the order of  $\alpha_s = 0.2 - 0.3$ , resulting in polarized PDFs which actually grow with decreasing  $x$  fast enough for the integral of the PDFs over the low- $x$  region to be (potentially) large.
- Can this solve the spin puzzle? To be continued... and probed at EIC.  
(D. Pitonyak, M. Sievert, YK, arXiv:1511.06737 [hep-ph] + in preparation)

# Transverse Momentum Distributions (TMDs)

- PDFs are insufficient to study the proton structure. Ideally one would like to know the transverse momentum and position distribution of the quarks and gluons in the proton. The tool of choice is the (quark or gluon) Wigner distribution along with associated distribution functions:



# TMDs at EIC

- EIC would allow to measure gluon and anti-quark TMDs for the first time ever, giving an unprecedented insight into proton structure.
- By studying TMDs at EIC we could better understand the proton's 3D structure, orbital motion of the partons, and spin-orbit correlations.

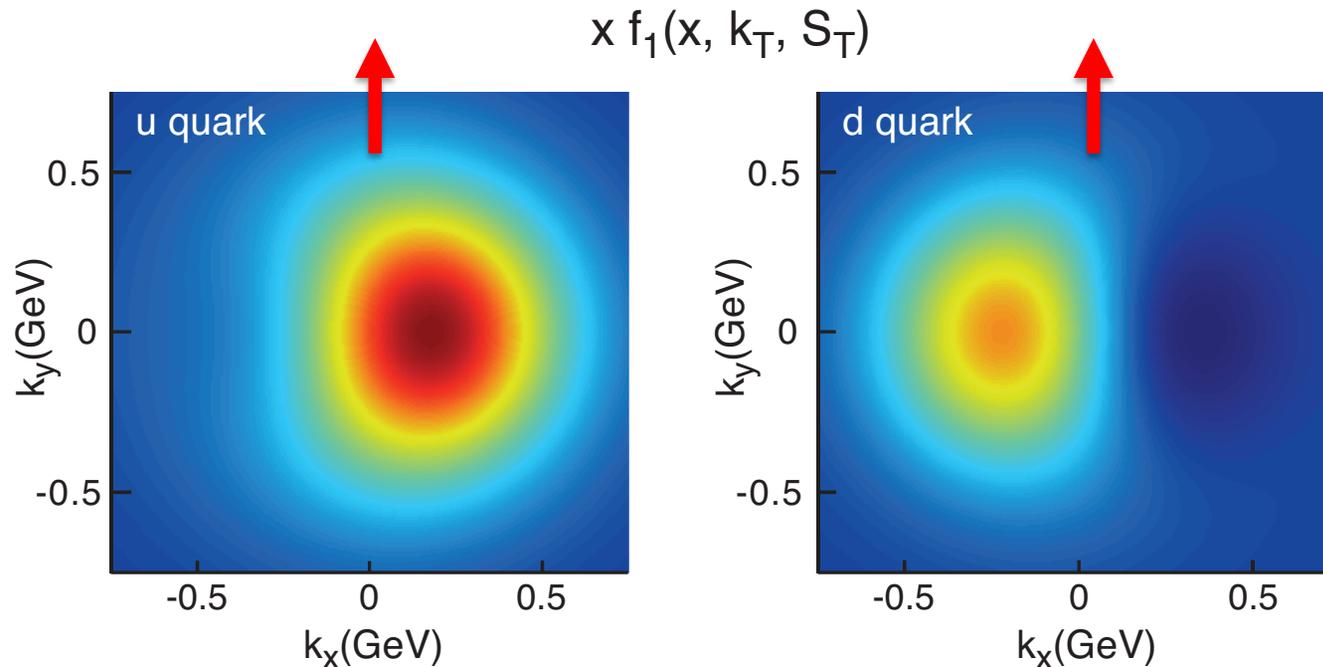
## Leading Twist TMDs



		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 =$		$h_1^\perp =$ — Boer-Mulders
	L		$g_{1L} =$ → —  → Helicity	$h_{1L}^\perp =$ → —  →
	T	$f_{1T}^\perp =$ — Sivers	$g_{1T}^\perp =$ —	$h_1 =$ — Transversity $h_{1T}^\perp =$ —

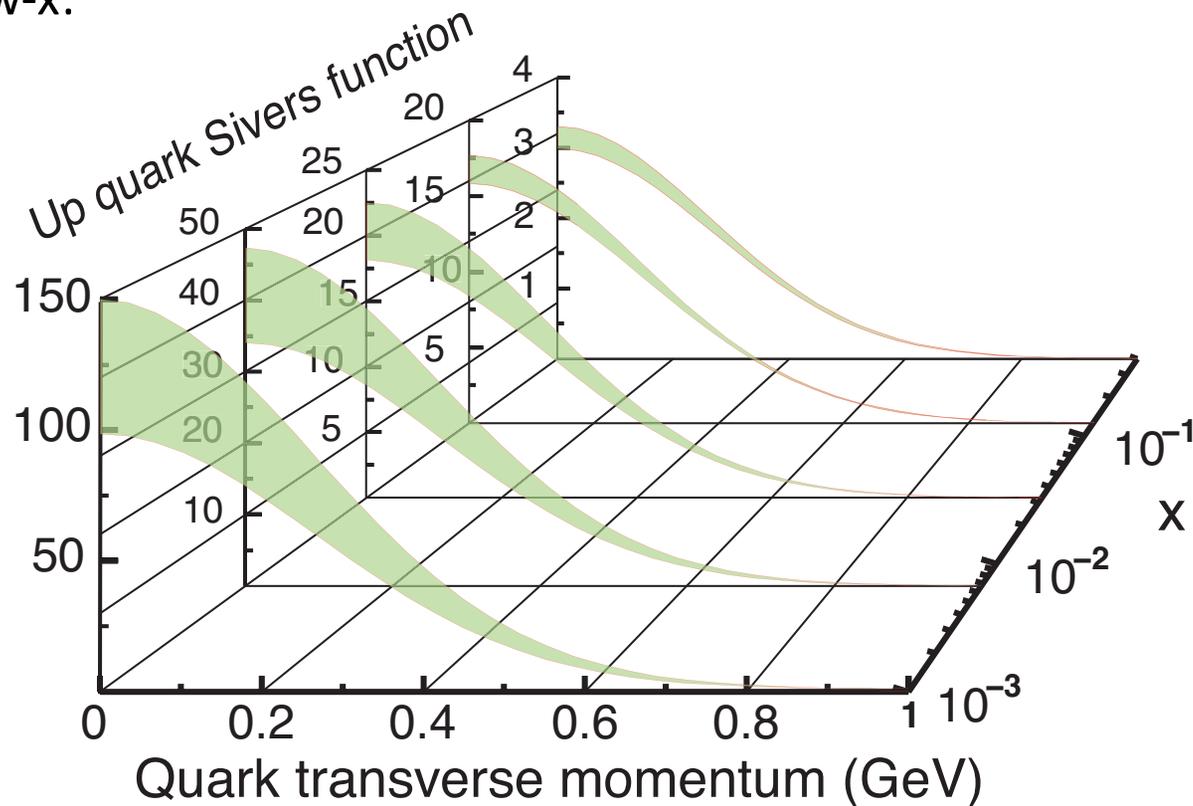
# TMD measurements at EIC

- TMD measurement could give us the transverse momentum distribution of partons, as shown below for u- and d-quark TMDs in a transversely polarized proton (along the y-axis):



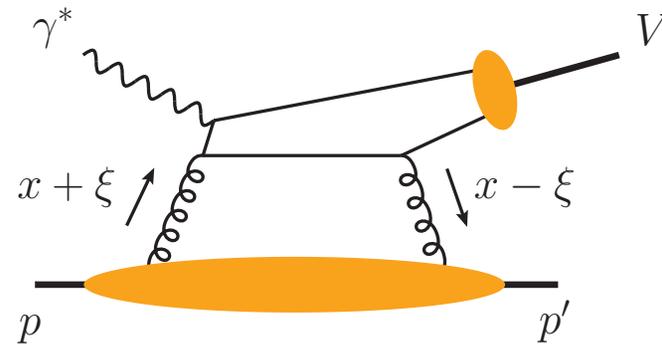
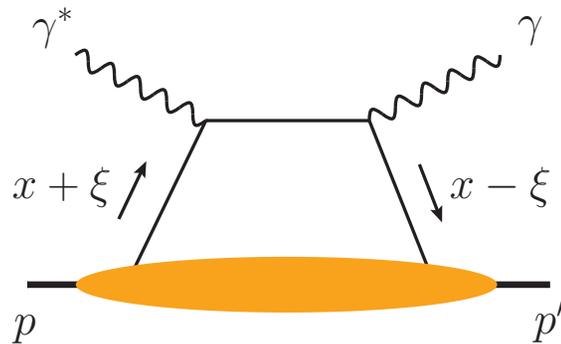
# TMD measurements at EIC

- A TMD known as the Sivers function (responsible for the single transverse spin asymmetry: numbers of left- and right-moving quarks in a transversely polarized proton are different) can also be measured down to very low- $x$ :



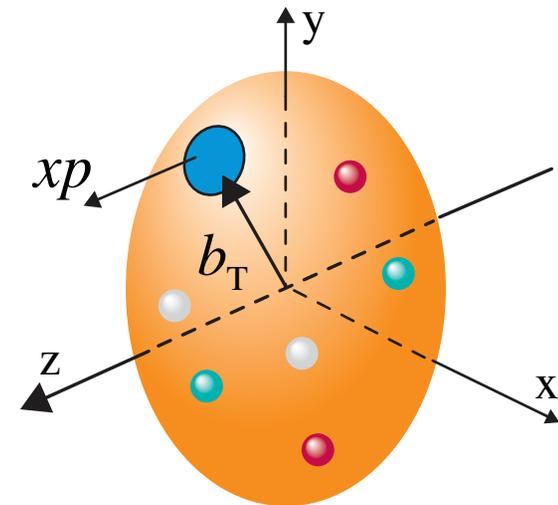
# Spatial Imaging of Quarks and Gluons

- Spatial imaging is complimentary to TMDs.
- It is accomplished by measuring **generalized parton distributions (GPDs)**  $H(x, \xi, t)$  and  $E(x, \xi, t)$ .



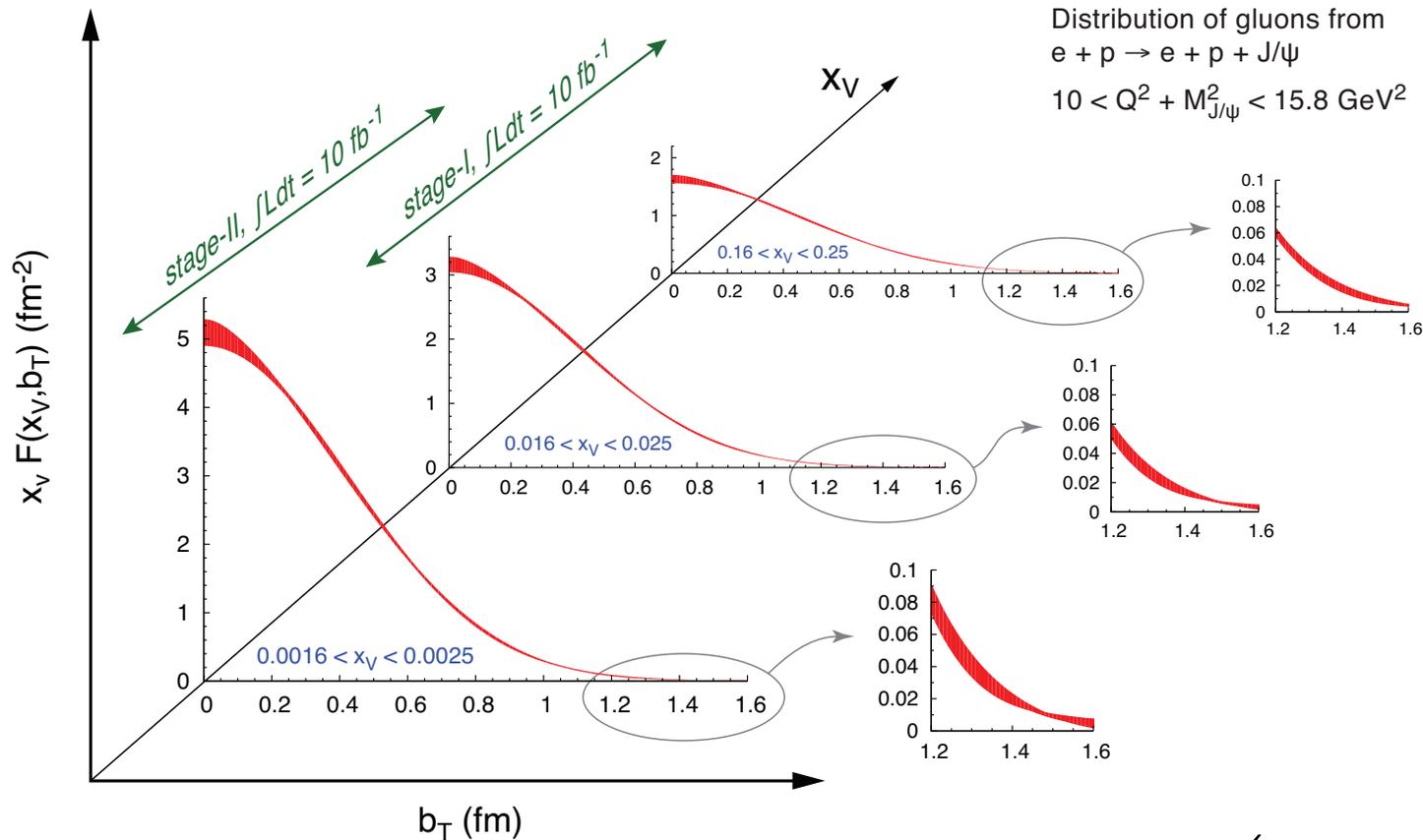
$$t = -\vec{\Delta}_T^2 \quad \vec{\Delta}_T \leftarrow \text{Fourier} \rightarrow \vec{b}_T$$

- GPDs contain detailed information about spin-orbit correlations and the angular momentum carried by the partons.



# GPD Measurements at EIC

- GPDs can be measured at EIC in exclusive vector meson production



$$x_v = x \left( 1 + \frac{M_{J/\psi}^2}{Q^2} \right)$$

# QCD Physics in a Nucleus

# Fundamental Questions in e+A

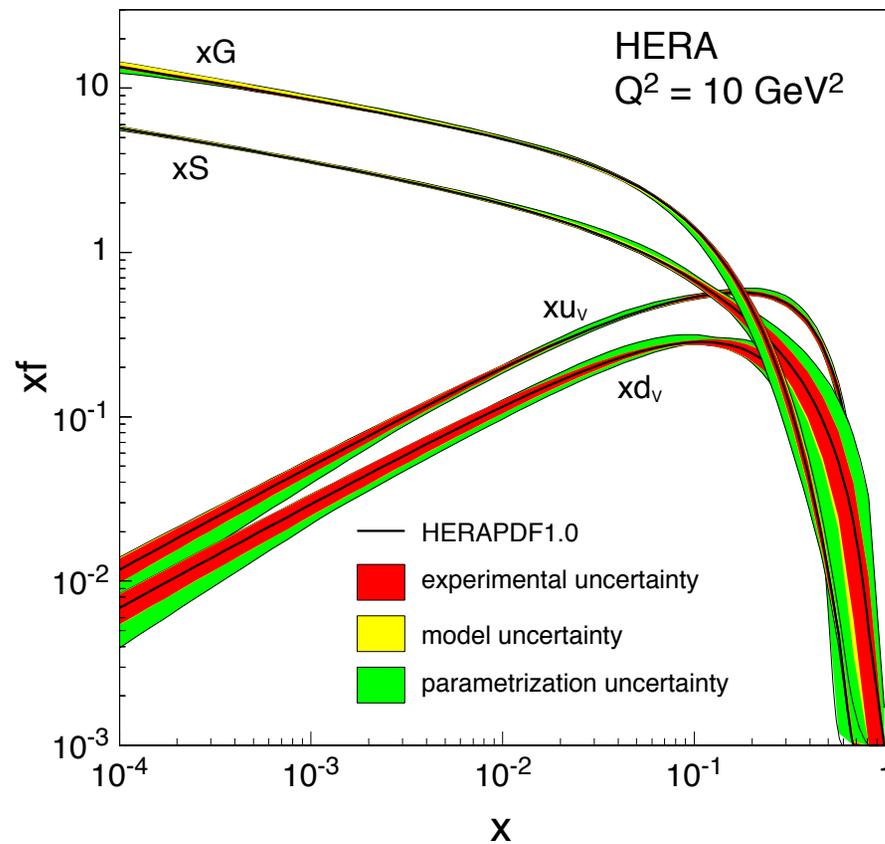
- Can we experimentally find evidence of a novel universal regime of non-linear QCD dynamics in nuclei?
- What is the role of saturated strong gluon fields, and what are the degrees of freedom in this high gluon density regime?
- What is the fundamental quark-gluon structure of light and heavy nuclei?
- Can the nucleus, serving as a color filter, provide novel insight into the propagation, attenuation and hadronization of colored quarks and gluons?

# Small-x Physics and Saturation

# A. Main Concepts

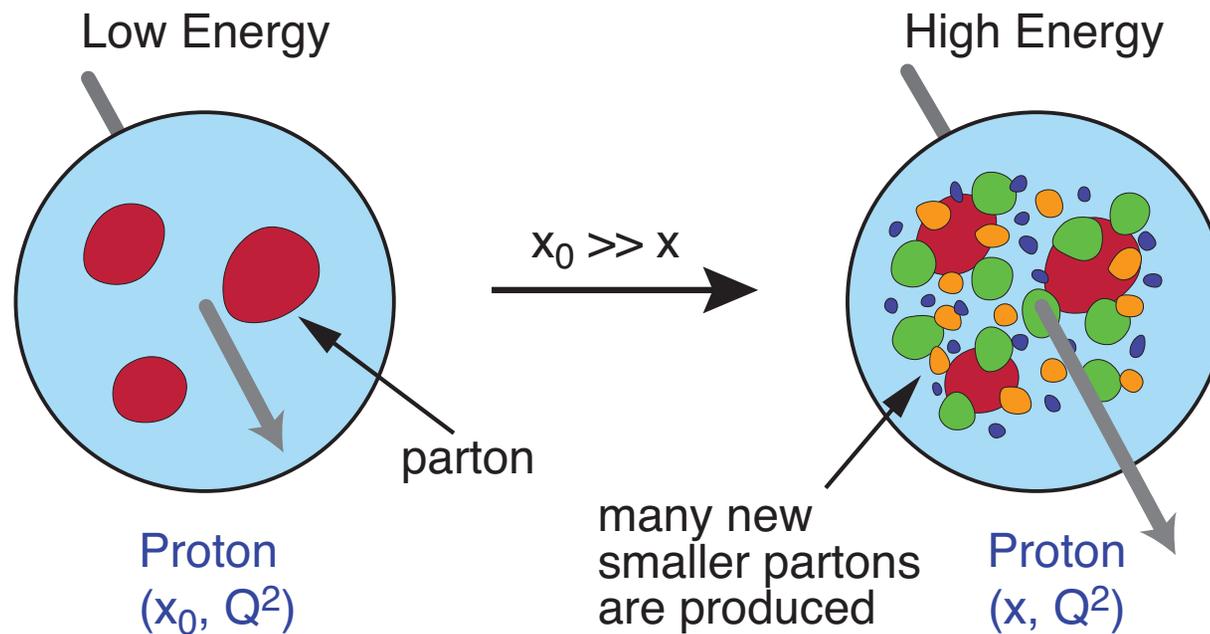
# Gluons at Small-x

- There is a large number of small-x gluons (and quarks) in a proton:



# High Density of Gluons

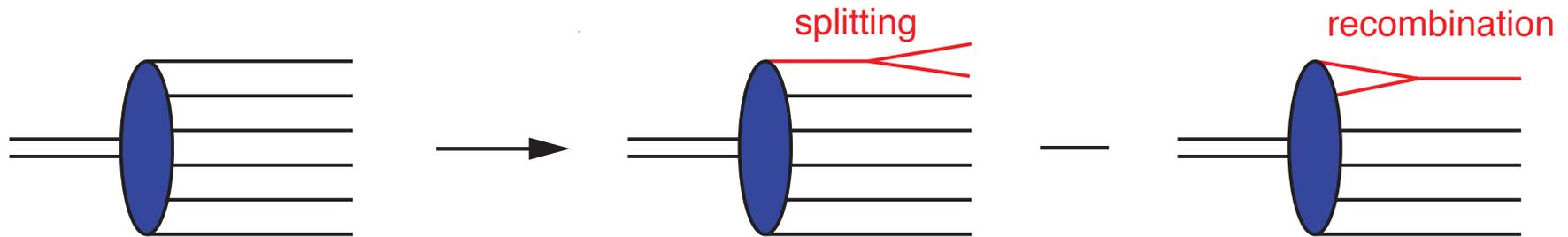
- High number of gluons populates the transverse extent of the proton or nucleus, leading to a very dense saturated wave function known as the Color Glass Condensate (CGC):



“Color Glass Condensate”

# Nonlinear Equation

At very high energy gluon recombination becomes important. As energy (rapidity) increases, gluons not only split into more gluons, but also recombine. Recombination reduces the number of gluons in the wave function. Here  $Y \sim \ln s \sim \ln 1/x$  is rapidity,  $s$  is cms energy.



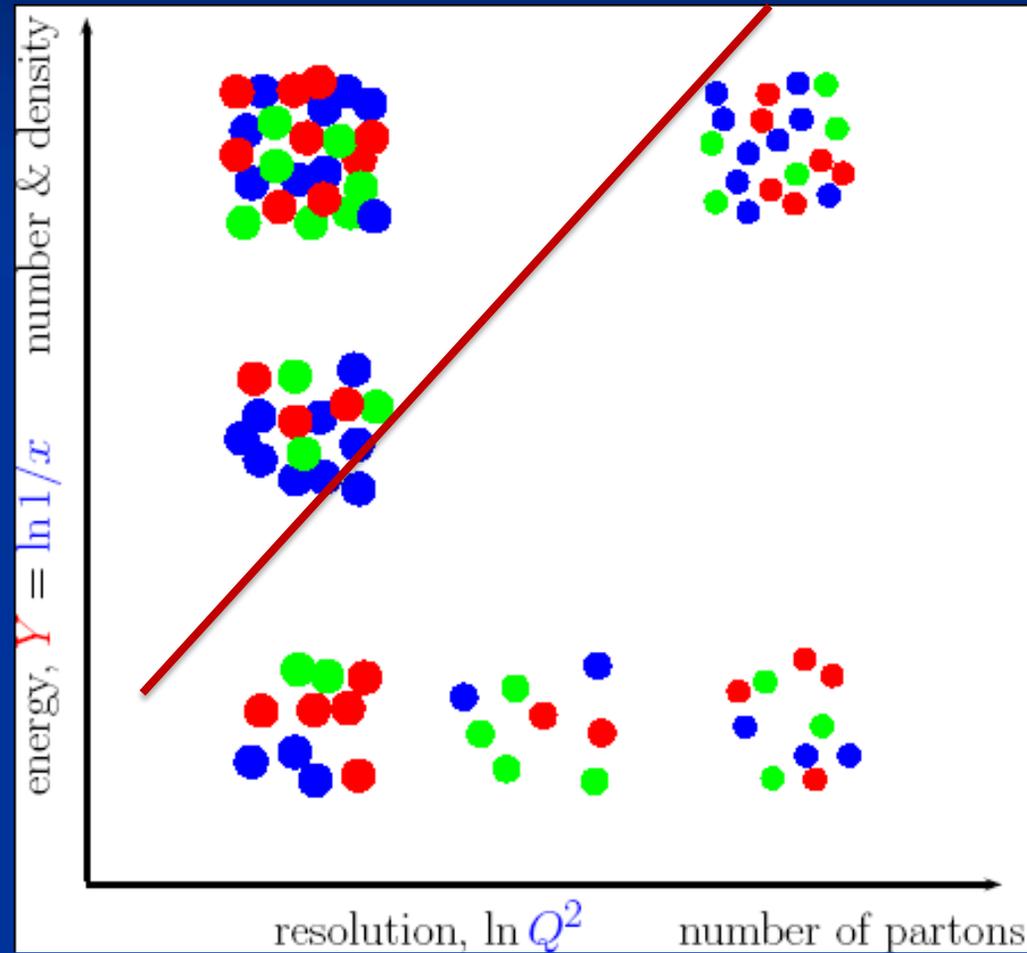
$$\frac{\partial}{\partial Y} N(x, k_T^2) = \alpha_s K_{BFKL} \otimes N(x, k_T^2) - \alpha_s [N(x, k_T^2)]^2$$

Number of gluon pairs  $\sim N^2$

I. Balitsky '96, Yu. K. '99;  
JIMWLK '98-'01

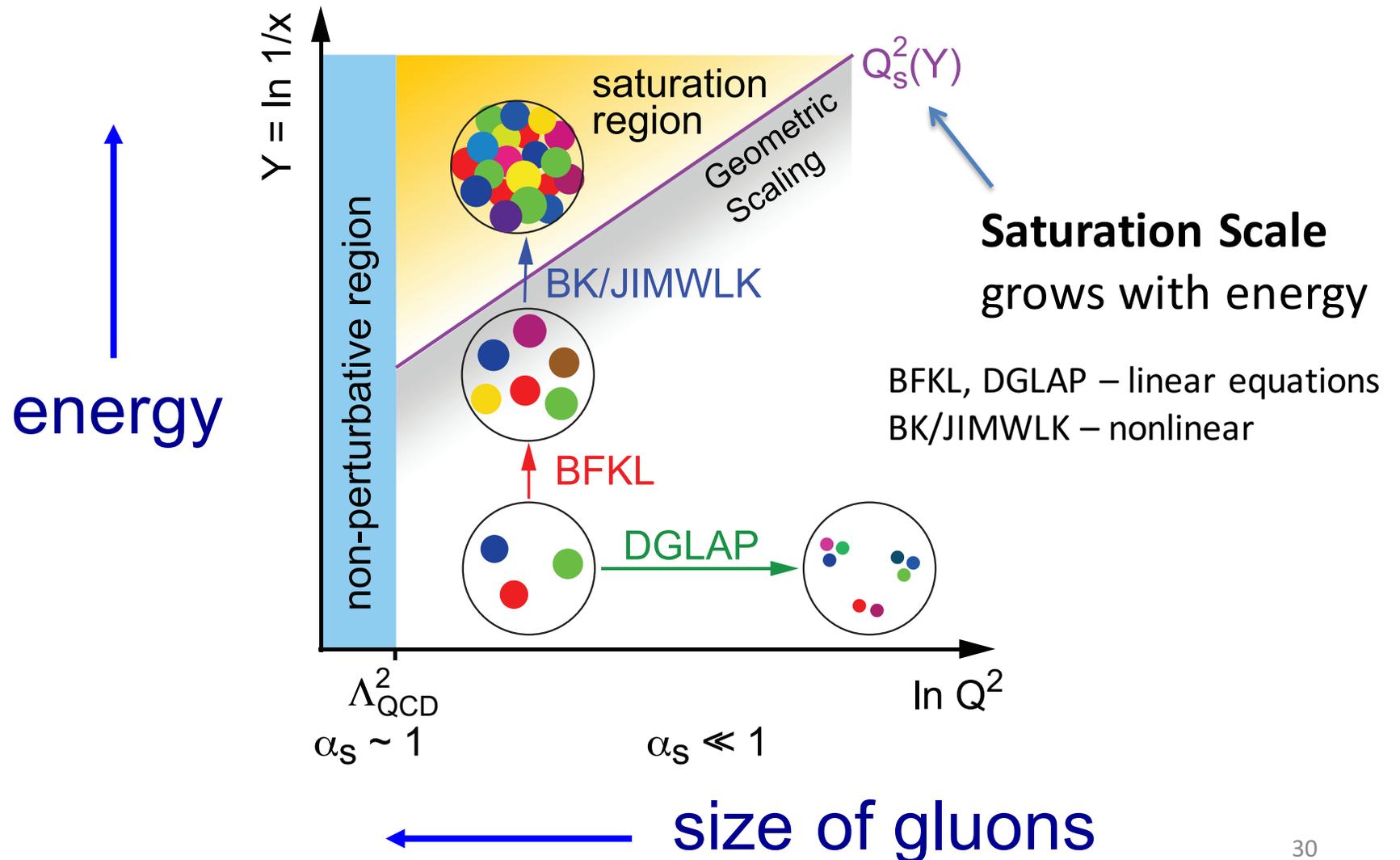
# Map of High Energy QCD

↑  
energy

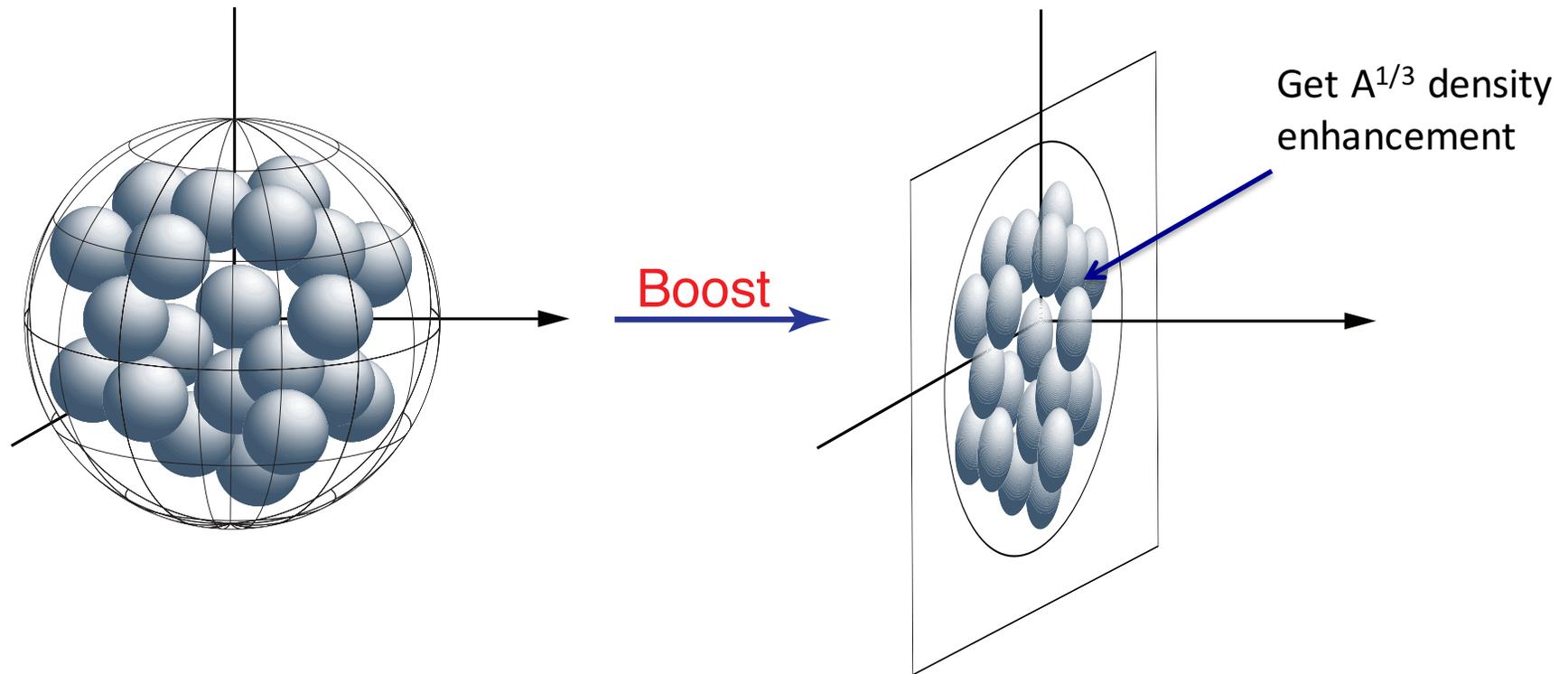


← size of gluons

# Map of High Energy QCD



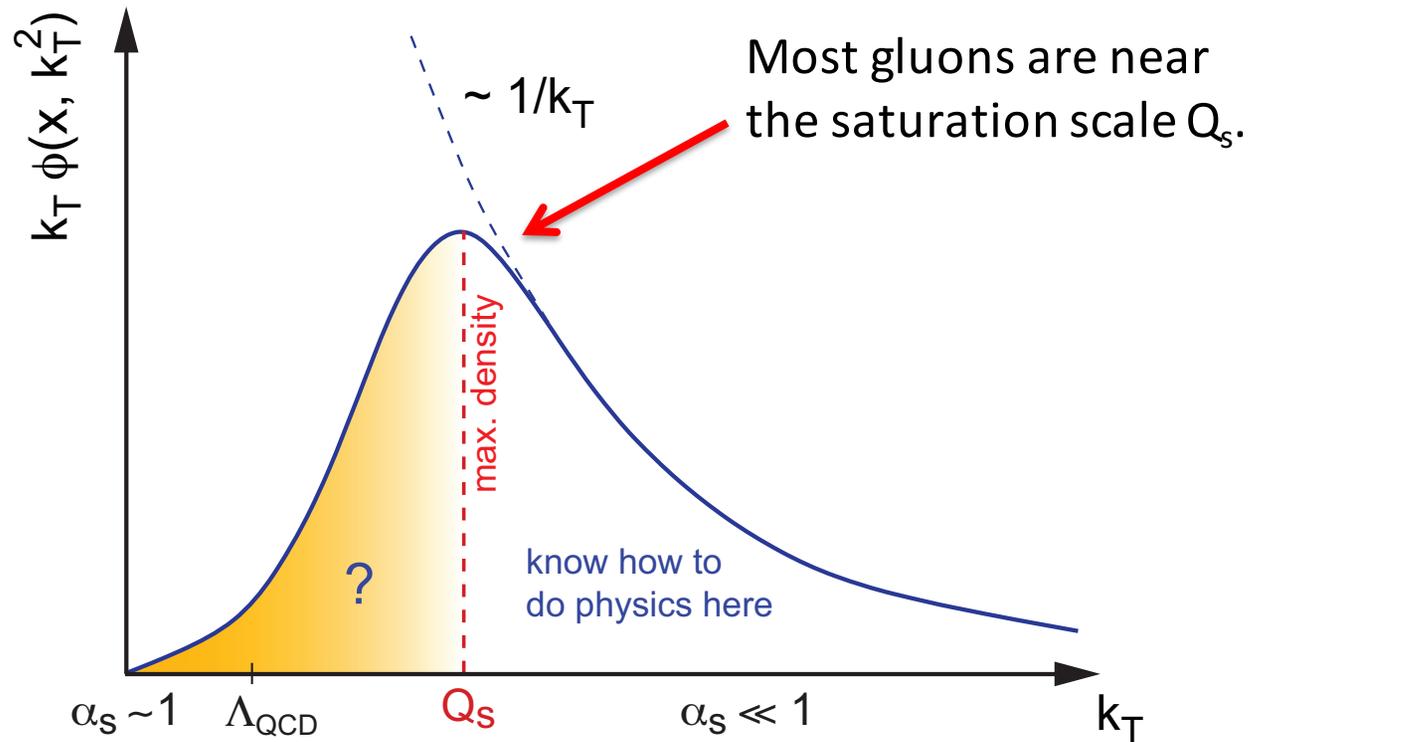
# McLerran-Venugopalan Model



- Large gluon density gives a large momentum scale  $Q_s$  (the saturation scale):  $Q_s^2 \sim \#$  gluons per unit transverse area  $\sim A^{1/3}$  (nuclear ooph).
- For  $Q_s \gg \Lambda_{\text{QCD}}$ , get a theory at weak coupling  $\alpha_s(Q_s^2) \ll 1$  and the leading gluon field is classical.

# Typical gluon “size”

Number of gluons (gluon TMD)  
times the phase space



Gluon “size” =  $1/\text{transverse momentum}$   
=  $1/Q_s$

momentum transverse  
to the beam

# High Energy QCD: saturation physics

- The nonlinear BK/JIMWLK equations and the MV model lead to a large internal momentum scale  $Q_s$  which grows with both the decreasing  $x$  /increasing energy  $s$  ( $\lambda \approx 0.3$ ) and the increasing nuclear atomic number  $A$

$$Q_s^2 \sim A^{1/3} \left( \frac{1}{x} \right)^\lambda$$

such that

$$\alpha_s = \alpha_s(Q_s) \ll 1$$

and we can calculate total cross sections, particle multiplicities, correlations, etc. , from first principles.

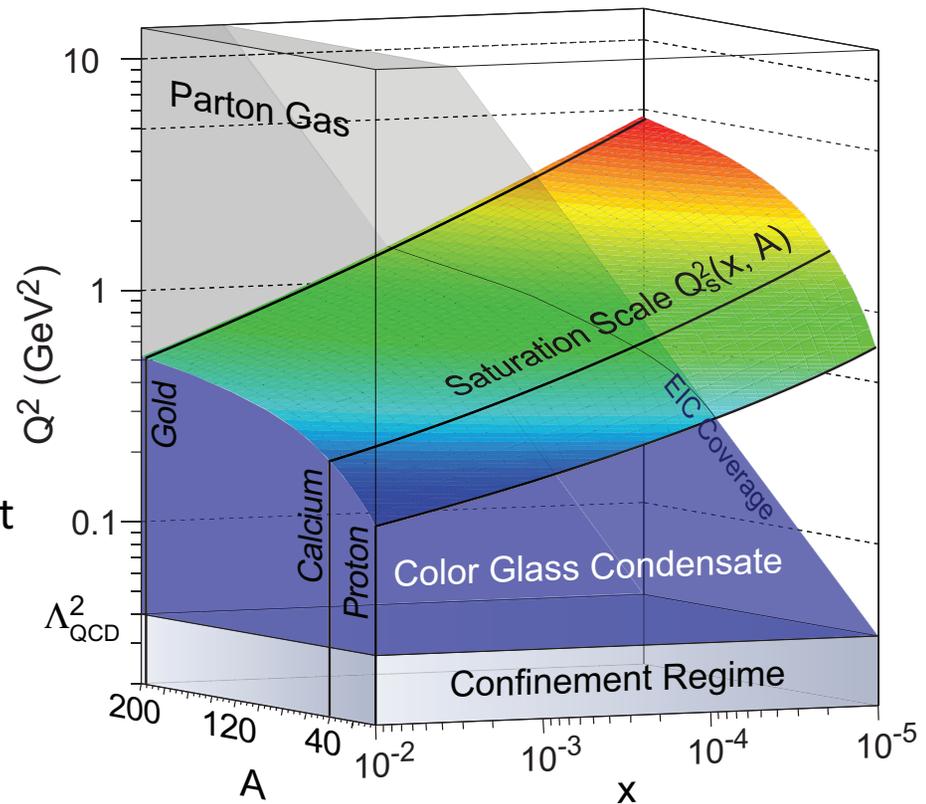
- Bottom line: coupling is weak, Feynman diagrams work.  
But: the system is dense and physics is nonlinear!

# Saturation Scale

To summarize, saturation scale is an increasing function of both energy ( $1/x$ ) and  $A$ :

$$Q_s^2 \sim \left( \frac{A}{x} \right)^{1/3}$$

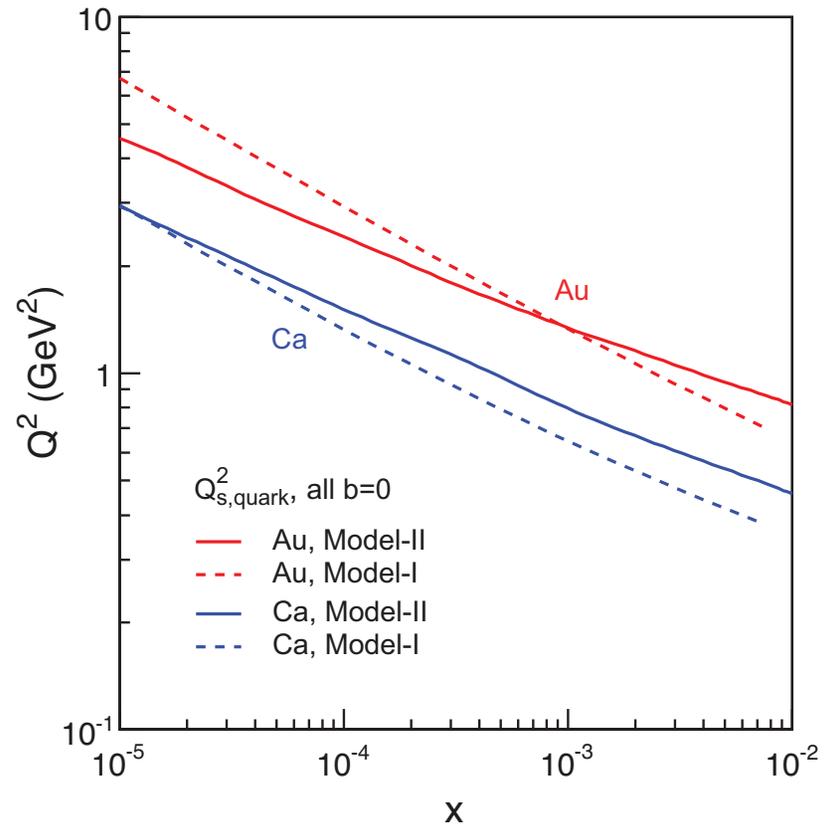
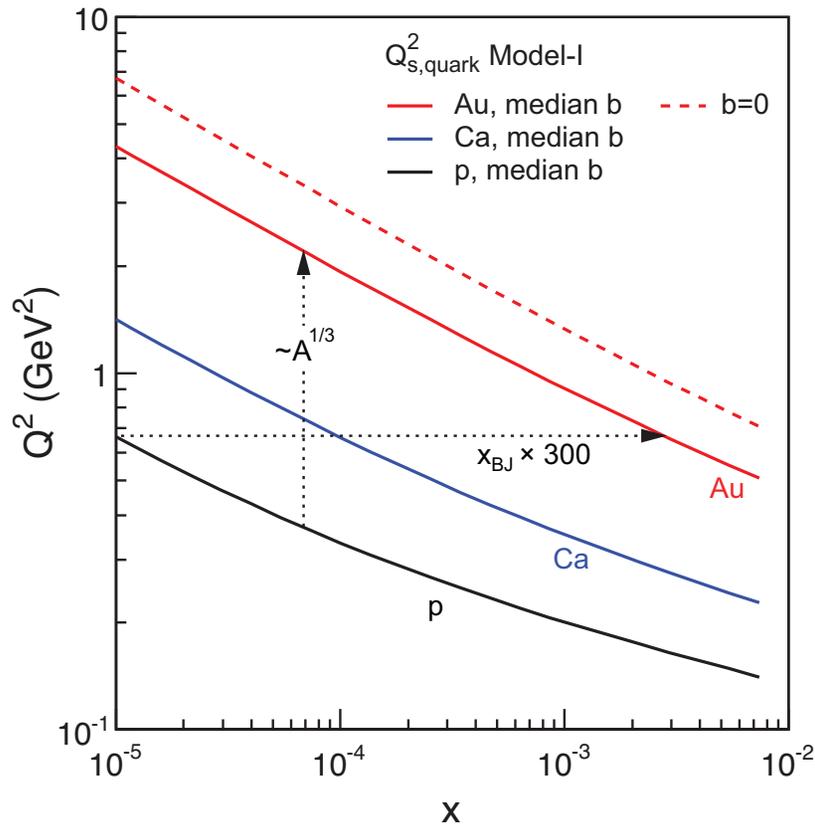
Gold nucleus provides an enhancement by  $197^{1/3}$ , which is equivalent to doing scattering on a proton at 197 times smaller- $x$  / higher- $s$ !



# Saturation Scales at EIC

Model I = MV-inspired dipole model

Model II = running-coupling BK evolution (rcBK)

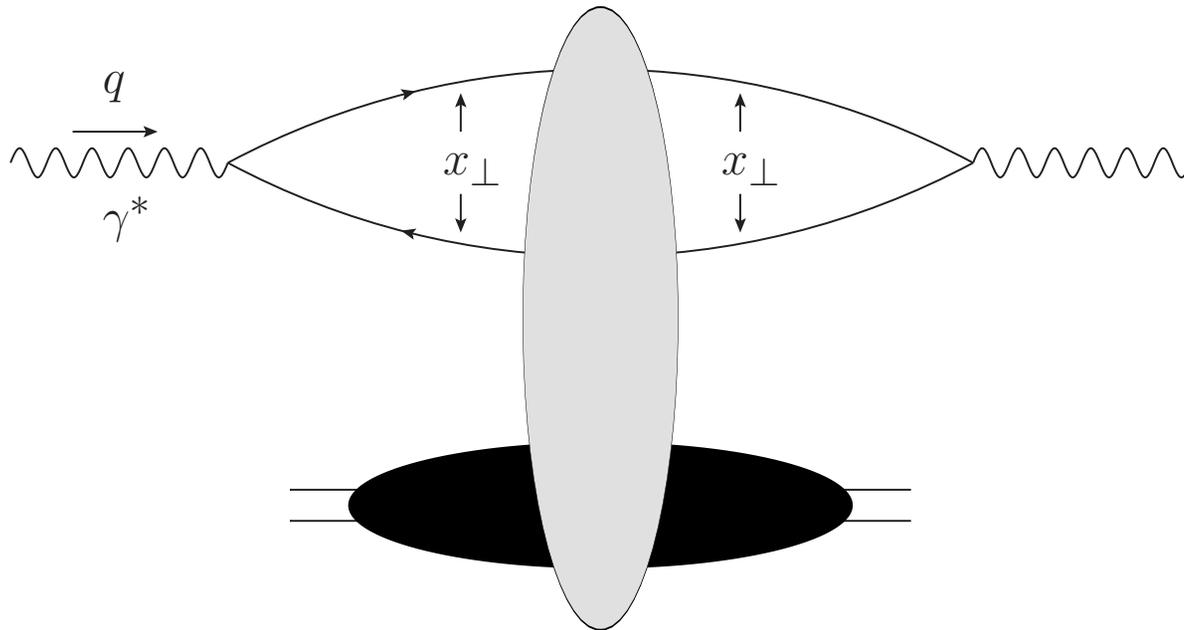


The difference in  $Q_s$  values is minimal in the EIC range.  
 Still theoretical uncertainty remains.

## B. Relevant Observables

# Dipole picture of DIS

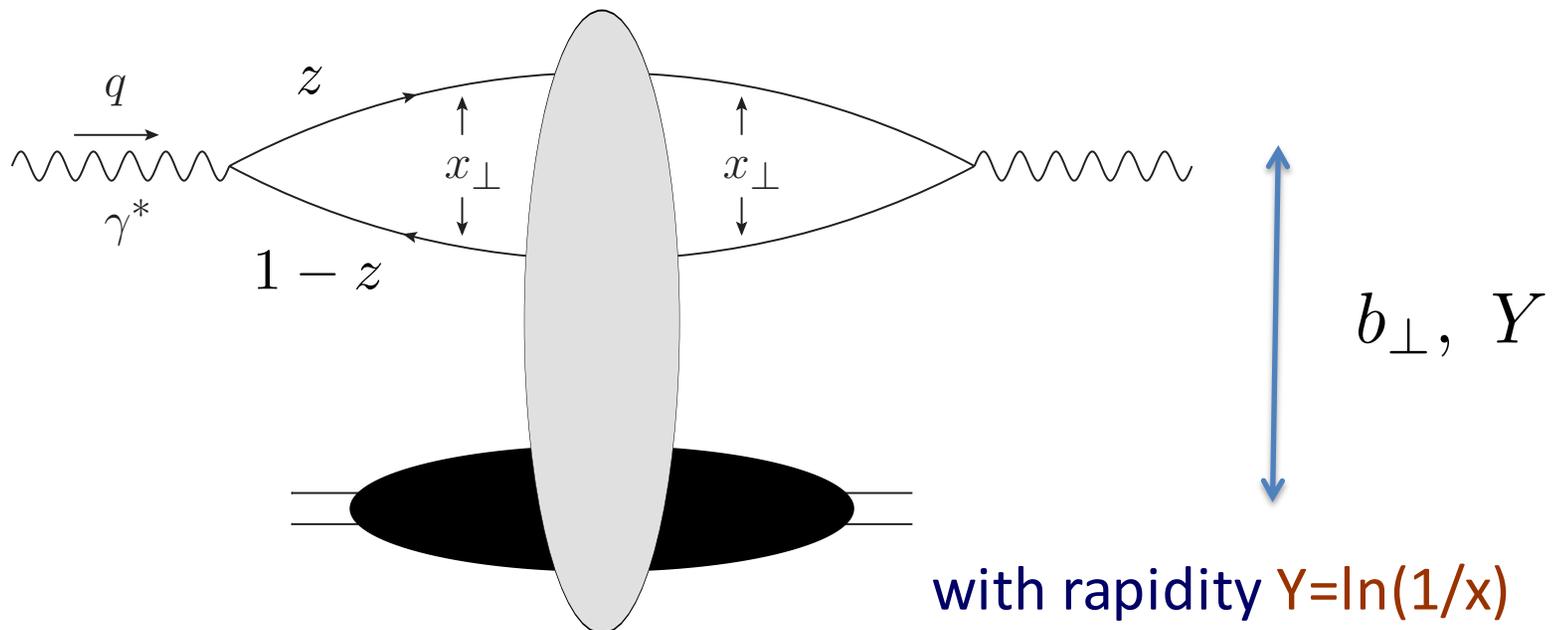
- In the dipole picture of DIS the virtual photon splits into a quark-antiquark pair, which then interacts with the target.
- The total DIS cross section and structure functions are calculated via:



# Dipole Amplitude

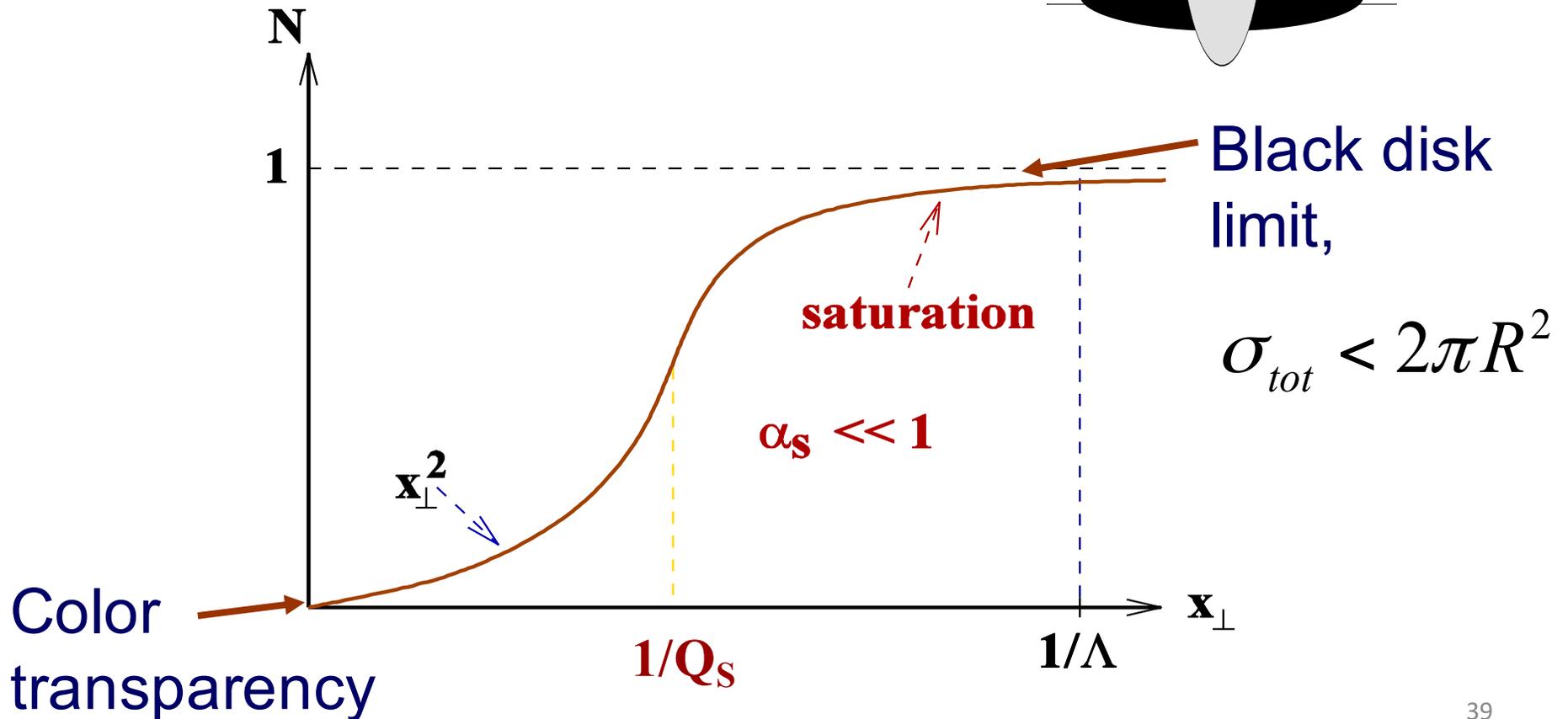
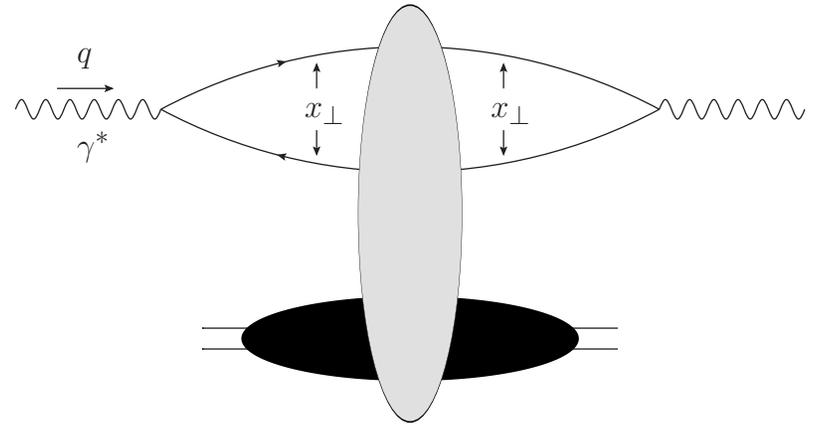
- The total DIS cross section is expressed in terms of the (Im part of the) forward quark dipole amplitude  $N$ :

$$\sigma_{tot}^{\gamma^* A} = \int \frac{d^2 x_{\perp}}{2\pi} d^2 b_{\perp} \int_0^1 \frac{dz}{z(1-z)} |\Psi^{\gamma^* \rightarrow q\bar{q}}(\vec{x}_{\perp}, z)|^2 N(\vec{x}_{\perp}, \vec{b}_{\perp}, Y)$$

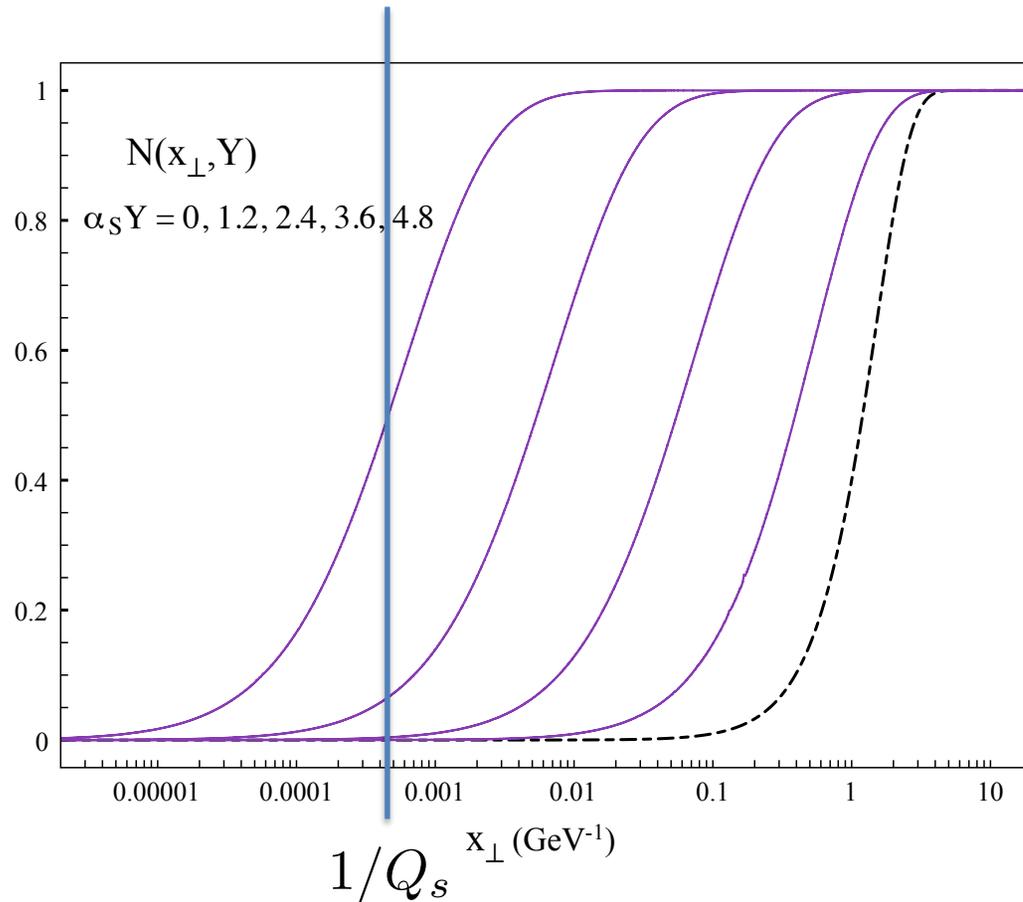


# Dipole Amplitude

The dipole-nucleus amplitude as a function of the dipole size is



# Evolution of the Dipole Amplitude with Rapidity

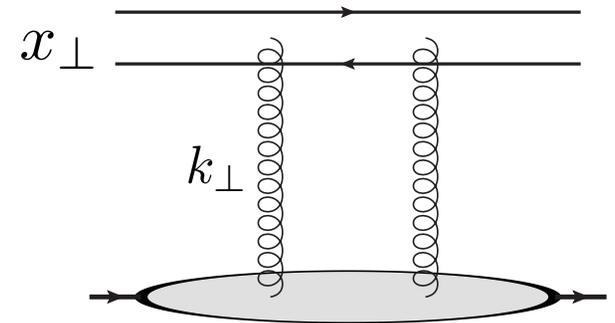


numerical solution  
by J. Albacete '03

BK solution preserves the black disk limit ( $N < 1$ ):

$$\sigma^{q\bar{q}A} = 2 \int d^2b N(x_{\perp}, b_{\perp}, Y)$$

# Dipole Amplitude as a Probe of Spatial Gluon Distribution



- Dipole amplitude is related to gluon distribution.
- It is related to the Wigner distribution for low-x gluons:

$$N(\vec{x}_{\perp}, \vec{b}_{\perp}, Y = \ln 1/x_{Bj}) \Leftrightarrow (\text{Fourier transform}) \Rightarrow W(\vec{k}_{\perp}, \vec{b}_{\perp}, x_{Bj})$$

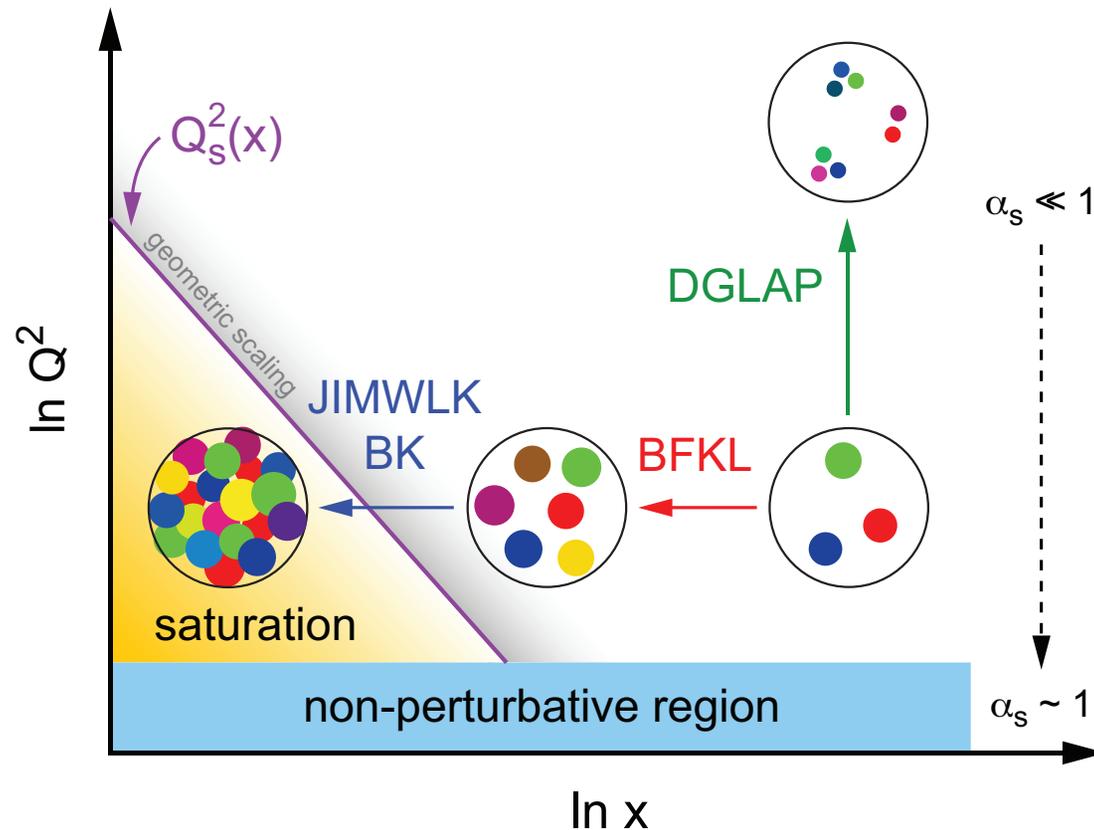
- Just like for the Wigner distribution, one can extract the gluon transverse momentum distribution (TMD) out of it:

$$\int d^2b_{\perp} N(\vec{x}_{\perp}, \vec{b}_{\perp}, Y = \ln 1/x_{Bj}) \Leftrightarrow (\text{Fourier transform}) \Rightarrow f(\vec{k}_{\perp}, x_{Bj})$$

- Dipole amplitude gives us information about the spatial distribution of small-x gluons.

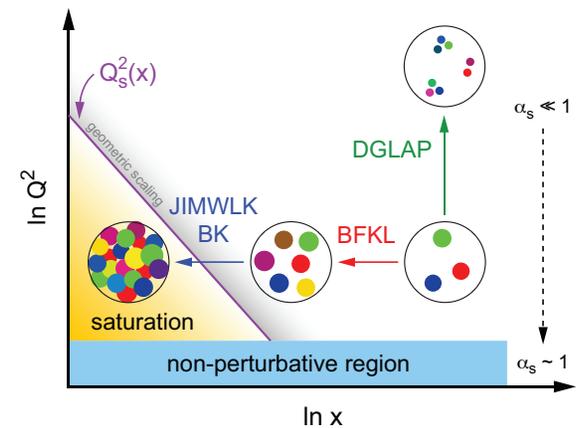
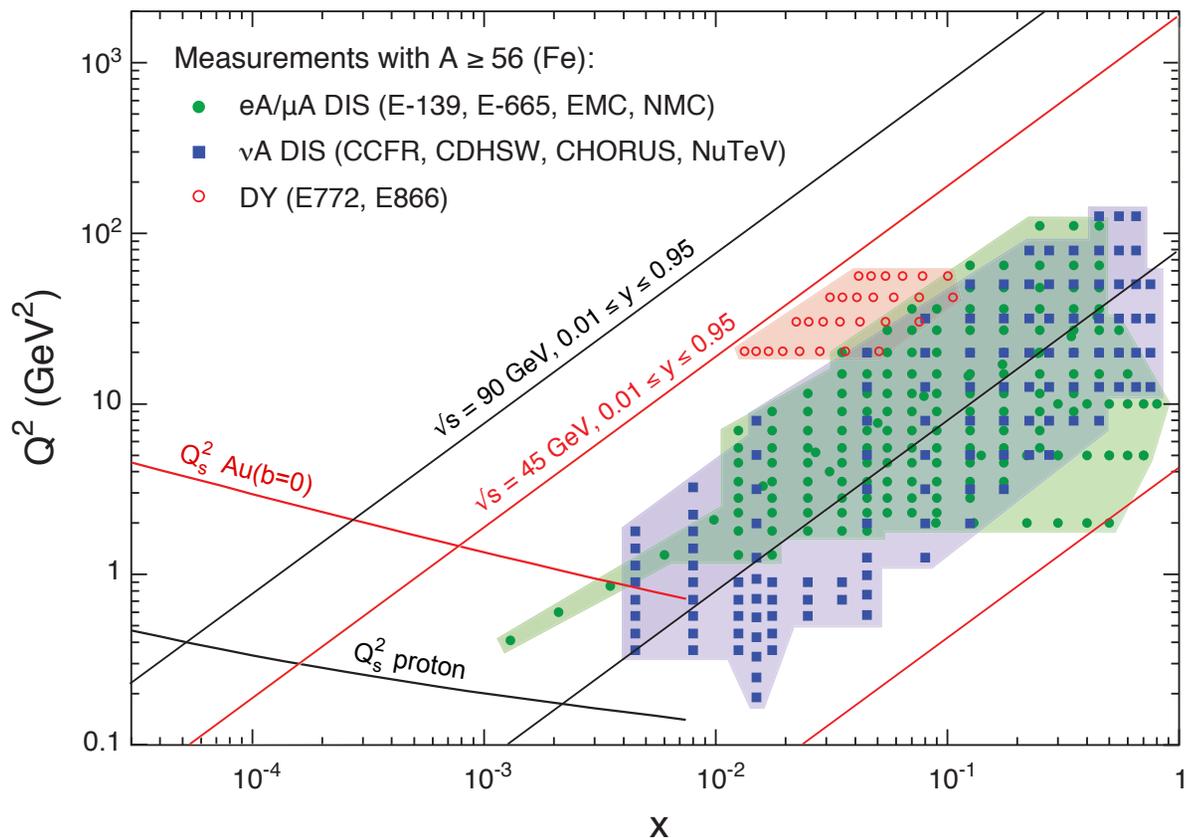
# Can Saturation be Discovered at EIC?

EIC has an unprecedented small- $x$  reach for DIS on large nuclear targets, allowing to seal the discovery of saturation physics and study of its properties:



# Can Saturation be Discovered at EIC?

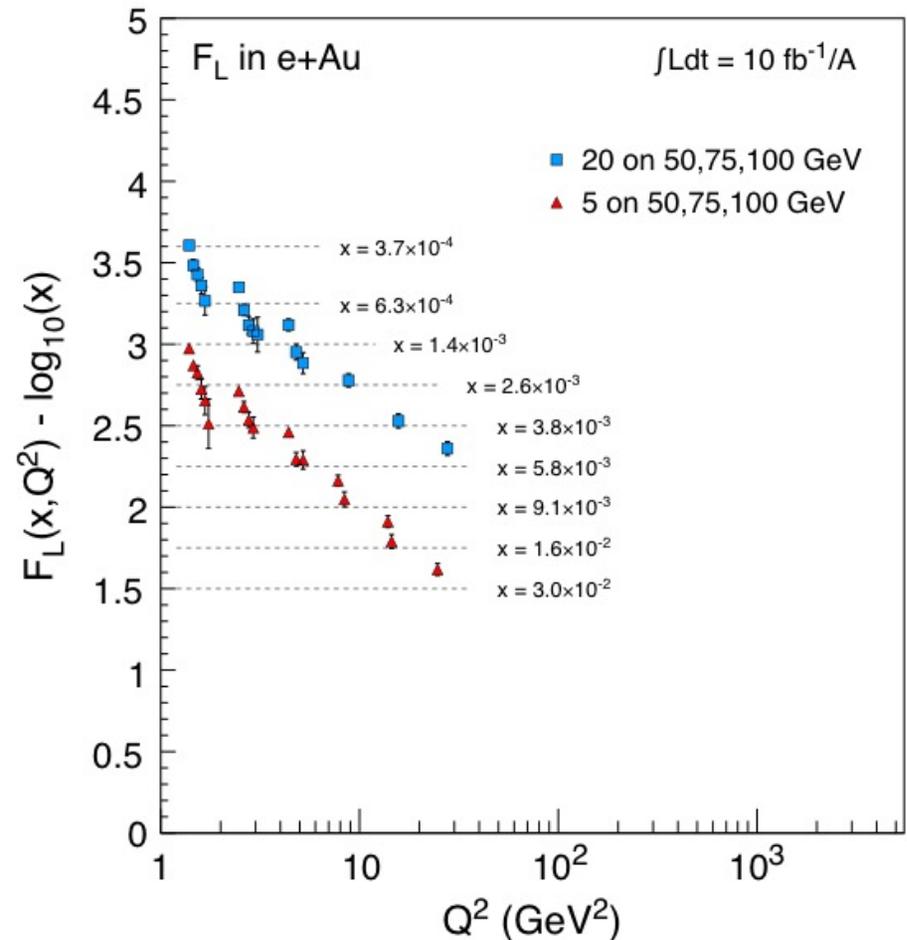
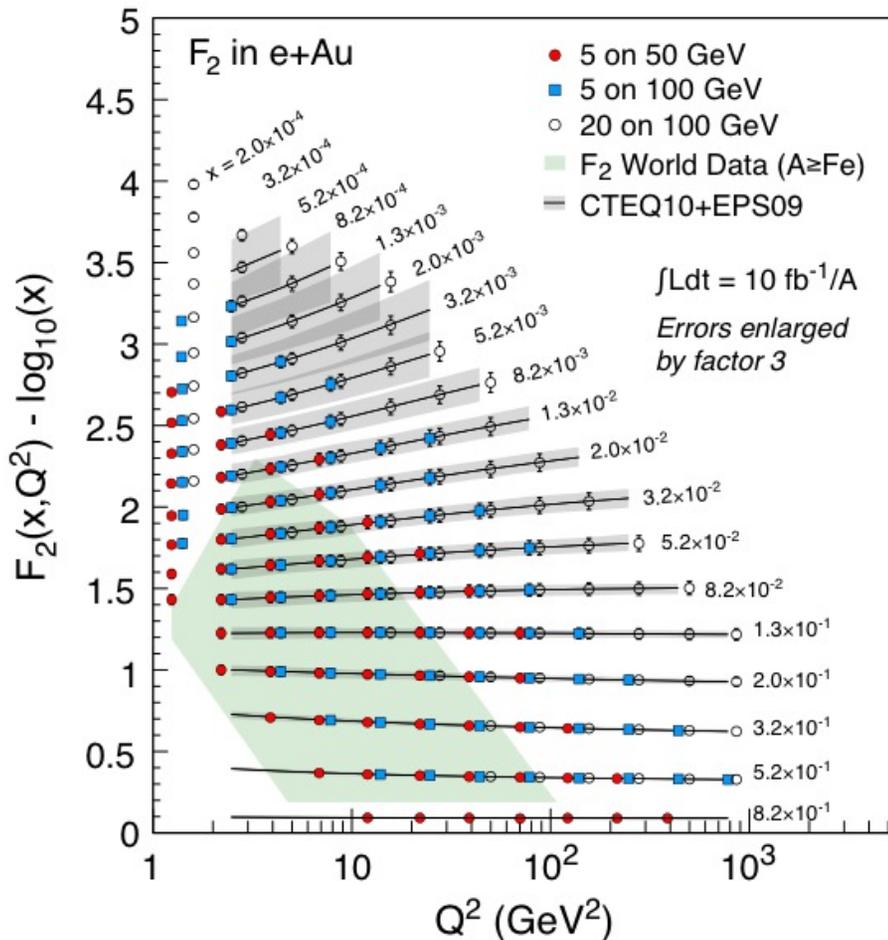
EIC has an unprecedented small-x reach for DIS on large nuclear targets, allowing to seal the discovery of saturation physics and study of its properties:



## (i) Nuclear Structure Functions

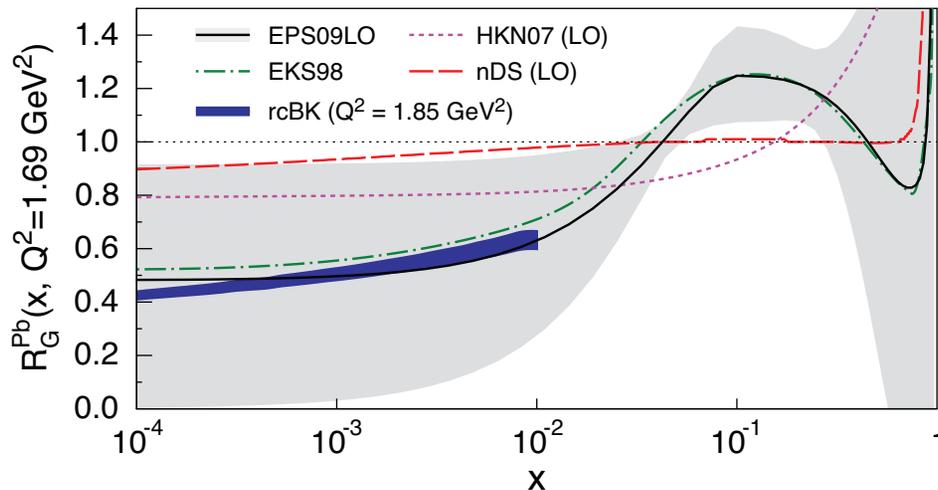
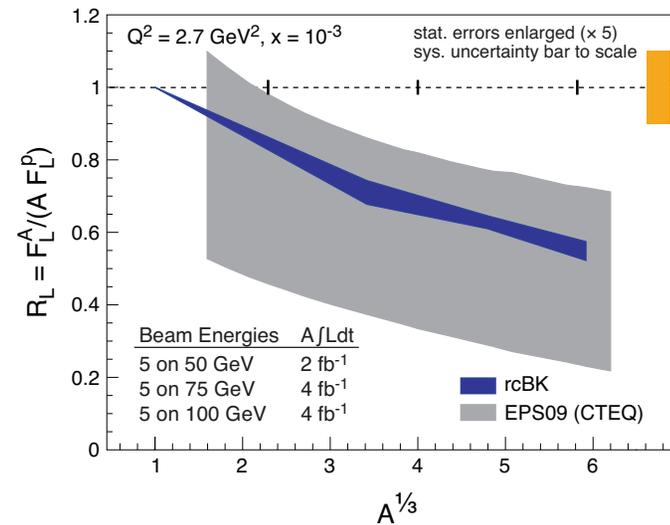
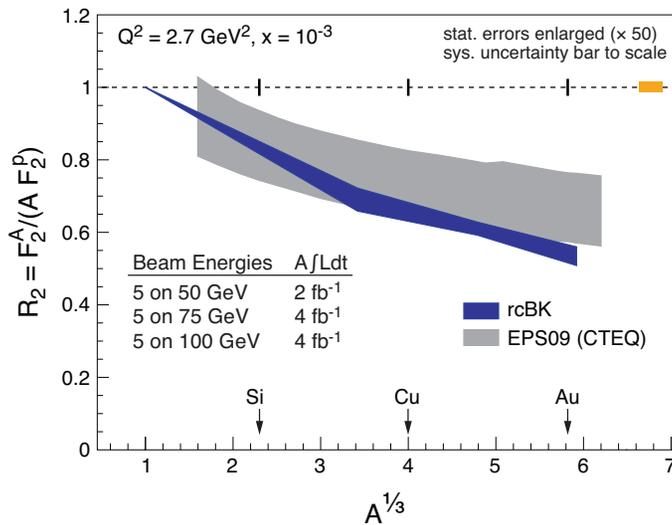
# Structure Function at EIC

Nuclear structure functions  $F_2$  and  $F_L$  which could be measured at EIC (values = EPS09+PYTHIA). Shaded area =  $(x, Q^2)$  range of the world e+A data.



# Nuclear Shadowing

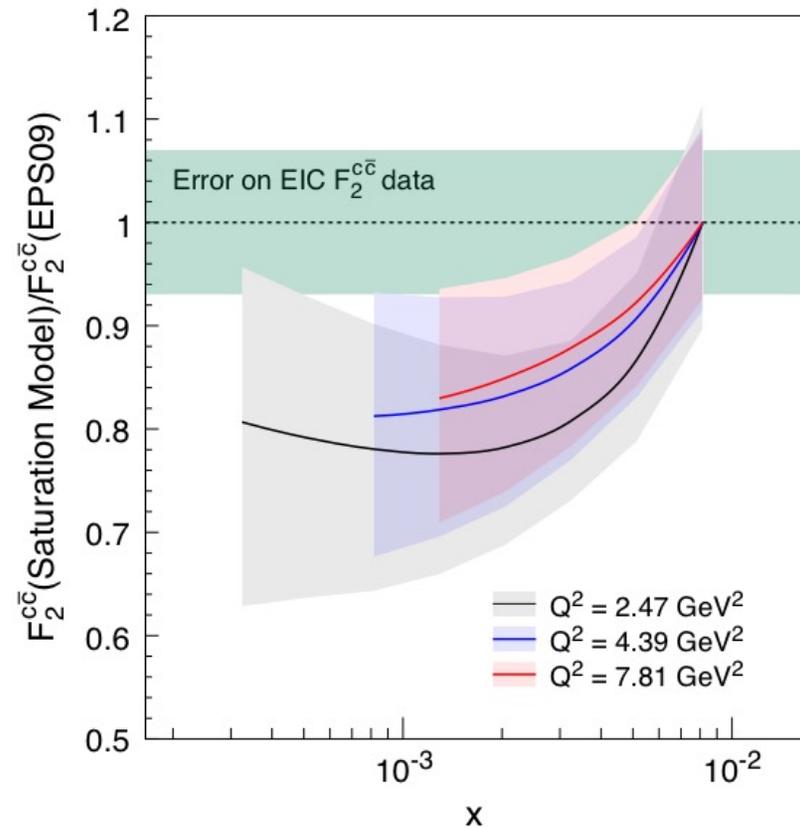
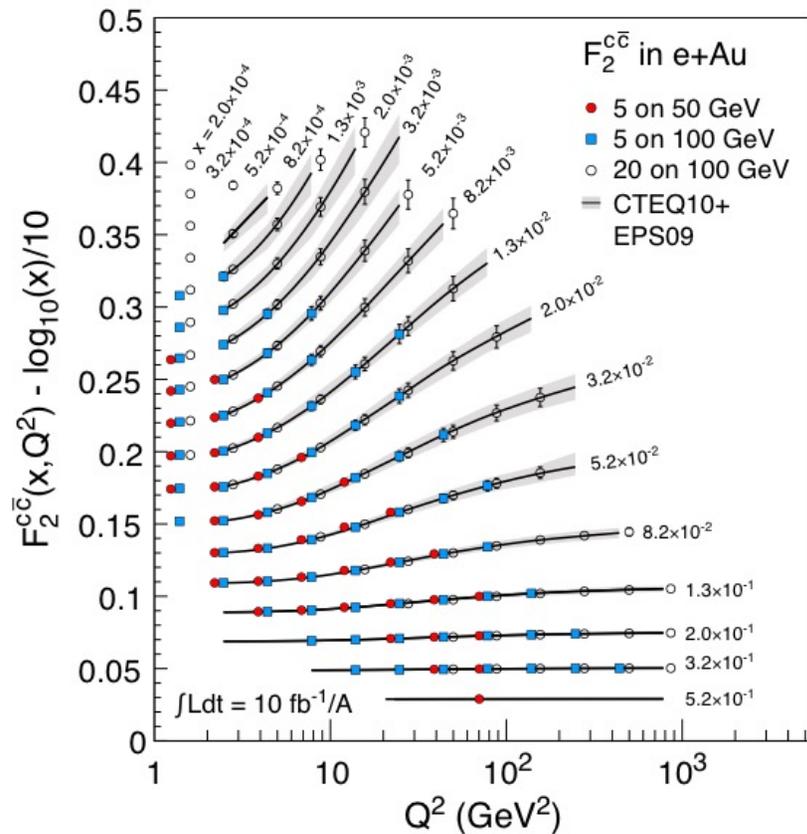
- Saturation effects may explain nuclear shadowing: reduction of the number of gluons per nucleon with decreasing  $x$  and/or increasing  $A$ :



But: as DGLAP does not predict the  $x$ - and  $A$ -dependences, it needs to be constrained by the data.

Note that including heavy flavors (charm) for  $F_2$  and  $F_L$  should help **distinguish between the saturation versus non-saturation predictions.**

# Nuclear Shadowing for Charm

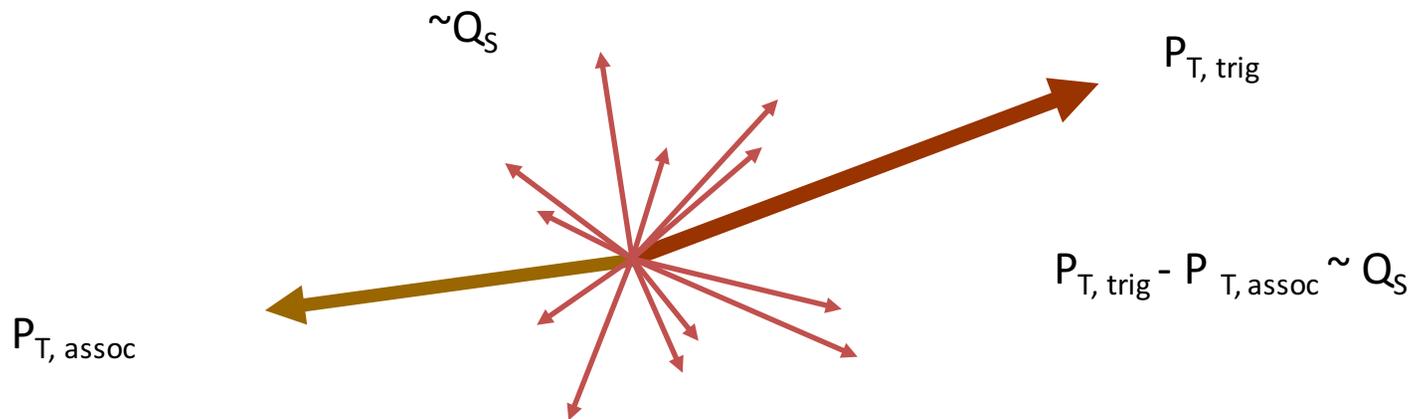
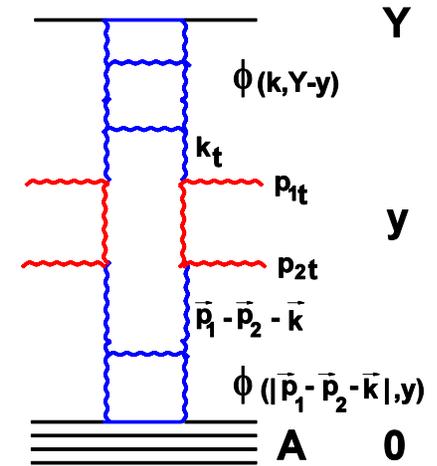


may help distinguish saturation vs DGLAP-based prediction  
 (see talk by Thomas Ullrich for more)

## (ii) Di-Hadron Correlations

# De-correlation

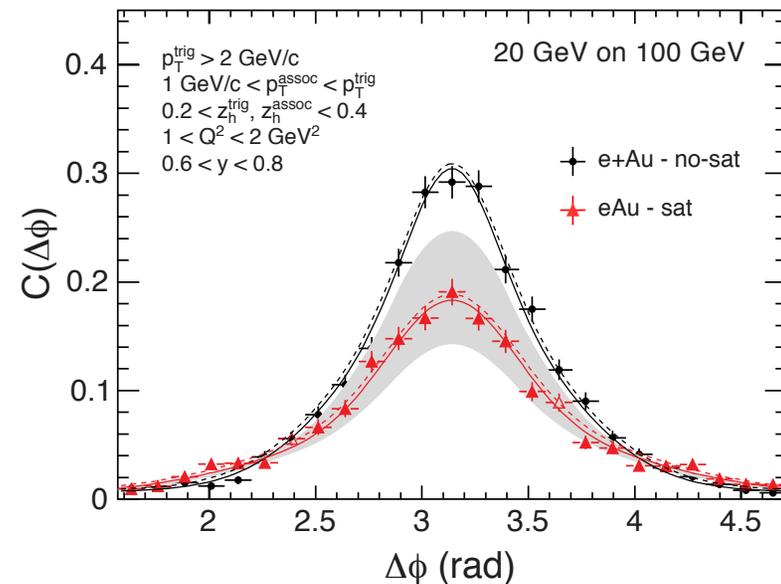
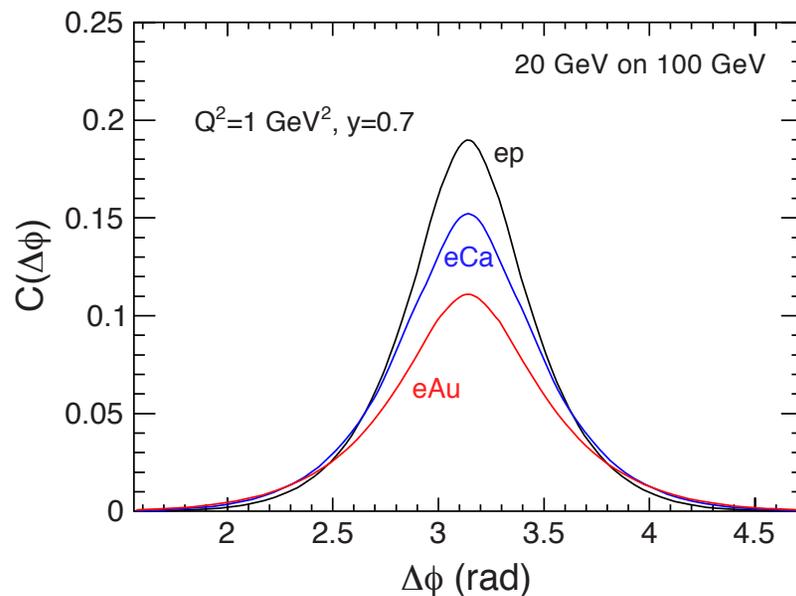
- Small- $x$  evolution  $\leftrightarrow$  multiple emissions
- Multiple emissions  $\rightarrow$  de-correlation.



- B2B jets may get de-correlated in  $p_T$  with the spread of the order of  $Q_S$

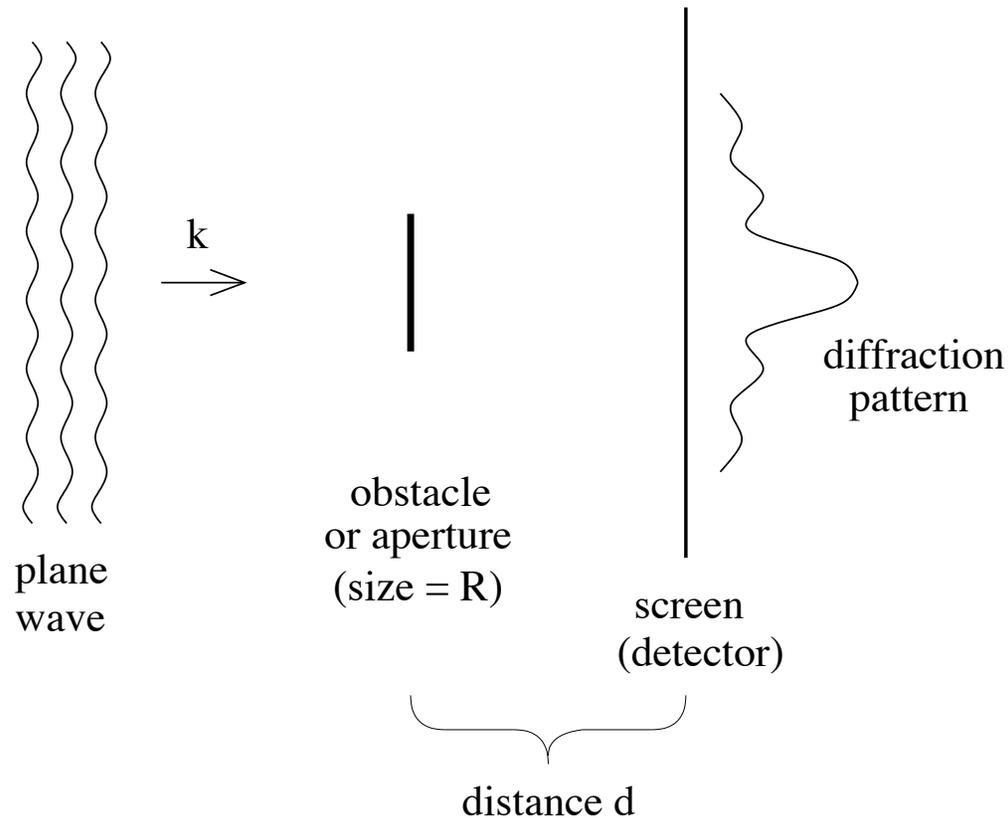
# Di-hadron Correlations

Depletion of di-hadron correlations is predicted for e+A as compared to e+p. (Dominguez et al '11; Zheng et al '14). This is a **signal of saturation**.



### (iii) Diffraction

# Diffraction in optics

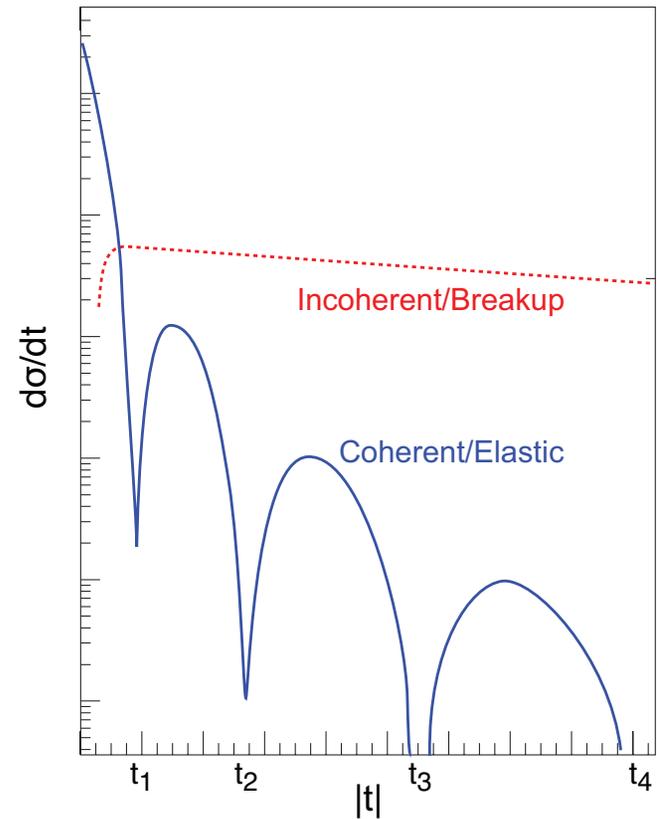
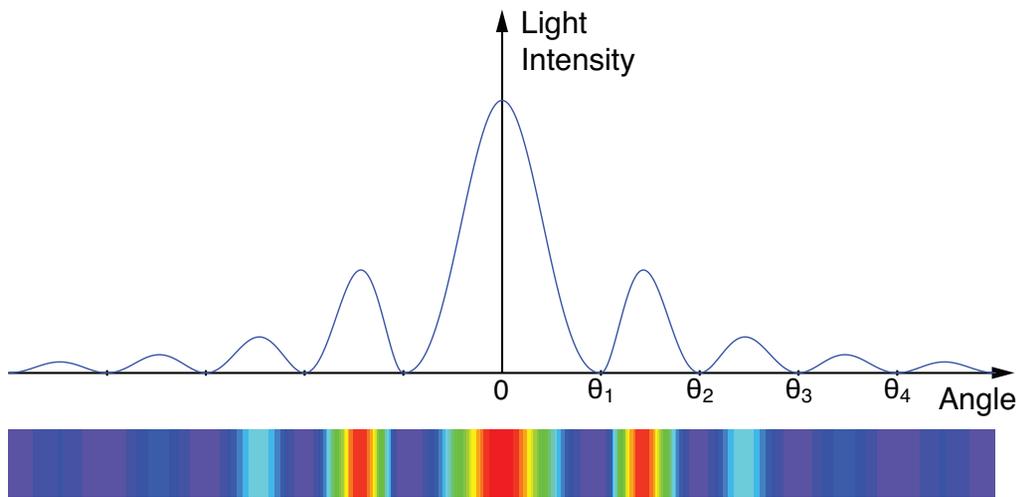


Diffraction pattern contains information about the size  $R$  of the obstacle and about the optical “blackness” of the obstacle.

In optics, diffraction pattern is studied as a function of the angle  $\theta$ . In high energy scattering the diffractive cross sections are plotted as a function of the Mandelstam variable  $t = k \sin \theta$ .

# Optical Analogy

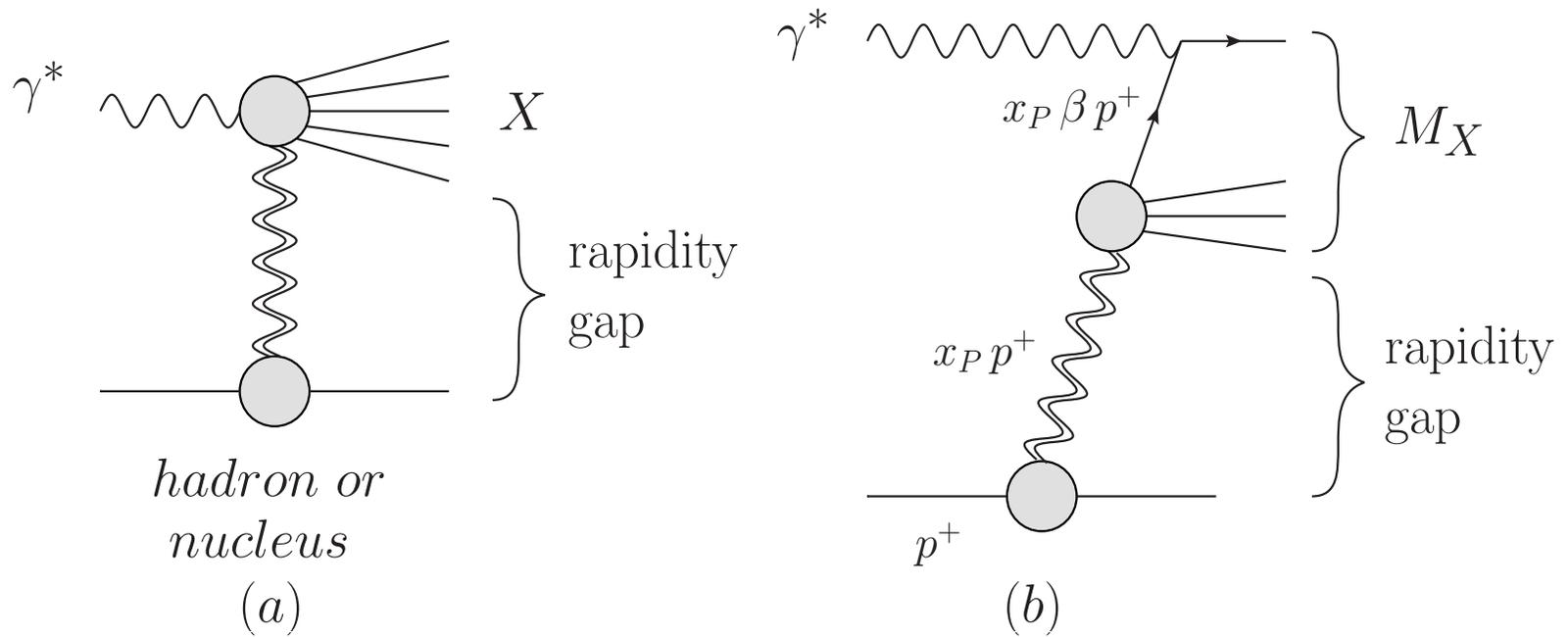
Diffraction in high energy scattering is not very different from diffraction in optics: both have diffractive maxima and minima:



Coherent: target stays intact;

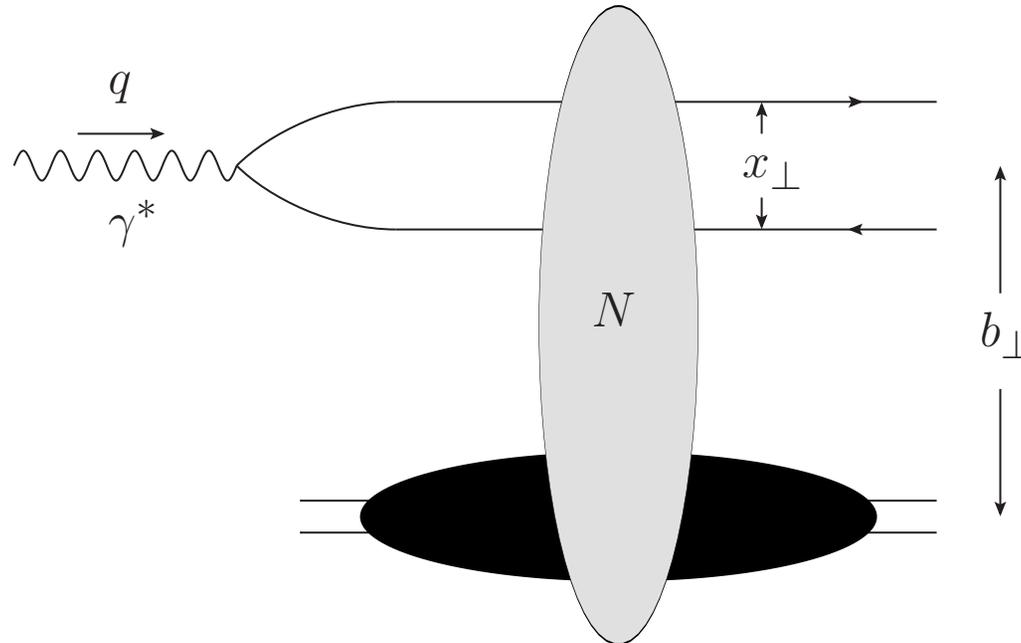
Incoherent: target nucleus breaks up, but nucleons are intact.

# Diffraction terminology



# Quasi-elastic DIS

Consider the case when nothing but the quark-antiquark pair (pions) is produced:



The quasi-elastic cross section is then

$$\sigma_{el}^{\gamma^* A} = \int \frac{d^2 x_\perp}{4\pi} d^2 b_\perp \int_0^1 \frac{dz}{z(1-z)} |\Psi^{\gamma^* \rightarrow q\bar{q}}(\vec{x}_\perp, z)|^2 N^2(\vec{x}_\perp, \vec{b}_\perp, Y)$$

Buchmuller et al '97, McLerran and Yu.K. '99

# Diffraction on a black disk

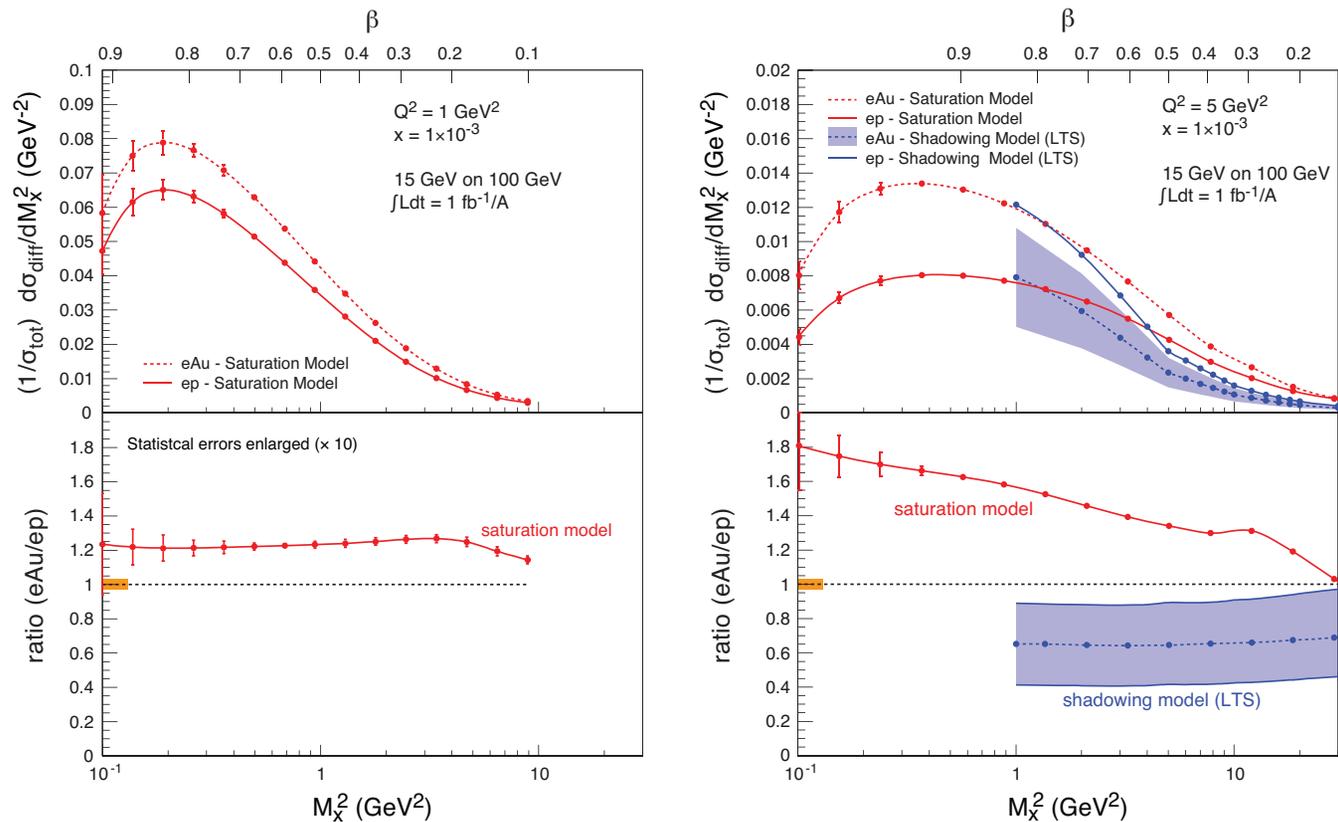
- For low  $Q^2$  (large dipole sizes) the black disk limit is reached with  $N=1$
- Diffraction (elastic scattering) becomes a half of the total cross section

$$\frac{\sigma_{el}^{q\bar{q}A}}{\sigma_{tot}^{q\bar{q}A}} = \frac{\int d^2b N^2}{2 \int d^2b N} \longrightarrow \frac{1}{2}$$

- Large fraction of diffractive events in DIS is a signature of reaching the black disk limit!
- HERA: ~15% (unexpected!); EIC: ~25% expected from saturation

# Diffraction over total cross sections

- Here's an early EIC measurement which may **distinguish saturation from non-saturation** approaches:

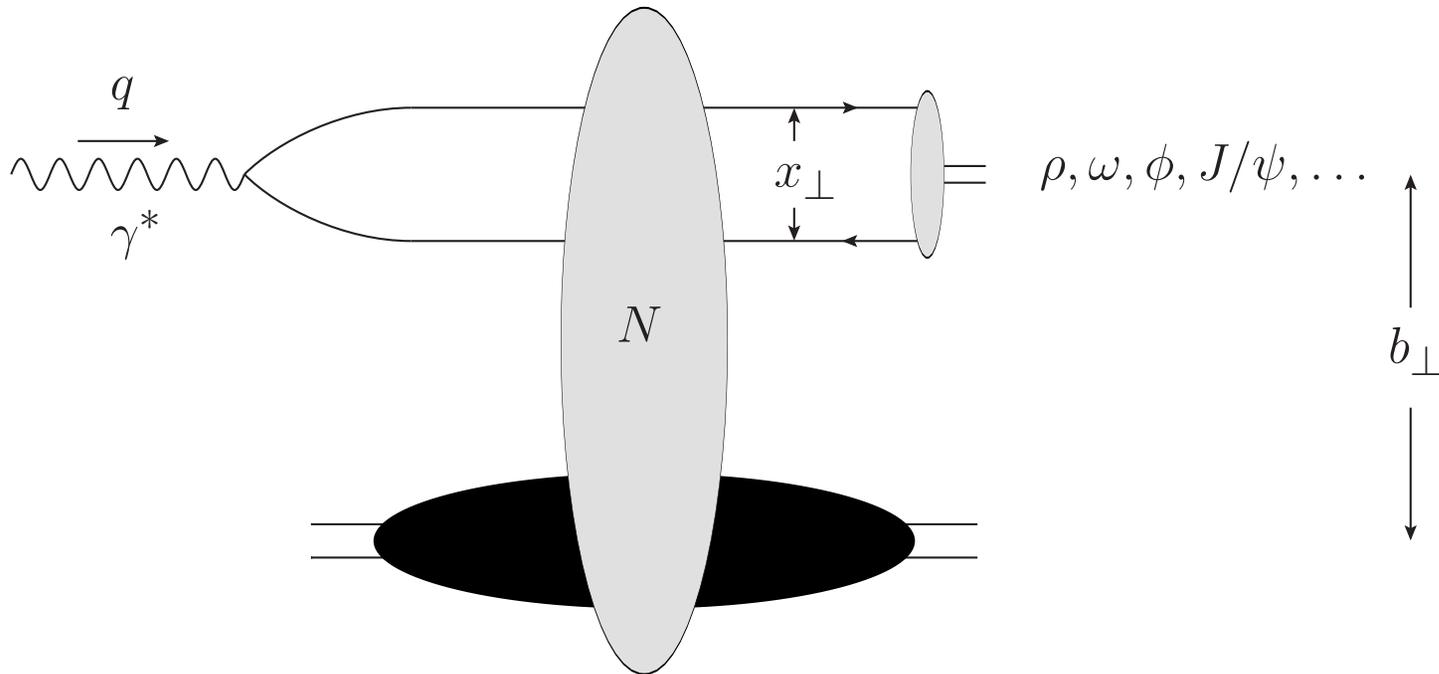


sat = Kowalski et al '08, plots generated by Marquet

no-sat = Leading Twist Shadowing (LTS), Frankfurt, Guzey, Strikman '04, plots by Guzey

# Exclusive Vector Meson Production

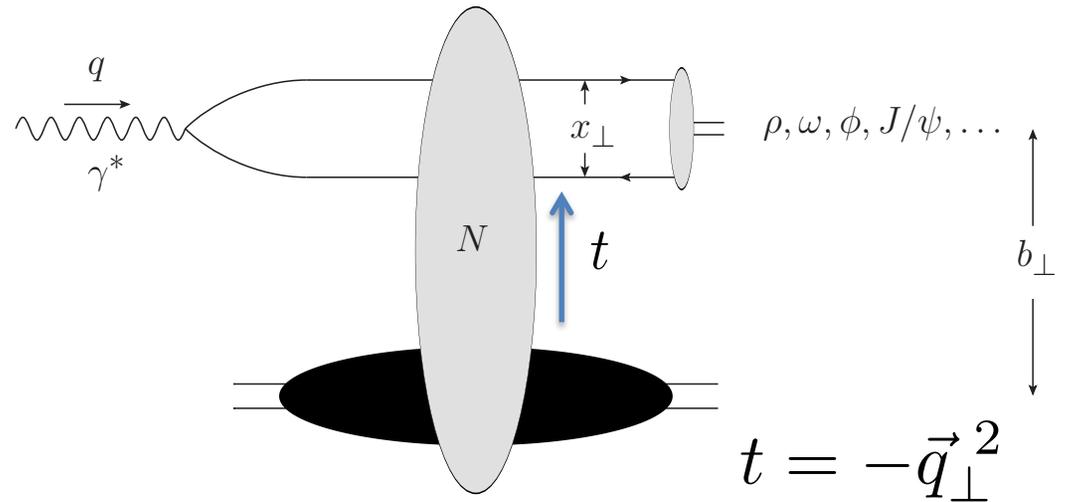
- An important diffractive process which can be measured at EIC is exclusive vector meson production:



# Exclusive VM Production: Probe of Spatial Gluon Distribution

- Differential exclusive VM production cross section is

$$\frac{d\sigma^{\gamma^*+A\rightarrow V+A}}{dt} = \frac{1}{4\pi} \left| \int d^2b e^{-i\vec{q}_\perp \cdot \vec{b}_\perp} T^{q\bar{q}A}(\hat{s}, \vec{b}_\perp) \right|^2$$



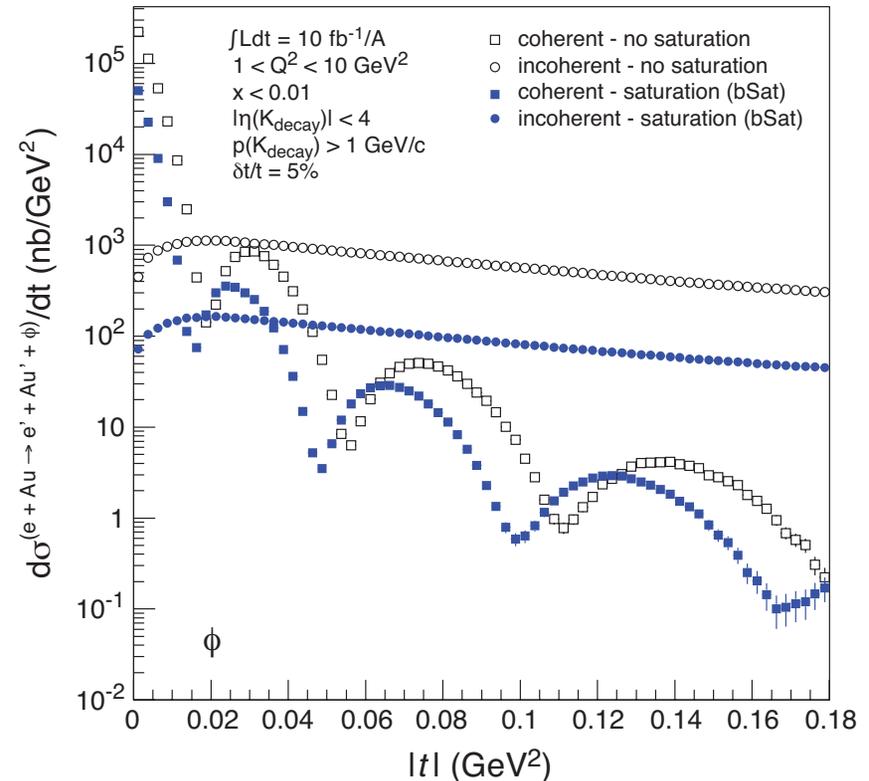
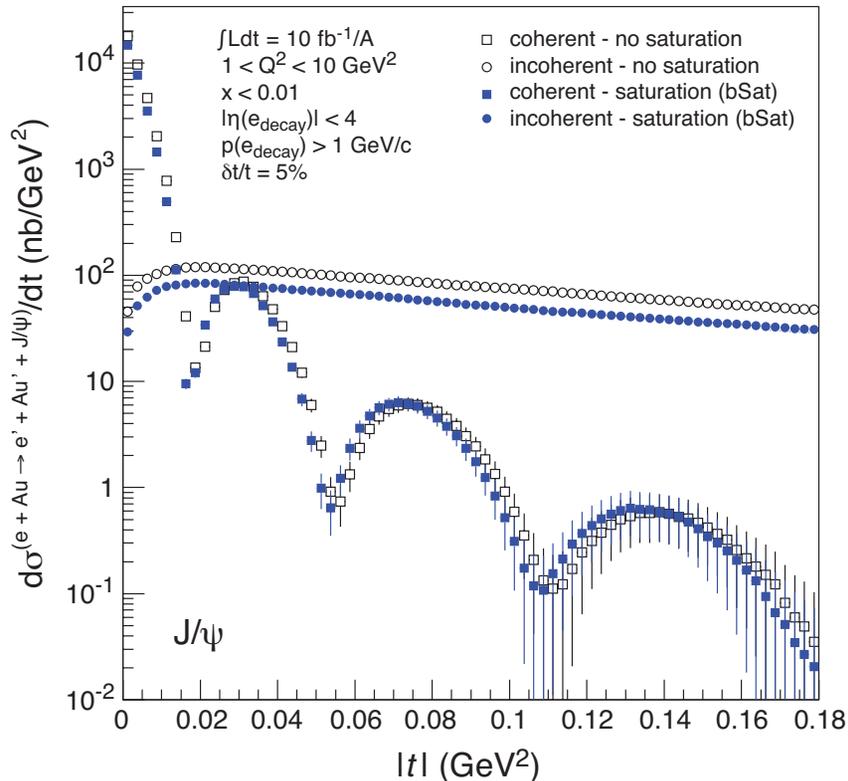
- the T-matrix is related to the dipole amplitude N:

$$T^{q\bar{q}A}(\hat{s}, \vec{b}_\perp) = i \int \frac{d^2x_\perp}{4\pi} \int_0^1 \frac{dz}{z(1-z)} \Psi^{\gamma^* \rightarrow q\bar{q}}(\vec{x}_\perp, z) N(\vec{x}_\perp, \vec{b}_\perp, Y) \Psi^V(\vec{x}_\perp, z)^*$$

Brodsky et al '94, Ryskin '93

- Can study t-dependence of the  $d\sigma/dt$  and look at different mesons **to find the dipole amplitude  $N(x,b,Y)$**  (Munier, Stasto, Mueller '01).
- Learn about the **gluon distribution in space**.

# Exclusive VM Production as a Probe of Saturation

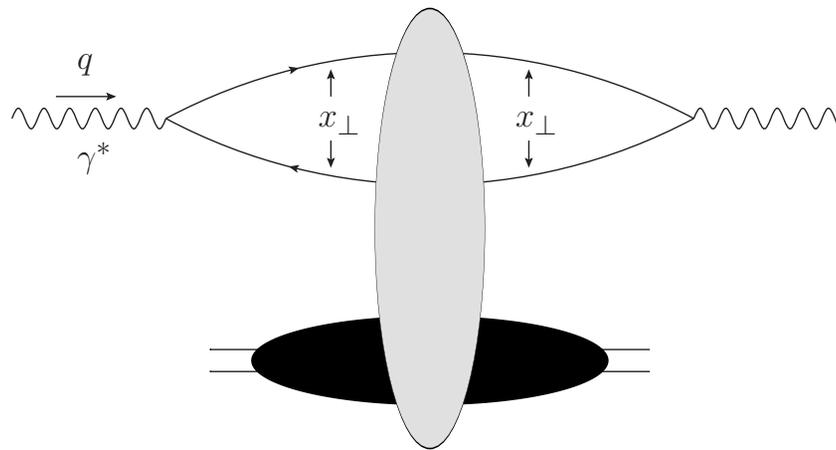


Plots by T. Toll and T. Ullrich using the Sartre event generator (b-Sat (=GBW+b-dep+DGLAP) + WS + MC).

- J/psi is smaller, less sensitive to saturation effects
- Phi meson is larger, more sensitive to saturation effects

# Dipole Amplitude and Other Operators

- Dipole scattering amplitude is a universal degree of freedom in saturation physics.
- It describes the total DIS cross section and structure functions:



- It also describes single inclusive quark and gluon production cross sections in DIS and in p+A collisions. <- **Universality!**
- Works for diffraction in DIS and p+A. <- **Universality!**
- For correlations need also quadrupoles (J.Jalilian-Marian, Yu.K. '04; Dominguez et al '11) and other Wilson line operators.

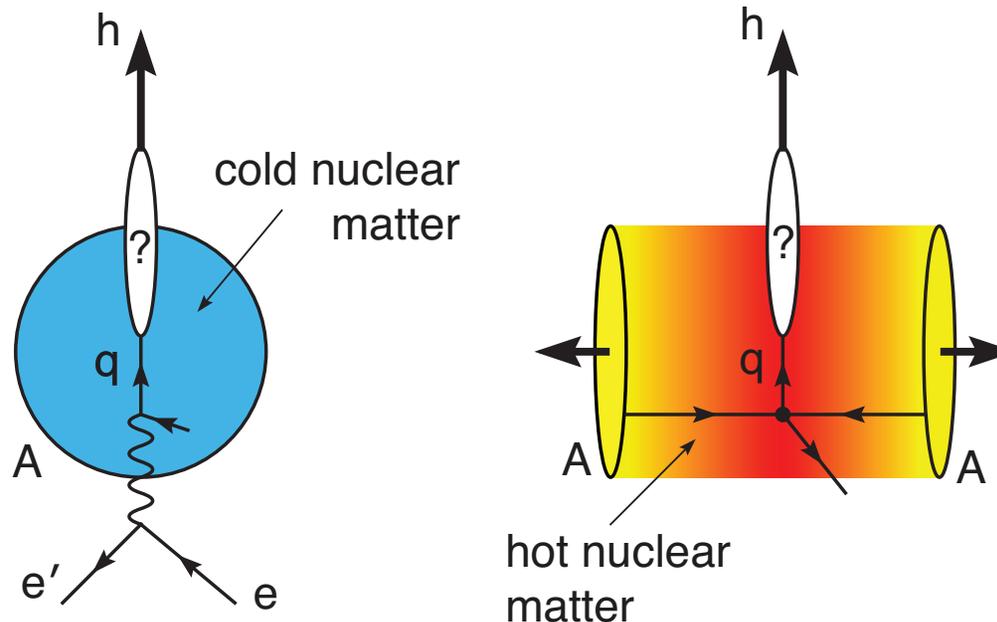
# Large-x Physics in e+A

# e+A at Large-x

- In e+A at EIC one could measure quark and gluon distributions (PDFs, GPDs, TMDs) and determine their spatial distributions at all values of Bjorken-x.
- We would also learn more about the properties of hadron formation in the cold nuclear matter.

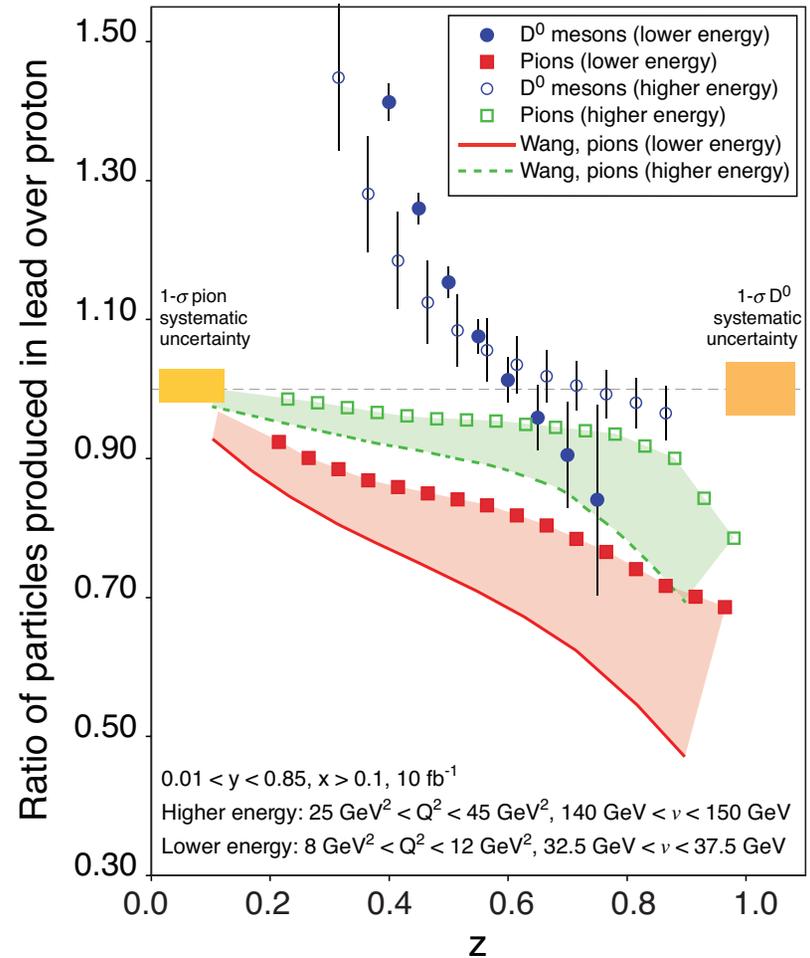
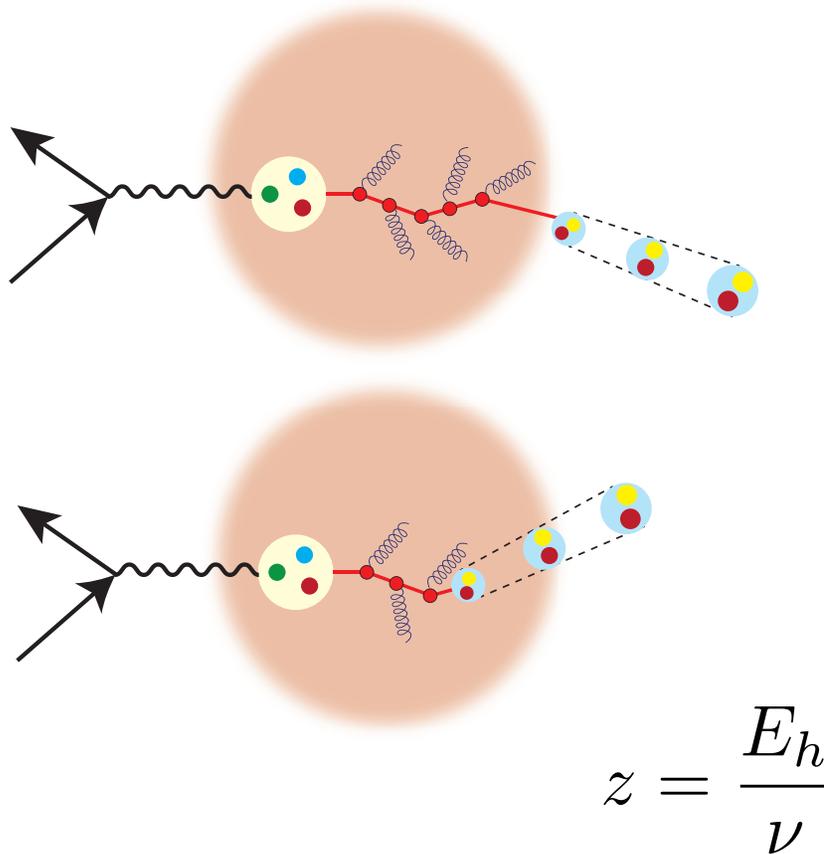
# Energy Loss in Cold Nuclear Matter

- EIC would be able to measure the energy loss of quarks in a cold nuclear matter, complementing the RHIC and LHC measurements of energy loss in hot QCD plasma:



# Energy Loss in Cold Nuclear Matter

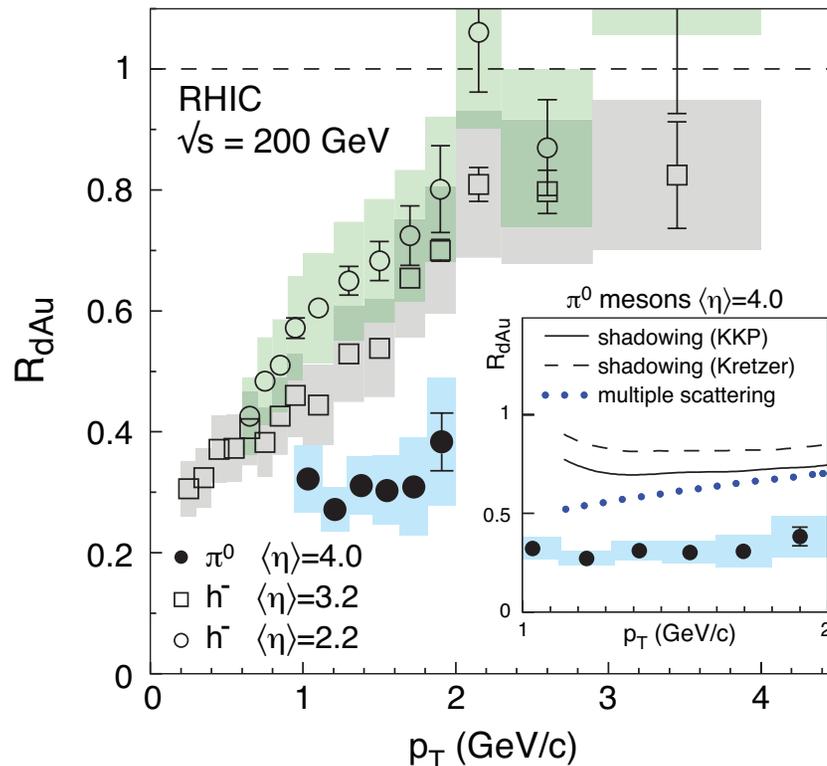
- By studying quark propagation in cold nuclear matter we can learn important information about hadronization and may even measure  $q_{had}$  in the cold nuclear medium:



# Connections to p+A and A+A collisions

# Connections to p+A

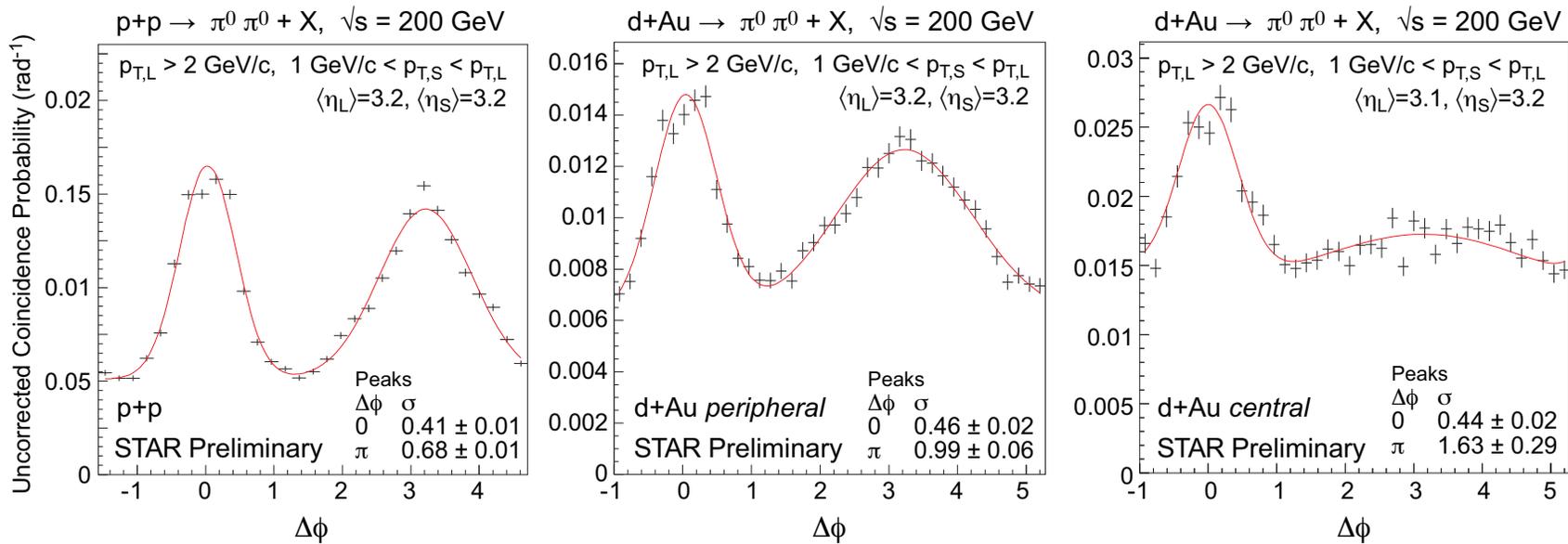
- In the saturation framework particle production in p+A is described by the dipole amplitude, just like structure functions in DIS. (**Universality!**)
- Correlations in both processes are described by other Wilson line operators like quadrupoles. (**Universality!**)
- Some evidence of saturation has been seen in d+Au collisions at RHIC:



$$R_{pA} = \frac{1}{N_{coll}} \frac{dN^{pA} / d^2 p_T dy}{dN^{pp} / d^2 p_T dy}$$

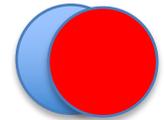
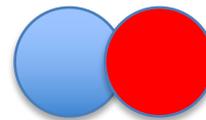
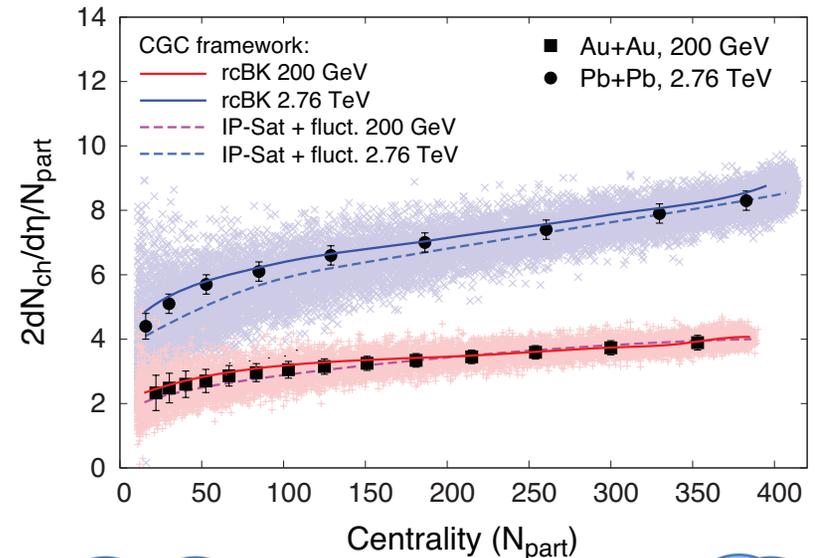
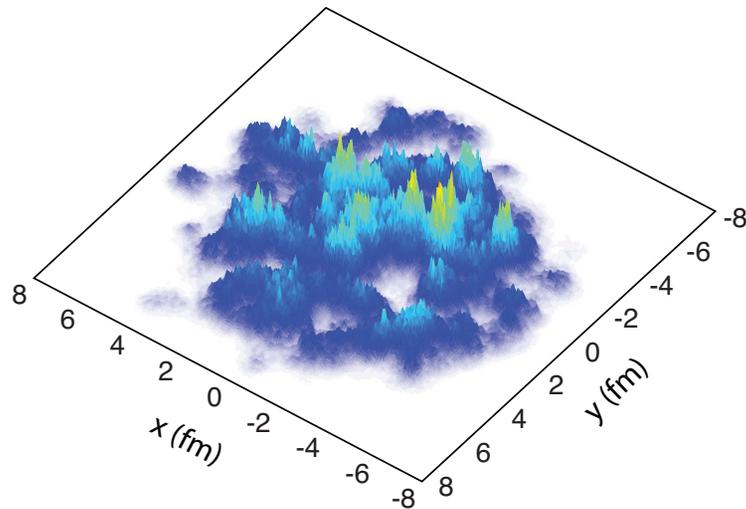
# Connections to p+A

Di-hadron back-to-back azimuthal correlation function decorrelates for central d+Au collisions in agreement with saturation predictions (cf. e+A):



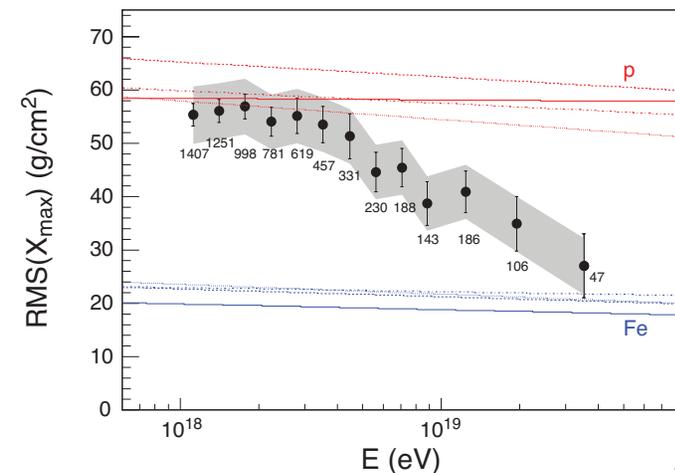
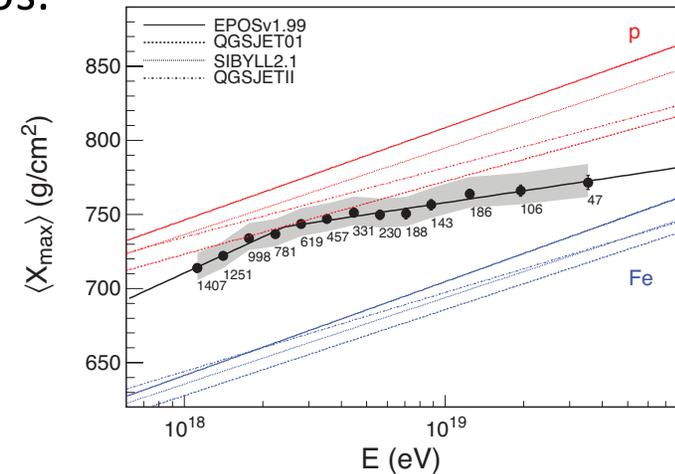
# Connections to Heavy Ion Physics

- CGC Physics also plays important role in the early-time dynamics of heavy ion collisions
- By exploring it at EIC we would get a better handle on formation of QGP and on fluctuations, including multiplicity and azimuthal harmonic flow coefficients  $v_n$ .



# Connections to Cosmic Rays

- There is a known problem in Auger data indicating that cosmic rays behave like protons at lower energies and like nuclei at higher energies, according to the existing QCD Monte-Carlos.
- $X_{\max}$  = atmospheric depth of the cosmic ray shower maximum
- It could be that the problem is with our understanding of QCD at this super-high energies.
- Perhaps saturation physics, with input from EIC, could help improve our understanding of the Auger data.



# Conclusions

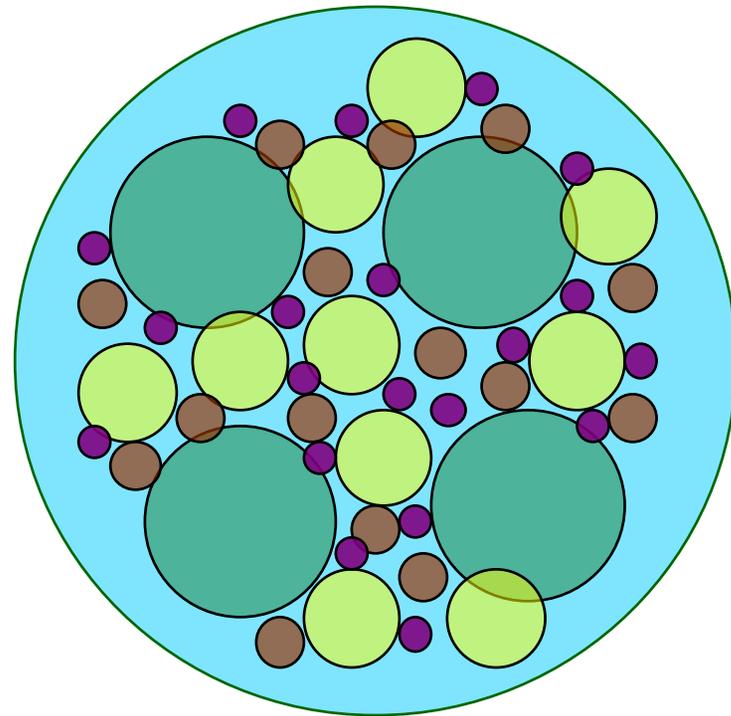
- EIC would allow to map out the spin structure of the proton, helping **resolve the spin crisis**.
- EIC would measure **quark and gluon distributions both as functions of  $x$  and  $k_T$** , for nucleons and nuclei.
- EIC would help us understand **spatial distribution of gluons and quarks** in the nucleons and nuclei.
- EIC is a unique opportunity to complete the **discovery of saturation/CGC physics** and to study its properties. By discovering saturation, we would make a significant progress in **understanding high-energy QCD**, answering one of the fundamental questions in the field and paving the way for better understanding of strong interactions at the future accelerators.

# Backup Slides

# Nonlinear Evolution at Work

- ✓ First partons are produced overlapping each other, all of them about the same size.
- ✓ When some critical density is reached no more partons of given size can fit in the wave function. The proton starts producing smaller partons to fit them in.

Proton



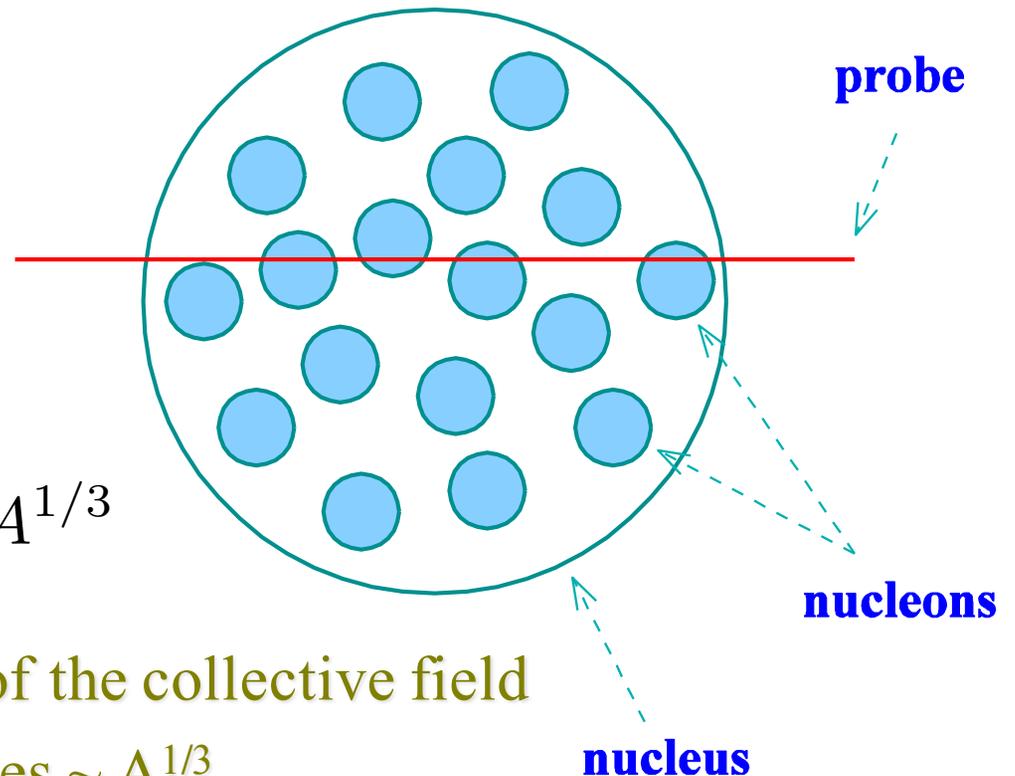
**Color Glass Condensate**

# Saturation Scale

To argue that  $Q_S^2 \sim A^{1/3}$  let us consider an example of a particle scattering on a nucleus. As it travels through the nucleus it bumps into nucleons. Along a straight line trajectory it encounters  $\sim R \sim A^{1/3}$  nucleons, with  $R$  the nuclear radius and  $A$  the atomic number of the nucleus.

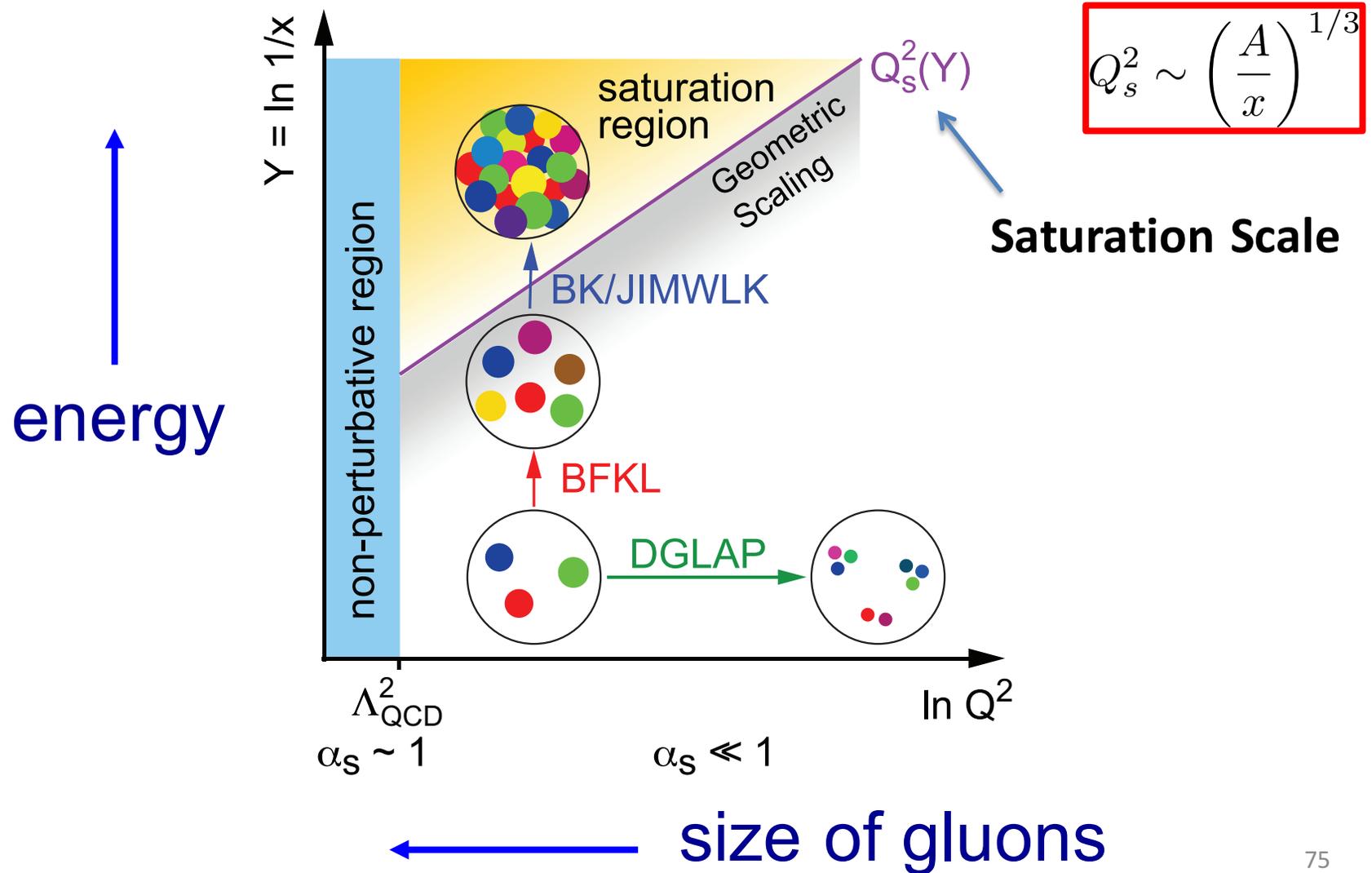
The particle receives  $\sim A^{1/3}$  random kicks. Its momentum gets broadened by

$$\Delta k \sim \sqrt{A^{1/3}} \Rightarrow (\Delta k)^2 \sim A^{1/3}$$

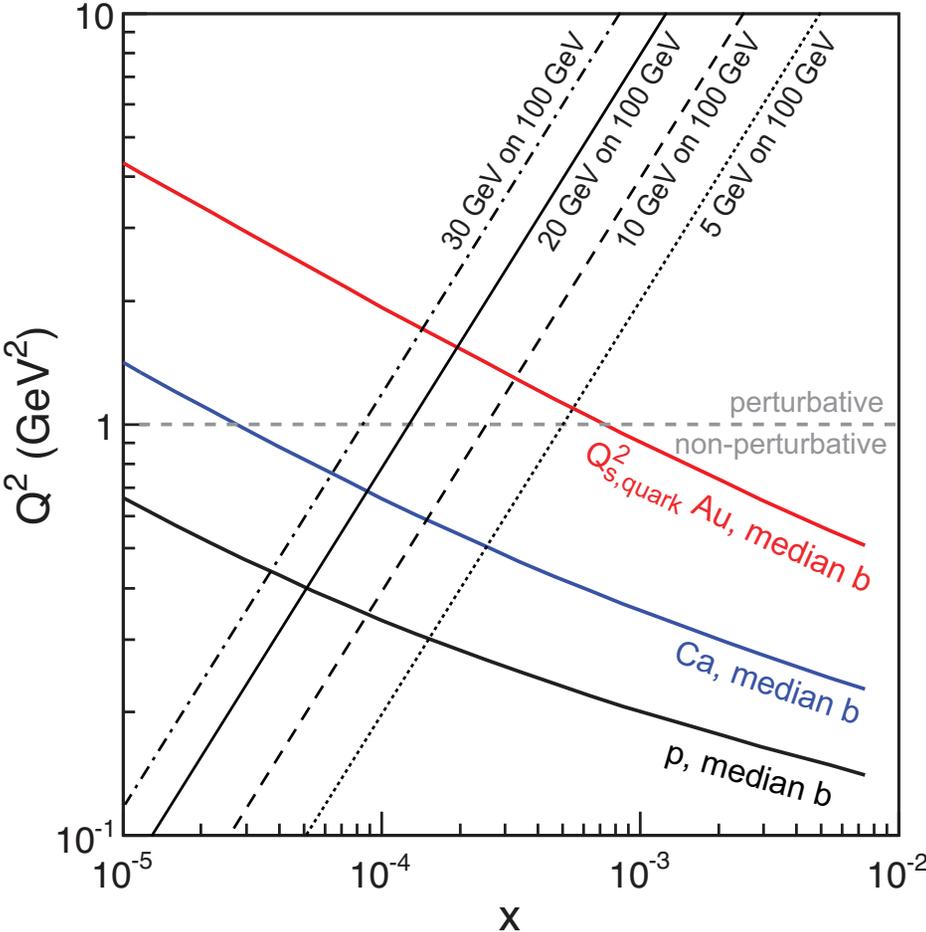


Saturation scale, as a feature of the collective field of the whole nucleus also scales  $\sim A^{1/3}$ .

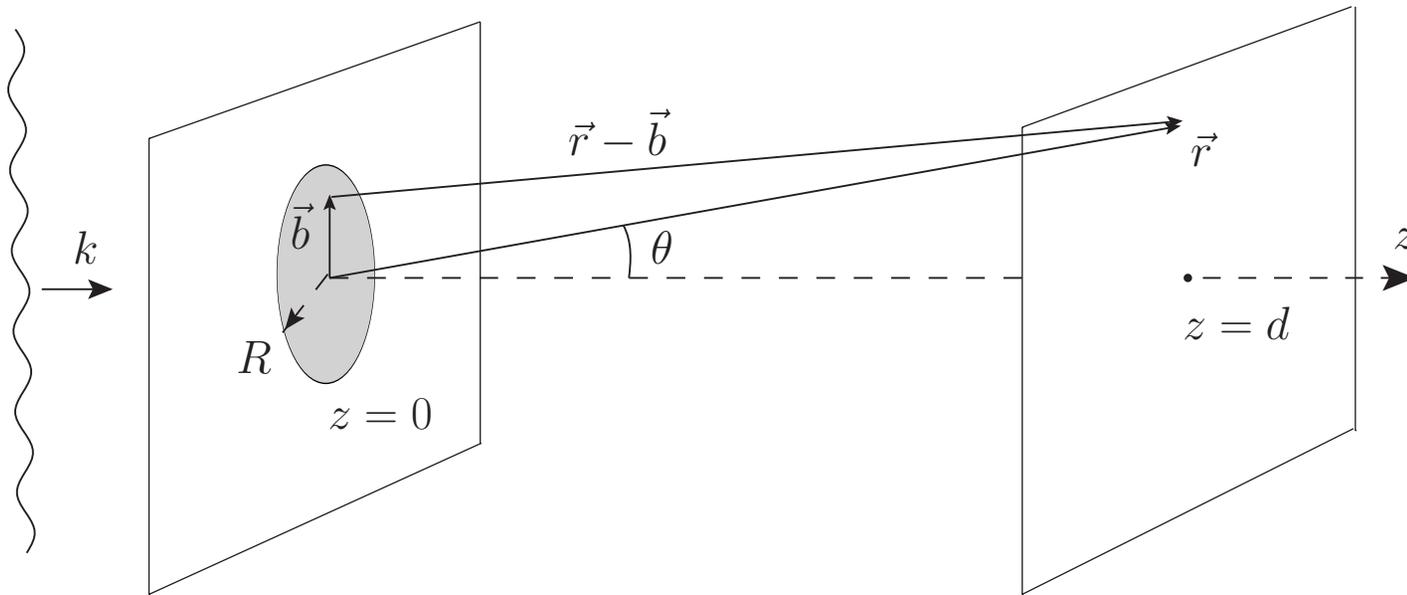
# Map of High Energy QCD



# Saturation Scales at EIC



# Diffraction in optics and QCD



- In optics, diffraction pattern is studied as a function of the angle  $\theta$ .
- In high energy scattering the diffractive cross sections are plotted as a function of the Mandelstam variable  $t = k \sin \theta$ .

# Impact Parameter Dependence

- Using exclusive VM production one can study the b-dependence of the T-matrix since inverting the above formula one gets (Munier, Stasto, Mueller '01)

$$T^{q\bar{q}A}(\hat{s}, \vec{b}_\perp) = \frac{i}{2\pi^{3/2}} \int d^2q e^{i\vec{q}_\perp \cdot \vec{b}_\perp} \sqrt{\frac{d\sigma^{\gamma^* + A \rightarrow V + A}}{dt}}$$

- The amplitude T is related to N and to the vector meson and  $\gamma^*$  wave functions:

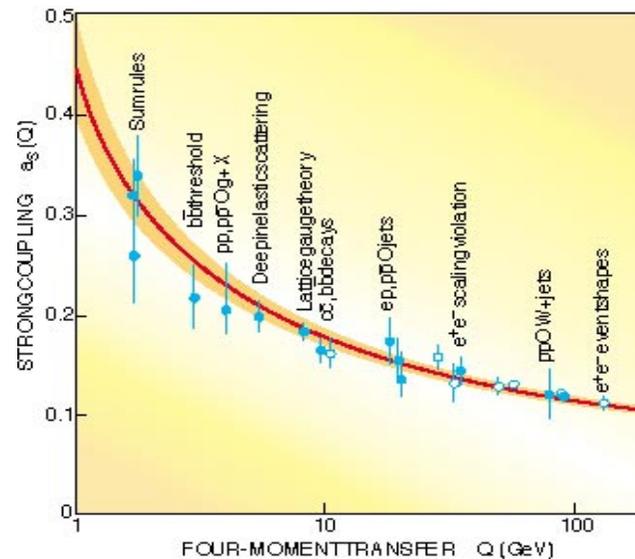
$$T^{q\bar{q}A}(\hat{s}, \vec{b}_\perp) = i \int \frac{d^2x_\perp}{4\pi} \int_0^1 \frac{dz}{z(1-z)} \Psi^{\gamma^* \rightarrow q\bar{q}}(\vec{x}_\perp, z) N(\vec{x}_\perp, \vec{b}_\perp, Y) \Psi^V(\vec{x}_\perp, z)^*$$

- Diffraction (elastic VM production) can help us figure out the b-dependence of the T-matrix, and hence see if saturation has been reached. It would also give us the b-dependent gluon distribution in the nucleus.

# Strong Coupling Scenarios

# Strong Coupling

- What if the realistic saturation scale at the EIC is not large enough for the coupling to be small?



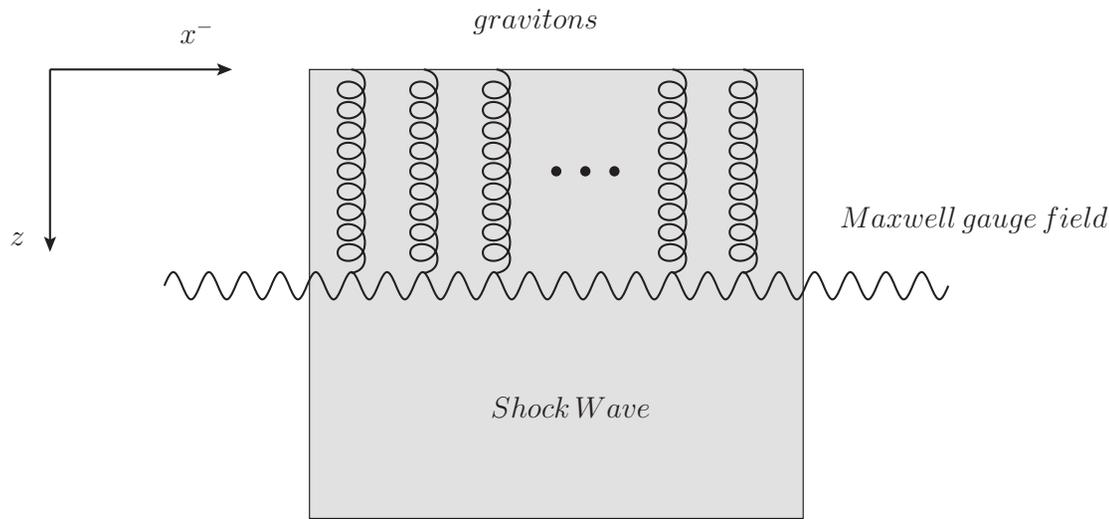
- The theoretical tool would then be AdS/CFT correspondence.
- Problems: N=4 SYM is not QCD, not clear how to obtain QCD in a controlled way; there is no E&M current in N=4 SYM, hence not clear what to calculate to describe DIS, etc.

# DIS in AdS/CFT: Currents Correlator

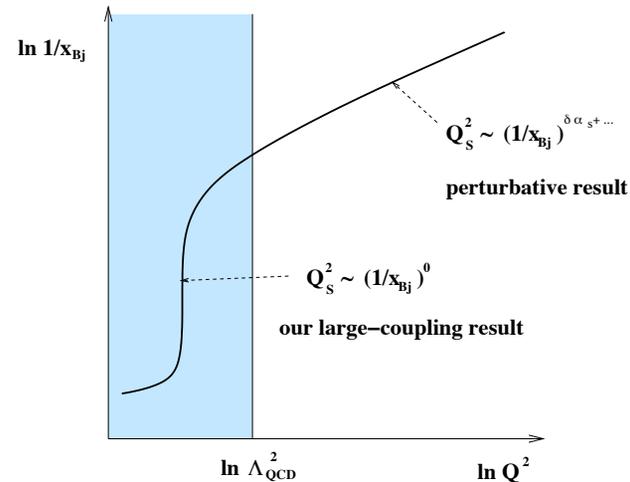
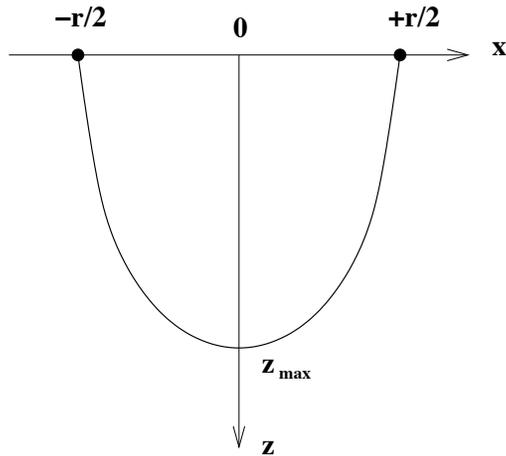
- DIS can be modeled in AdS/CFT by calculating correlator of two  $R$ -currents in the background of a thermal medium or a shock wave (Levin et al '08, Mueller et al '08, Avsar et al '09). The saturation scale is then

$$Q_s^2 \sim \Lambda^2 \frac{A^{1/3}}{x}$$

- Very fast  $x$ -dependence, such scale has not been observed. Moreover, if it grows with  $x$  this fast, it would quickly get into pQCD region making the couplings small...



# DIS in AdS/CFT: Dipole Amplitude



- One can directly calculate the dipole amplitude in DIS obtaining (Albacete et al '08)

$$Q_s^2 \sim \lambda \Lambda^2 A^{2/3}$$

(more plausible x-dependence (none), but strong A-dependence – not observed)

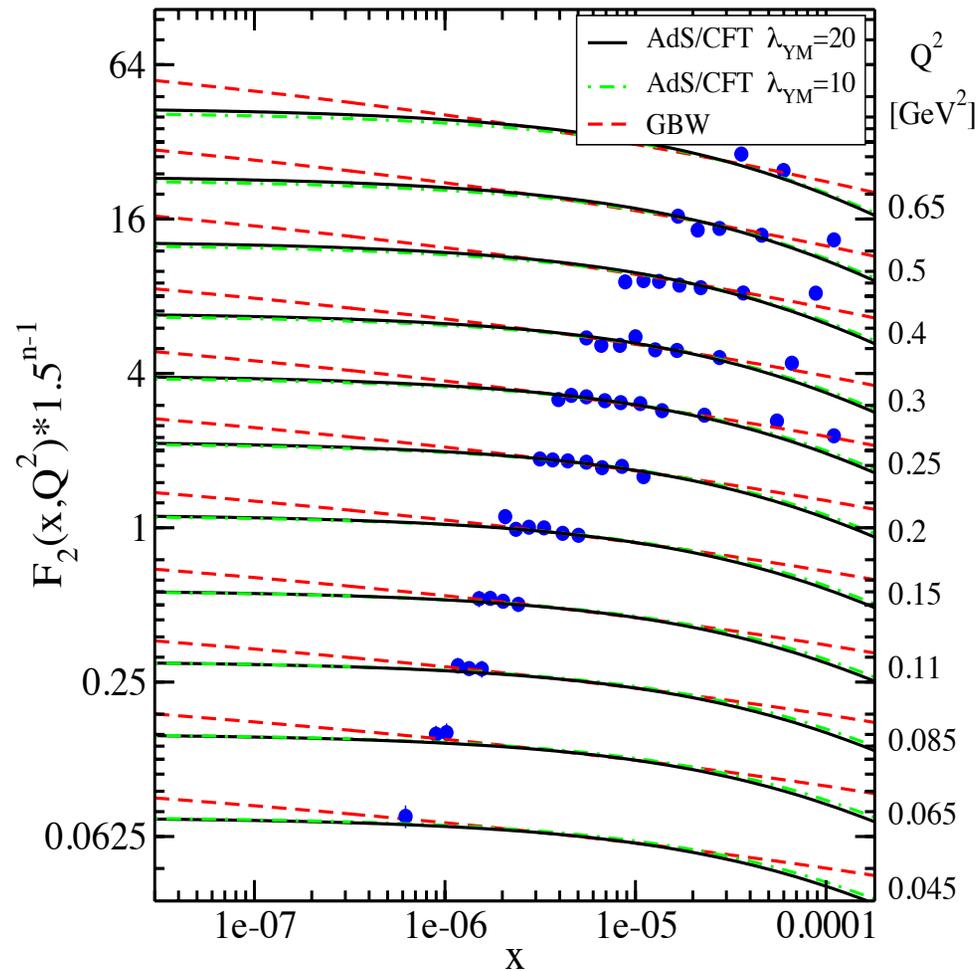
- or (Dumitru and Noronha '14, more realistic A-dependence)

$$Q_s^2 \sim \lambda \Lambda^2 A^{1/3}$$

- More work is needed to sort things out. This may be an opportunity.

# AdS/CFT vs the Data

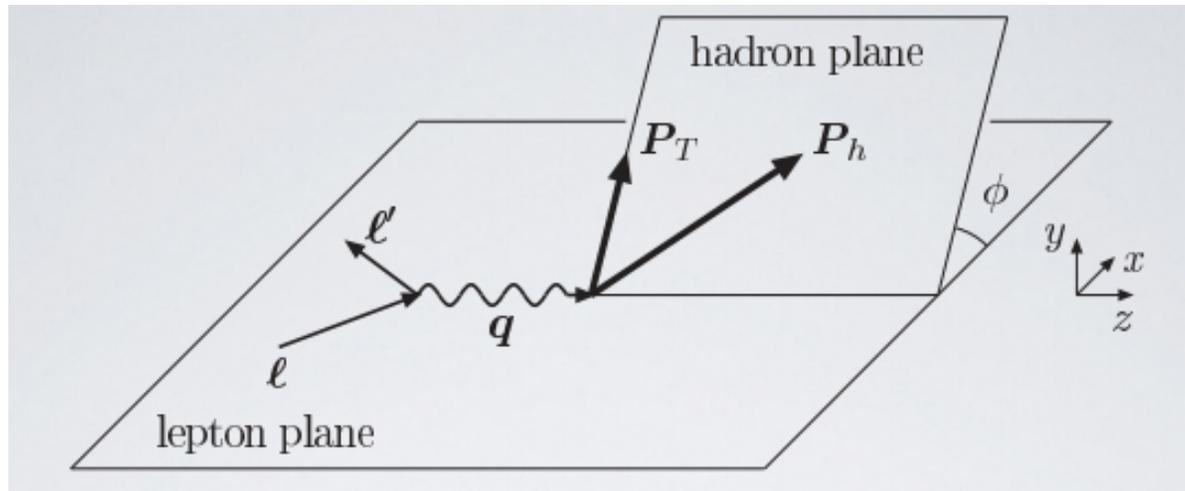
- One can describe the low- $Q^2$   $F_2$  HERA data using AdS/CFT approach (YK, Lu, Rezaeian, '09):



# Strong vs Weak Coupling

- Can experiments distinguish between strongly vs weakly-coupled saturation scenarios at an EIC?
- This is largely an open question.
- Purely large-coupling scenario at all momentum scales unlikely – in heavy ions AdS predicts stopping of heavy ions in the collision (not observed at RHIC or LHC) and very strong growth of hadron multiplicity with energy. Most likely early-time dynamics in A+A is weakly-coupled.
- A combination of weakly and strongly-coupled dynamics is possible at an EIC since  $Q_s$  is not huge. This would be hard to tackle theoretically.

# Strong Color Fluctuations



One could study the  $p_T$ -broadening of produced hadrons in DIS on a nucleus as a function of the angle  $\phi$  between the lepton and hadron planes. The broadening

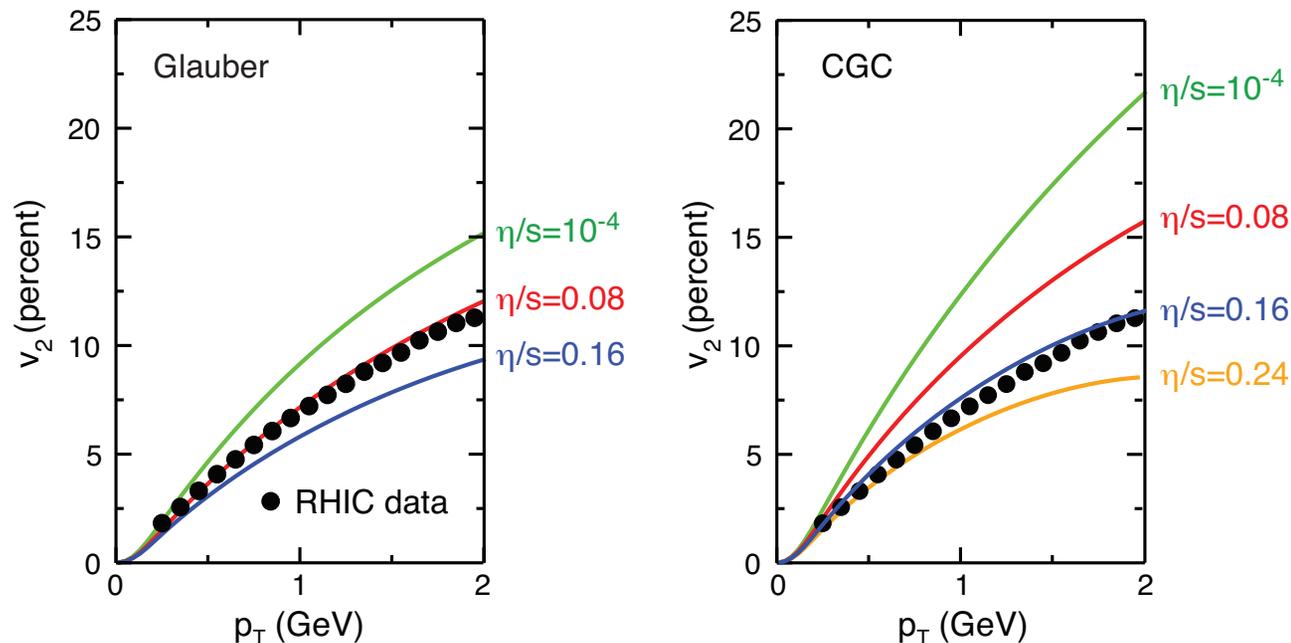
$$\langle \Delta p_T^2(\phi) \rangle_{AN} = \langle p_T^2(\phi) \rangle_A - \langle p_T^2(\phi) \rangle_N$$

would be sensitive to strong color fluctuations in the density of partons.

# Connections to Heavy Ion Physics

Harmonic flow coefficients are sensitive probes of the dynamics of quark-gluon plasma and the initial conditions for its formation:

$$\frac{dN}{d\phi} = \frac{N}{2\pi} \left[ 1 + \sum_n 2 v_n \cos(n\phi) \right]$$



A comparison of data vs theory using viscous hydrodynamics with Glauber-like initial conditions (left) or the saturation-inspired ones (right).